

# The Selective Disclosure of Evidence

## An Experiment

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In many settings, agents communicate by disclosing **selected evidence**:

- A *job candidate* selects which experiences to list in her vitae
- A *journalist* selects which facts to include in an article
- A *scientist* selects which results to present in a paper
- A *lawyer* selects which evidence to subpoena for a trial
- A *company* selects which product features to highlight in an ad

These examples have three distinguishing features:

- Evidence is **verifiable**: Sender does not fabricate it
- Evidence is **noisy**: A piece of evidence may not fully reveal the state
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Yet, **selective disclosure** seems pervasive force in communication

We build on a small theory literature in communication that studies disclosure of noisy evidence

We develop new comparative statics to inform parsimonious experimental design

We experimentally investigate how subjects deal with **selective disclosure**:

- Which evidence do senders select to disclose?
- How do receivers respond to evidence that may be selected?
- How does their behavior impact communication overall?

Builds on Milgrom (1981)

- Sender has private information about a state of the world
- Sender receives  $N$  private signals that are informative about the state
- Sender can disclose up to  $K$  of these signals to the Receiver
- Receiver observes disclosed signals and guesses the state

Treatment variations consist of changing  $K$  and  $N$ : a rich set of predictions

Data corroborates main qualitative predictions of the theory

1. Senders overwhelmingly engage in **selective disclosure**

*Main deviation:* A minority of senders is “deception averse”

2. Receivers account for **selection bias**, i.e., for the fact that evidence they see is selected

*Main deviation:* Often not as much as they should

3. Aggregate effects on communication are in line with prediction

*Main deviation:* Some quantitative departures still to explore



## The Basic Setting:

- ▶ Milgrom (1981, Bell), information unraveling
- ▶ Fishman and Hagerty (1990, QJE), optimal amount of discretion
- ▶ Di Tillio, Ottaviani and Sorensen (2021, Ecma), effect of selection on information transmission

## Mechanism-Design Approach:

- ▶ Glazer and Rubinstein (2004, Ecma) – receiver's verification
- ▶ Glazer and Rubinstein (2006, TE) – sender's verification

## Richer Settings

- ▶ Shin (2003, Ecma): uncertainty over available evidence
- ▶ Dziuda (2011, JET): unknown sender's preferences

## Disclosure:

- ▶ Jin, Luca and Martin (2022, AEJ: Micro) – failure of unravelling and why
- ▶ Hagenbach and Perez-Richet (2018, GEB) – preference alignment
- ▶ Li and Schipper (2020, GEB) – vague disclosure
- ▶ Frechette, Lizzeri and Perego (2022, Ecma) – partial commitment

## Cheap Talk:

- ▶ Cai and Wang (2006, GEB) – overcommunication wrt the theory
- ▶ Blume, Lai and Lim (2020, Handbook of Experimental GT) - review

## Partially Verifiable Disclosure

- ▶ Burdea, Montero, Sefton (2023, GEB) – Glazer and Rubinstein ('04, '06)
- ▶ Li and Schipper (2018) – asymmetric info on the amount of evidence
- ▶ Penczynski, Koch and Zhang (2023) – selection and competition

**model**

Milgrom (1981, §7)

Sender privately observes the state  $\theta \in \Theta$ :

- $\Theta$  finite and ordered,  $p \in \Delta(\Theta)$  common prior

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Receiver observes the message  $m$  and takes an action  $a \in A$

Given state  $\theta$  and action  $a$ ,

– Receiver's payoff is  $u(\theta, a) = -(a - \theta)^2$

wants to guess the state

– Sender's payoff is  $v(\theta, a) = a$

higher actions preferred



More formally, message space is

$$\mathcal{M} = \{\emptyset\} \cup \{\bar{s} \in S^k \mid 1 \leq k \leq K \text{ and } \bar{s}_i \geq \bar{s}_j \text{ for } i \leq j\}$$

Verifiability requires that Sender can only disclose signals that belong to  $\bar{s}$ :

$$m \in M(\bar{s}) = \{m' \in \mathcal{M} \mid \text{if } m' \neq \{\emptyset\}, \exists 1 \leq k \leq K \text{ and an injective} \\ \rho : \{1, \dots, k\} \rightarrow \{1, \dots, N\} \text{ s.t. } m' = (\bar{s}_{\rho(1)}, \dots, \bar{s}_{\rho(k)})\}$$

To fix ideas, suppose signal space is  $S = \{A, B, C, D\}$  and  $N = 4$

Suppose available signals are  $\bar{s} = (A, B, D, D)$

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If  $K = 1$

- $M(\bar{s}) = \{\emptyset, A, B, D\}$

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Suppose available signals are  $\bar{s} = (A, B, D, D)$

If  $K = 2$

$$- M(\bar{s}) = \{\emptyset, A, B, D, AB, AD, BD, DD\}$$

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If  $K < N$ , Sender faces **exogenous communication constraint**,  $\bar{s} \notin M(\bar{s})$

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Changes in  $(K, N)$  span models from disclosure to cheap talk

**equilibrium**

# Equilibrium

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Analysis focuses on pure-strategy **PBEs** in which sender's strategy does not depend on  $\theta$

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When  $K < N$ , game admits multiple equilibrium outcomes

We refine PBEs using a notion of **neologism proofness** (Farrel '93) that we adapted to our setting with verifiable information

Under this refinement, we show that our theory predicts a **unique** equilibrium outcome

# Equilibrium

## Definition

A sender's strategy is **maximally selective** if, given each  $\bar{s}$ , she discloses the  $K$  highest signals

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## Theorem

There exists a pure-strategy PBE in which the sender plays a maximally selective strategy.

Moreover, the induced outcome is the unique one in the class of neologism-proof equilibrium outcomes.

**comparative statics**

We study the effects of changing  $N$  and  $K$  on **equilibrium informativeness**

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$$\mathcal{I}(K, N) = \mathbb{V}(\theta) - \mathbb{E}(\mathbb{V}(\theta|m))$$

$\mathcal{I}(K, N)$  is a monotone transformation of **correlation** btw  $\theta$  and  $a$

## Proposition 1

Equilibrium informativeness increases in  $K$

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### Intuition

- ▶ Easier to send messages that other types cannot imitate
- ⇒ Less pooling
- ⇒ More information transmitted

## Proposition 2

Assume  $K = N$ . Equilibrium informativeness increases in  $N$ .

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## Proposition 3

Suppose  $f(\cdot|\theta)$  has full support for every  $\theta$ .

Equilibrium informativeness decreases to zero as  $N \rightarrow \infty$ .

Moreover, equilibrium informativeness needs not be monotonic in  $N$ .

**Intuition:** Increasing  $N$  generates two contrasting effects:

## Imitation Effect

- Sender can cherry pick more effectively, making higher signals less informative

## Separation Effect

- Sender has more evidence to prove her type
- Selection contains information about undisclosed signals: “lower” signals are more informative



## Example: Conclusive Good News

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$\theta_L$	$\eta$	$1 - \eta$
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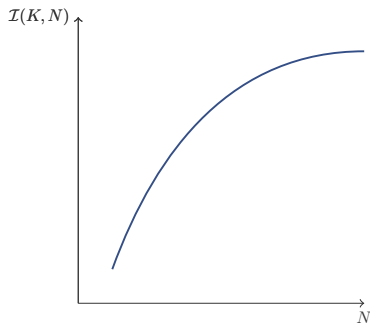
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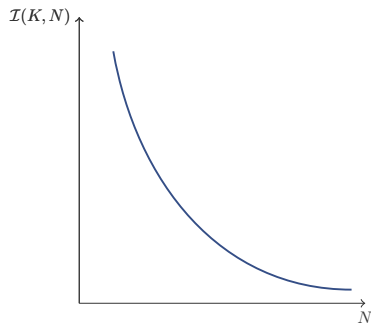
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$\mathcal{I}(K, N)$  = more complex

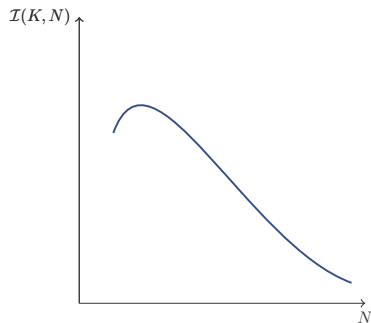
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**experiment**

Binary state: Yellow Urn ( $\theta_L$ , “low” state) and Red Urn ( $\theta_H$ , “high” state)

Signal space:  $S = \{A, B, C, D\}$

Information structure  $f$ :

State	Signal			
	$A$	$B$	$C$	$D$
$\theta_L$	10%	20%	25%	45%
$\theta_H$	45%	25%	20%	10%

Receiver's action  $a \in [0, 1]$

Since  $\Theta$  is binary and  $u_R(a, \theta) = -(a - \theta)^2$ , the receiver's task is equivalent to eliciting her beliefs via a quadratic scoring rule (QSR)

A large literature on belief elicitation has shown that QSR can be biased when subjects are not risk-neutral

To avoid this issue, we implement a binarized scoring rule *a la* Hossain and Okui ('13), which is robust to various risk preferences

	$N = 1$	$N = 3$	$N = 10$	$N = 50$
$K = 1$	$i$	$\cdot$	$ii$	$iii$
$K = 3$	$\cdot$	$iv$	$v$	$vi$

- Fixed roles
- 6 treatments, between subjects
- 4 sessions per treatment
- 30 rounds per session, random rematching
- 17.5 subjects per sessions on average
- Undergrad population Columbia and NYU: Spring, Summer, Fall 2023
- Average payout \$30 per subject

Round 7 of 30: Communication Stage

You are the Sender

Reminder:

If the secret Urn is **Yellow**, this is the probability of each ball being drawn:

A	B	C	D
10 %	20 %	25 %	45 %

If the secret Urn is **Red**, this is the probability of each ball being drawn:

A	B	C	D
45 %	25 %	20 %	10 %

The secret Urn is **Yellow**

Available Balls

2

2

1

5

A

B

C

D

+

+

+

+

-

-

-

-

Your message to the Receiver is:

☐

☐

☐

Send



Round 7 of 30: Communication Stage

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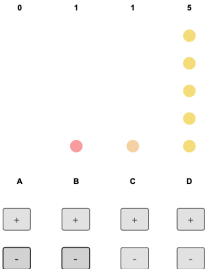
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The secret Urn is **Yellow**

Available Balls



Your message to the Receiver is:

A

A

B

Send

Round 7 of 30: Guessing Stage

You are the Receiver

Reminder:

If the secret Urn is **Yellow**, this is the probability of each ball being drawn:

A	B	C	D
10 %	20 %	25 %	45 %

If the secret Urn is **Red**, this is the probability of each ball being drawn:

A	B	C	D
45 %	25 %	20 %	10 %

The Sender had 10 available balls and they could disclose 3 or less. This is the Sender's message:



Use the slider below to indicate your Guess of how likely it is that the secret Urn is Red.

Your Guess: 10



Submit

**Round 7 of 30: Payoff**

**You are the Receiver**

The secret Urn was **Yellow**

In this Round you earned 100 points.

Continue

**How were your points determined?**

The secret Urn was Yellow. Your Guess was 10.

The two Computer's Random Numbers were 59 and 44.

Your Guess was smaller than or equal to the largest of the two Computer's Random Numbers, so you earned 100 points.

Round 7 of 30: Summary

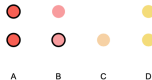
You are the Sender

## Sender's Summary

The secret Urn was **Yellow**

Available Balls

2      2      1      5



Sender's Message:



## Receiver's Summary

The Sender had 10 available balls and they could disclose 3 or less. This is the Sender's message:



Use the slider below to indicate your Guess of how likely it is that the secret Urn is Red.

Guess: 10



## Round 7 of 30: History

You are the Sender

Round	Secret Urn	Message	Guess
7	Yellow	A A B	10
6	Red	A A ○	77
5	Red	A B B	77
4	Red	A A A	97
3	Red	A A ○	87
2	Yellow	C C ○	52
1	Red	○ ○ ○	0

[Next](#)

# Testable Predictions

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**Senders:** Do senders engage in selective disclosure as predicted by equilibrium?

- E.g., do they play the maximally selective strategy?

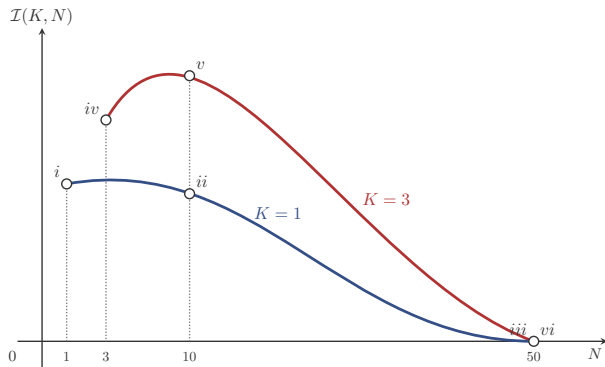
**Receivers:** Do receivers account for selection when responding to messages?

- E.g., do they become more skeptical of favorable messages as  $N$  increases?

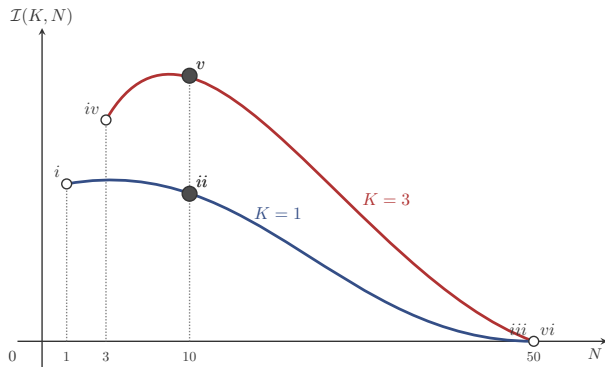
**Informativeness:** Are comparative statics corroborated by the data?

- Four statistical tests

# Testable Predictions: Informativeness



# Testable Predictions: Informativeness

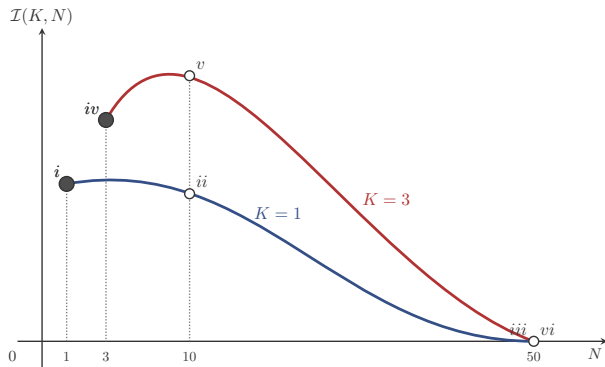


**Test 1.** Informativeness increases in  $K$

$$v > ii$$



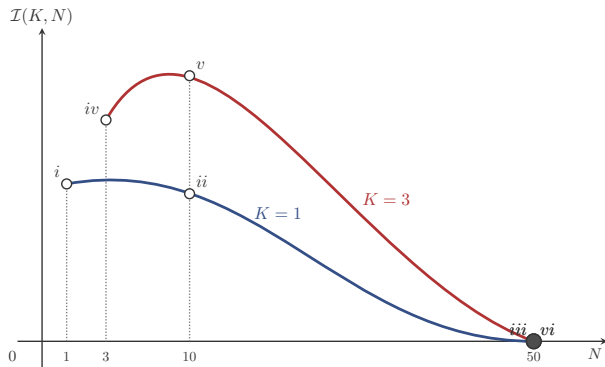
# Testable Predictions: Informativeness



**Test 2.** Fixing  $K = N$ , informativeness increases in  $N$

$$iv > i$$

# Testable Predictions: Informativeness

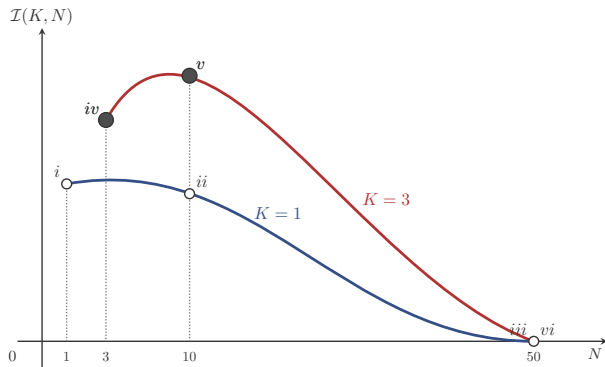


**Test 3.** Informativeness eventually decreases to 0 in  $N$

(imitation effect)

$$iii = vi = 0$$

# Testable Predictions: Informativeness



**Test 4.** If  $K = 3$ , informativeness initially increases in  $N$  (separation effect)

$$v > iv$$

**results**

**senders**

We begin by looking at Senders' behavior

## Goal.

- Investigate the extent to which senders engage in **selective disclosure**?

We present three facts about sender's behavior, from aggregate to disaggregate

How often do senders play the **maximally selective** strategy, i.e., disclose the  $K$  highest available signals?

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	pooled	$N = 1$	$N = 3$	$N = 10$	$N = 50$
$K = 1$	<b>83%</b>	80%	.	90%	79%
$K = 3$	<b>64%</b>	.	57%	74%	61%



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$K = 3$	<b>64%</b>	.	57%	74%	61%

Equilibrium behavior is predominant. Yet, many senders don't play equilibrium

What do they do? Need a more disaggregated approach

What messages are sent? Highly-dimensional problem.

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To make progress, we consider the “GPA” of a message, e.g.  $AAC \rightsquigarrow 3.3$

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If senders engage in selective disclosure, the GPA of messages sent should increase in  $N$

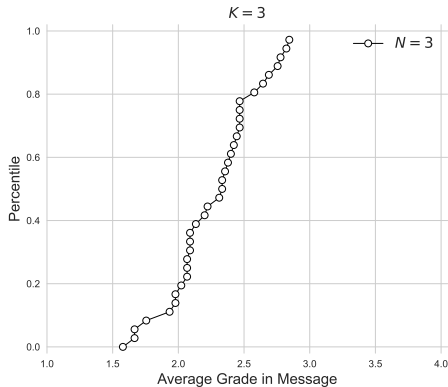
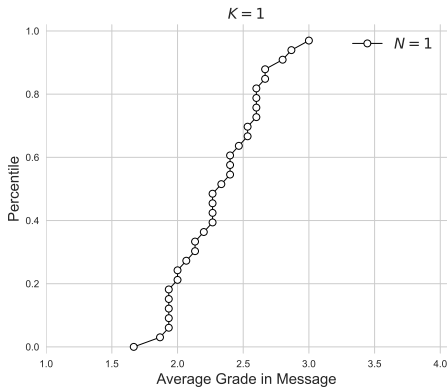
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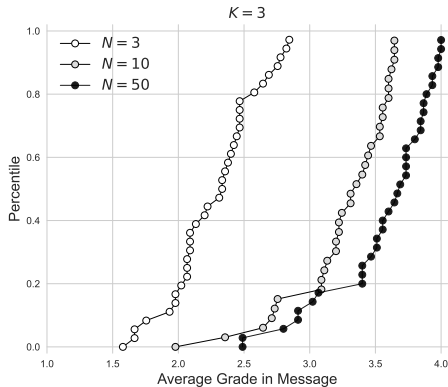
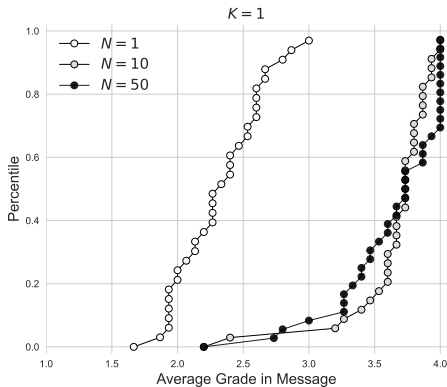
# Senders' Behavior (2/3)

results: senders



# Senders' Behavior (2/3)

results: senders



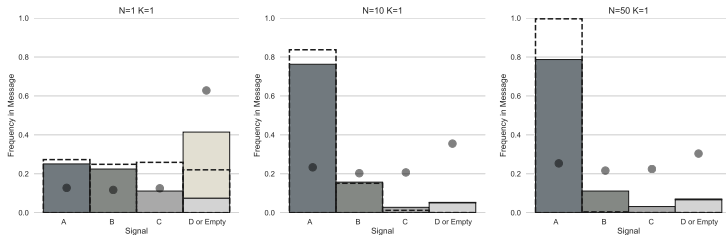
Finally, we can look at the *distribution* of signals that are disclosed

The frequency of  $A$ -signals should increase in  $N$



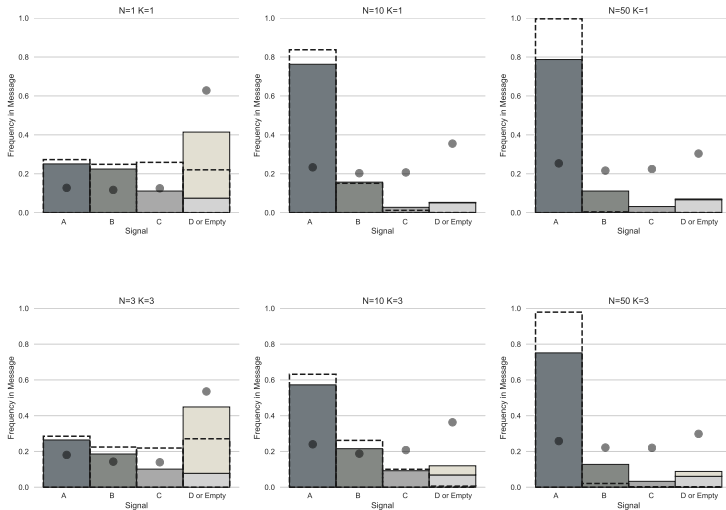
# Senders's Behavior (3/3)

results: senders



# Senders's Behavior (3/3)

results: senders



## Summary for Senders.

- We find that senders' behavior is consistent with the equilibrium force of **selective disclosure**
- Predominantly, Senders attempt to deceive receivers by selecting the most favorable evidence available to them

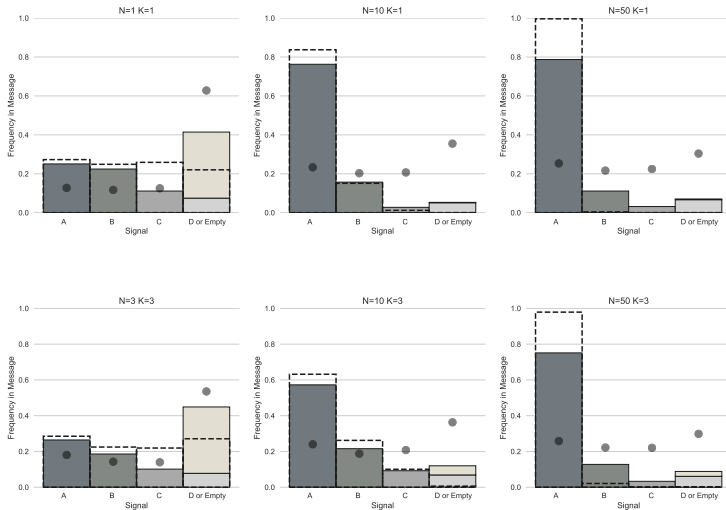
## Summary for Senders.

- We find that senders' behavior is consistent with the equilibrium force of **selective disclosure**
- Predominantly, Senders attempt to deceive receivers by selecting the most favorable evidence available to them

Yet, this behavior is not universal and we also see some **deception aversion**

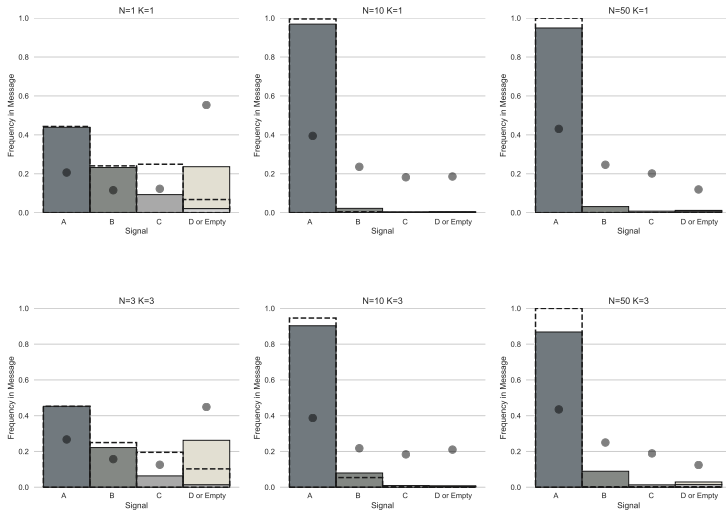
# Senders's Behavior: Missing As

results: senders



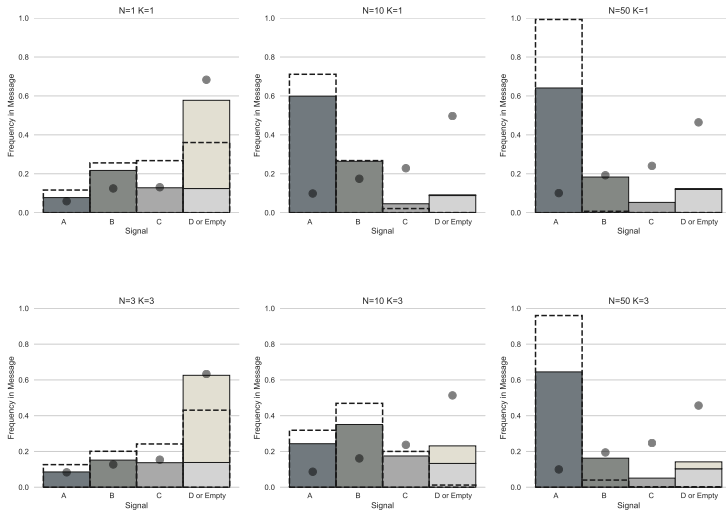
# Senders's Behavior: Missing As, $\theta_H$

results: senders



# Senders's Behavior: Missing As, $\theta_L$

results: senders



## Equilibrium type (56%)

- ▶ Most common
- ▶  $N > K$ : Mostly report best balls independently of the state
- ▶  $N = K$ : Disclose fewer than  $K$  balls

## Deception Averse Type (17%)

- ▶ A's reported more often when the state is high
- ▶ D's reported more often when the state is low
- ▶  $N = K$ : Disclose fewer than  $K$  balls

## Others (27%)

- ▶ Similar to equilibrium types when the state is high
- ▶ Report A's less but do not report D's when the state is low
- ▶ Some low rates of A's when the state is high [confusion]



**receivers**

We now turn to receivers' behavior

## Goal.

- Investigate the extent to which receivers account for the fact that the evidence they see is selected?

We present two facts about receivers' behavior, from aggregate to disaggregate

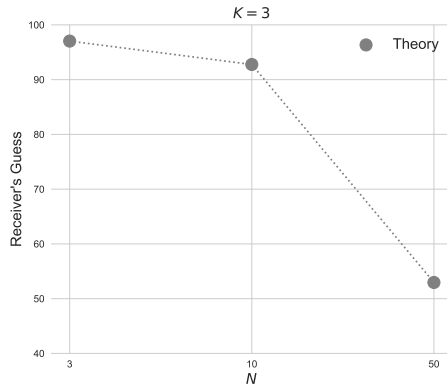
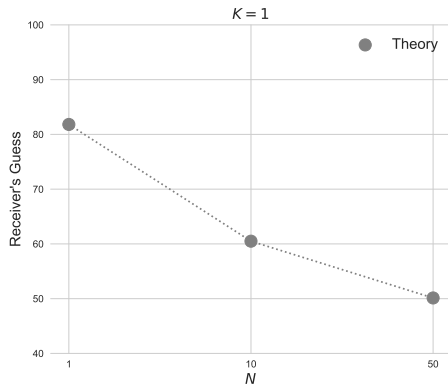
We consider the “most favorable” messages that are sent by senders

“Most favorable” messages are those with the highest GPA (top quintile)

As  $N$  increases, due to selective disclosure on the part of senders, receivers should become **increasingly skeptical** of these messages

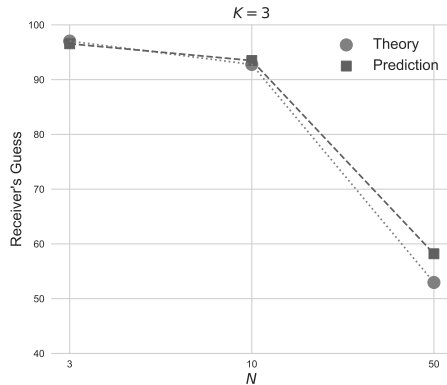
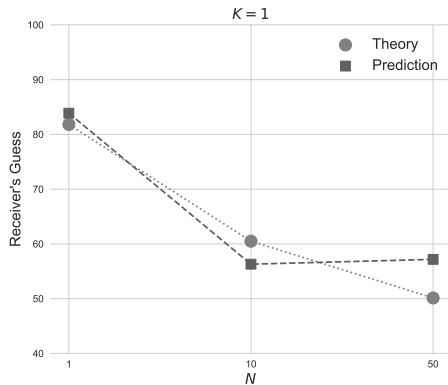
# Receivers' Behavior (1/2)

results: receivers



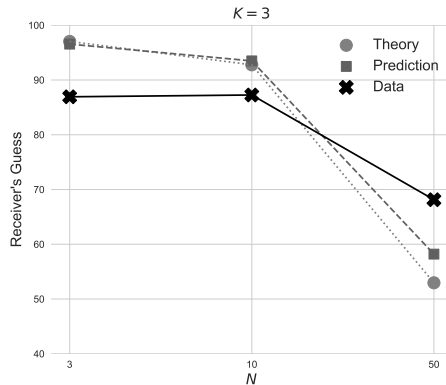
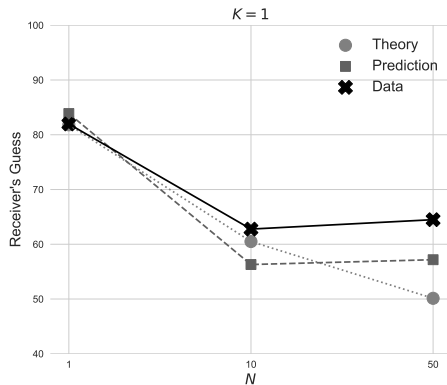
# Receivers' Behavior (1/2)

results: receivers



# Receivers' Behavior (1/2)

results: receivers



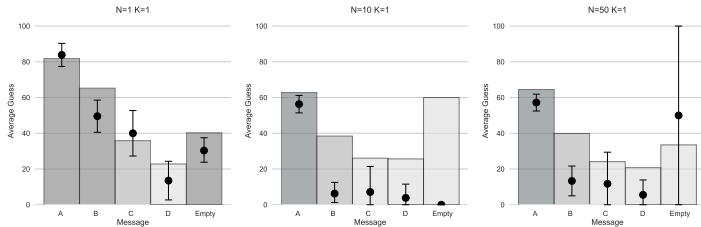
What about receivers' response to messages that are not the “most favorable”

For this, we need a more disaggregated look

As  $N$  increases, due to selective disclosure on the part of senders, receivers should become **extremely skeptical** to the least-favorable messages

# Receivers' Behavior (2/2)

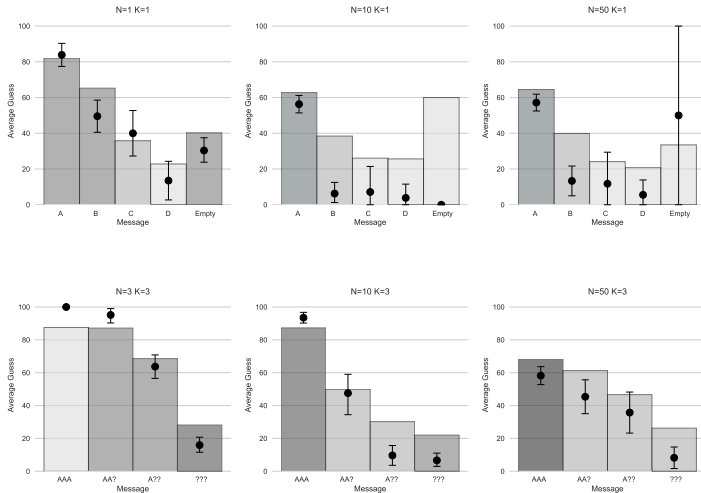
results: receivers





# Receivers' Behavior (2/2)

results: receivers



## Summary for Receivers.

- We find that receivers' behavior correctly accounts for the fact that the evidence they see is selected
- For the most favorable evidence, behavior is *quantitatively* close to equilibrium
- For less favorable evidence, while *qualitatively* consistent with equilibrium, receivers' are insufficiently skeptical

## Summary for Receivers.

- We find that receivers' behavior correctly accounts for the fact that the evidence they see is selected
- For the most favorable evidence, behavior is *quantitatively* close to equilibrium
- For less favorable evidence, while *qualitatively* consistent with equilibrium, receivers' are insufficiently skeptical

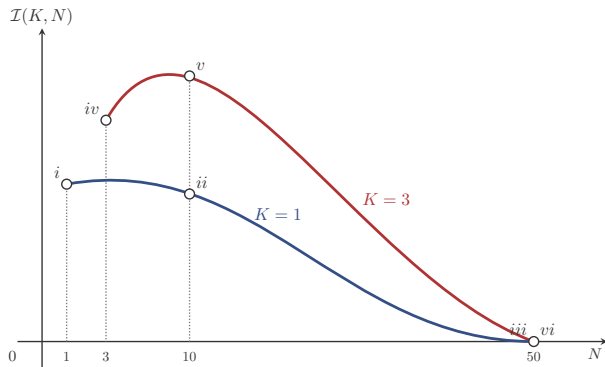
Connection to experimental literature on disclosure: “no news is bad news”

- ▶ Variation in updating strategies
  - ▶ Extent they **account for selection**
- ▶ Being closer to equilibrium  $\nrightarrow$  higher payoffs
- ▶ However, in many treatments, subjects better at accounting for selection get the highest payoff

**informativeness**

**Test 1.** Informativeness increases in  $K$

$$v > ii$$



	theory	senders' data	all data
<i>v.</i> ( $N10, K3$ )	.93	.93	.84
<i>ii.</i> ( $N10, K1$ )	.79	.80	.74

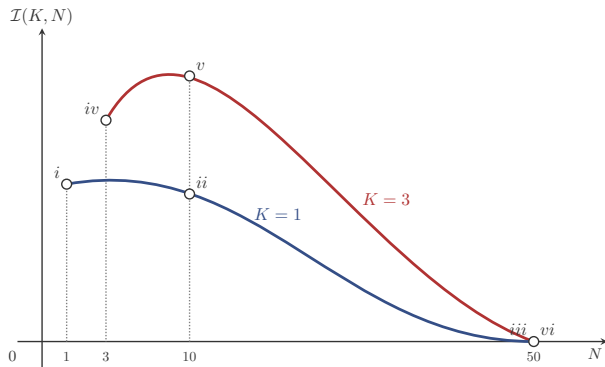
	theory	senders' data	all data
<i>v.</i> ( $N10, K3$ )	.93	.93	.84
<i>ii.</i> ( $N10, K1$ )	.79	.80	.74

**Test 1, ✓** Informativeness significantly increases from *ii* to *v* (p-value 0.00)



**Test 2.** Fixing  $K = N$ , informativeness increases in  $N$

$$iv > i$$



	theory	senders' data	all data
<i>iv.</i> ( $N3, K3$ )	.88	.90	.84
<i>i.</i> ( $N1, K1$ )	.81	.81	.75

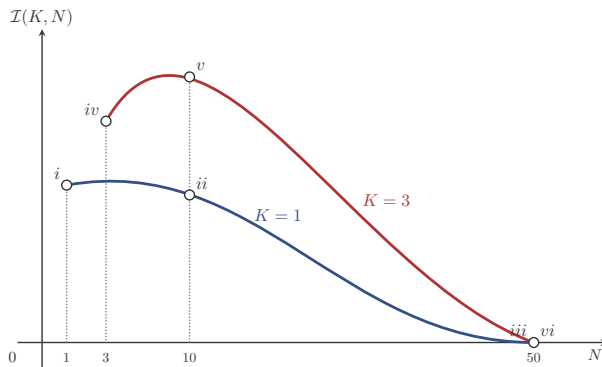
	theory	senders' data	all data
$iv. (N3, K3)$	.88	.90	.84
$i. (N1, K1)$	.81	.81	.75

**Test 2, ✓** Informativeness significantly increases from  $i$  vs  $iv$  (p-value 0.00)

**Test 3.** Informativeness eventually decreases to 0 in  $N$

(imitation effect)

$$iii = vi = 0$$



	theory	senders' data	all data
<i>vi.</i> ( $N50, K3$ )	.76	.80	.71
<i>iii.</i> ( $N50, K1$ )	.75	.79	.72

	theory	senders' data	all data
<i>vi.</i> ( $N50, K3$ )	.76	.80	.71
<i>iii.</i> ( $N50, K1$ )	.75	.79	.72

## Test 3

✓ Informativeness in *iii* and *vi* are not significantly different from each other

	theory	senders' data	all data
<i>vi.</i> ( $N50, K3$ )	.76	.80	.71
<i>iii.</i> ( $N50, K1$ )	.75	.79	.72

## Test 3

- ✓ Informativeness in *iii* and *vi* are not significantly different from each other
- ✓ They are significantly lower than in *ii* and *v* qualitatively OK

	theory	senders' data	all data
<i>vi.</i> ( $N50, K3$ )	.76	.80	.71
<i>iii.</i> ( $N50, K1$ )	.75	.79	.72

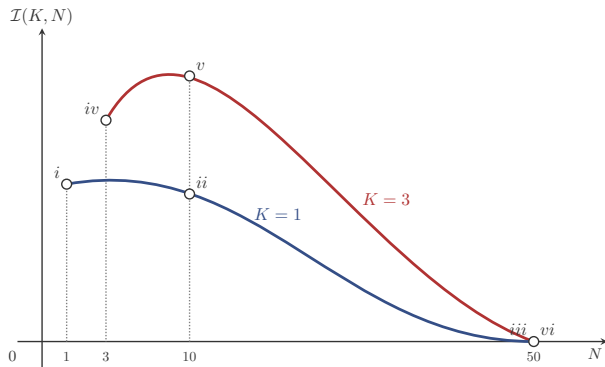
## Test 3

- ✓ Informativeness in *iii* and *vi* are not significantly different from each other
- ✓ They are significantly lower than in *ii* and *v* qualitatively OK
- ✗ But are significantly different than zero quantitatively off



**Test 4.** If  $K = 4$ , informativeness initially increases in  $N$  (separation effect)

$$v > vi$$



	theory	senders' data	all data
$v. (N10, K3)$	.93	.93	.84
$iv. (N3, K3)$	.88	.90	.84

	theory	senders' data	all data
$v. (N10, K3)$	.93	.93	.84
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## Test 4

- ✓ Informativeness significantly increases from  $iv$  and  $v$  in senders' data

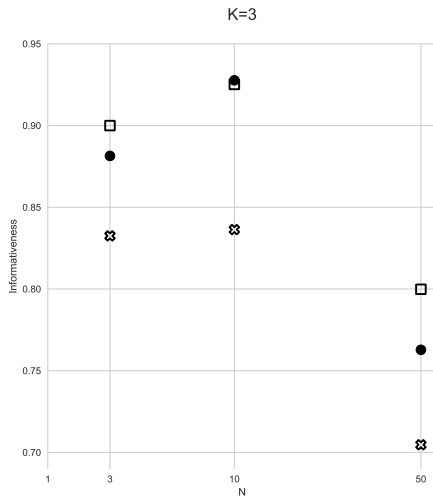
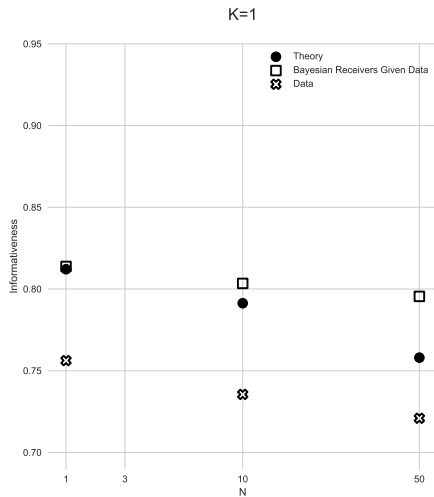
	theory	senders' data	all data
$v. (N10, K3)$	.93	.93	.84
$iv. (N3, K3)$	.88	.90	.84

## Test 4

- ✓ Informativeness significantly increases from  $iv$  and  $v$  in senders' data
- ✗ It doesn't in receivers' data

# Informativeness: All Results

results



The model offers a rich set of comparative statics

We find some quantitative deviations from theoretical point predictions

Yet, for the most part, data support qualitative predictions of the theory

**conclusion**

# Conclusion

---

An experimental study of selective disclosure, a pervasive force in communication

We develop new comparative statics in a model of constrained disclosure of noisy evidence: Theory to inform a parsimonious experimental design

Data corroborates main qualitative predictions of the theory

1. Senders overwhelmingly engage in **selective disclosure**

*Main deviation:* A minority of senders is “deception averse”

2. Receivers account for **selection bias**, i.e., for the fact that evidence they see is selected

*Main deviation:* Often not as much as they should

3. Aggregate effects on communication are in line with prediction

*Main deviation:* Some quantitative departures still to explore



**thank you**

# Appendix

# Some Literature

---

**Disclosure:** Jin, Luca and Martin (2022, AEJ: Micro)

**Cheap talk:** Blume, Lai and Lim (2020, Handbook of Experimental GT)

**Partially verifiable disclosure:** Penczynski, Koch and Zhang (2021)

**Theory:** Milgrom (1981, Bell), Fishman and Hagerty (1990, QJE), Di Tillio, Ottaviani and Sorensen (2021, Ecma)

## Some Notation: Strategies and Beliefs

Denote  $\mathcal{M}$  the space of all messages

### Sender's Strategy

pure and  $\theta$ -independent

- $\sigma : \Omega^N \rightarrow \mathcal{M}$  s.t.  $\sigma(\bar{\omega}) \in M(\bar{\omega})$ , for all  $\bar{\omega}$

where  $M(\bar{\omega})$  is the space of available messages given  $\bar{\omega}$

### Receiver's Beliefs and Strategy

- $\mu : \mathcal{M} \rightarrow \Delta(\Omega^N)$
- $a : \mathcal{M} \rightarrow \Delta(A)$

Given  $\mu$ , receiver's optimal strategy given by

$$a(m) = \mathbb{E}(\theta|m) = \sum_{\bar{\omega}} \mu(\bar{\omega}|m) \mathbb{E}(\theta|\bar{\omega}) \quad \forall m$$

# Sequential Equilibrium

A **Sequential Equilibrium** is a pair  $(\sigma^*, \mu^*)$  s.t.

1. For all  $\bar{\omega} \in \Omega^N$ ,  $\sigma^*(\bar{\omega}) \in M(\bar{\omega})$  and

$$\sum_{\bar{\omega}'} \mu^*(\bar{\omega}' | \sigma^*(\bar{\omega})) \mathbb{E}(\theta | \bar{\omega}') \geq \sum_{\bar{\omega}'} \mu^*(\bar{\omega}' | m') \mathbb{E}(\theta | \bar{\omega}') \quad m' \in M(\bar{\omega})$$

2. For all  $m$ ,  $\text{supp } \mu^*(\cdot | m) \subseteq C(m) = \{\bar{\omega} \in \Omega^N : m \in M(\bar{\omega})\}$ . In particular, if  $m \in \sigma^*(\Omega^N)$ ,

$$\mu^*(\bar{\omega} | m) = q(\bar{\omega} | \sigma^{*-1}(m)) \quad \forall \bar{\omega}$$

where  $q(\bar{\omega}) = \sum_{\theta} p(\theta) f(\bar{\omega} | \theta)$

Unlike classic disclosure games, the sequential equilibrium outcome is **not unique** when  $K < N$ .

- ▶ Off-path beliefs can support other equilibrium outcome.
- ▶ Refinements for signalling games (e.g., Cho-Kreps '87, Banks-Sobel '87) have no force here.
- ▶ Refinements for cheap talk games: Farrel (1993)'s **Neologism Proofness**.

## Equilibrium Multiplicity

$\Theta = \{0, 1\}$  and  $p(1) = \frac{1}{2}$ .  $N = 2$  and  $K = 1$ .

$\Omega = \{A, B\}$ ,  $f(A|\theta_H) = 1$  and  $f(A|\theta_L) = \frac{1}{2}$ .

$\theta$		$\bar{\omega}$		$M(\bar{\omega})$	$\sigma^*(\bar{\omega})$
1	----->	(A, A)	.....	$\{\emptyset, A\}$	A
0	----->	(A, B)		$\{\emptyset, A, B\}$	A
	----->	(B, B)		$\{\emptyset, B\}$	B

$$\mathbb{E}[\theta|m = A] = \frac{4}{7} \text{ and } \mathbb{E}[\theta|m = B] = \mathbb{E}[\theta|m = \emptyset] = 0 \implies$$

No incentive to deviate

## Equilibrium Multiplicity

$\Theta = \{0, 1\}$  and  $p(1) = \frac{1}{2}$ .  $N = 2$  and  $K = 1$ .

$\Omega = \{A, B\}$ ,  $f(A|\theta_H) = 1$  and  $f(A|\theta_L) = \frac{1}{2}$ .

$\theta$		$\bar{\omega}$		$M(\bar{\omega})$	$\sigma^*(\bar{\omega})$
1	----->	(A, A)	.....	$\{\emptyset, A\}$	$\emptyset$
0	----->	(A, B)		$\{\emptyset, A, B\}$	$\emptyset$
	----->	(B, B)		$\{\emptyset, B\}$	$\emptyset$

$$\mathbb{E}[\theta|m = \emptyset] = \frac{1}{2} \text{ and } \mathbb{E}[\theta|m = A] = \mathbb{E}[\theta|m = B] = 0 \implies$$

No incentive to deviate



# Equilibrium: Uniqueness

---

## Proposition

The equilibrium with maximal selective disclosure is Neologism Proof.

---

# Neologism Proof Equilibrium

A **neologism** is a pair  $(m, C)$ ,  $C \subseteq \{\bar{\omega} \in \Omega^N : m \in M(\bar{\omega})\}$

Literal meaning of  $(m, C) \rightsquigarrow$  "My type  $\bar{\omega}$  belongs to  $C$ "

A neologism  $(m, C)$  is **credible** relative to equilibrium  $(\sigma^*, \mu^*)$  if

1.  $\sum_{\bar{\omega}'} q(\bar{\omega}'|C) \mathbb{E}(\theta|\bar{\omega}') > \sum_{\bar{\omega}'} \mu^*(\bar{\omega}'|\sigma^*(\bar{\omega})) \mathbb{E}(\theta|\bar{\omega}')$  for all  $\bar{\omega} \in C$
2.  $\sum_{\bar{\omega}'} q(\bar{\omega}'|C) \mathbb{E}(\theta|\bar{\omega}') \leq \sum_{\bar{\omega}'} \mu^*(\bar{\omega}'|\sigma^*(\bar{\omega})) \mathbb{E}(\theta|\bar{\omega}')$  for all  $\bar{\omega} \notin C$

The equilibrium is **Neologism Proof** if no neologism is credible.

# Equilibrium: Uniqueness

## Proposition

The equilibrium with maximal selective disclosure is Neologism Proof.

---

Neologism Proofness delivers outcome uniqueness

An equilibrium  $(\sigma, \mu)$  induces an outcome  $x : \Omega^N \rightarrow A$ ,

$$x(\bar{\omega}) = \sum_{\bar{\omega}'} \mu(\bar{\omega}' | \sigma(\bar{\omega})) \mathbb{E}(\theta | \bar{\omega}') \quad \forall \bar{\omega}.$$

# Equilibrium: Uniqueness

---

## Proposition

The equilibrium with maximal selective disclosure is Neologism Proof.

---

## Proposition

Let  $(\sigma^*, \mu^*)$  be the equilibrium with maximal selective disclosure and  $(\sigma, \mu)$  be any other Neologism Proof equilibrium. Let  $x^*$  and  $x$  their respective outcomes. Then,  $x^* = x$ .

---

## Back to the Example

$\theta$		$\bar{\omega}$		$M(\bar{\omega})$	$\sigma^*(\bar{\omega})$
1	----->	$(A, A)$	.....	$\{\emptyset, A\}$	$\emptyset$
0	----->	$(A, B)$		$\{\emptyset, A, B\}$	$\emptyset$
	----->	$(B, B)$		$\{\emptyset, B\}$	$\emptyset$

$$m = A \text{ and } C = \{(A, A), (A, B)\} \implies$$

$$\mathbb{E}[\theta|m = A] = \frac{4}{7} > \mathbb{E}[\theta|m = \emptyset] = \frac{1}{2}$$

Credible neologism  $\implies$  no Neologism Proof equilibrium

# Experimental Design: Sender Interface

Round 7 of 30: Communication Stage

You are the Sender

Reminder:

If the secret Urn is **Yellow**, this is the probability of each ball being drawn:

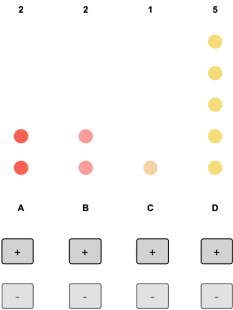
A	B	C	D
10 %	20 %	25 %	45 %

If the secret Urn is **Red**, this is the probability of each ball being drawn:

A	B	C	D
45 %	25 %	20 %	10 %

The secret Urn is **Yellow**

Available Balls



Your message to the Receiver is:



Send

# Experimental Design: Sender Interface

Round 7 of 30: Communication Stage

You are the Sender

Reminder:

If the secret Urn is **Yellow**, this is the probability of each ball being drawn:

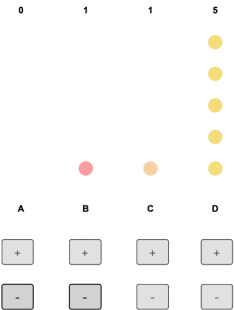
A	B	C	D
10 %	20 %	25 %	45 %

If the secret Urn is **Red**, this is the probability of each ball being drawn:

A	B	C	D
45 %	25 %	20 %	10 %

The secret Urn is **Yellow**

Available Balls



Your message to the Receiver is:

A

A

B

Send

# Experimental Design: Receiver Interface

Round 7 of 30: Guessing Stage

You are the Receiver

**Reminder:**

If the secret Urn is **Yellow**, this is the probability of each ball being drawn:

A	B	C	D
10 %	20 %	25 %	45 %

If the secret Urn is **Red**, this is the probability of each ball being drawn:

A	B	C	D
45 %	25 %	20 %	10 %

The Sender had 10 available balls and they could disclose 3 or less. This is the Sender's message:



Use the slider below to indicate your Guess of how likely it is that the secret Urn is Red.

Your Guess: 10



Submit

» Back



# Experimental Design: Summary

**Round 7 of 30: Payoff**

**You are the Receiver**

The secret Urn was **Yellow**

In this Round you earned 100 points.

Continue

**How were your points determined?**

The secret Urn was Yellow. Your Guess was 10.

The two Computer's Random Numbers were 59 and 44.

Your Guess was smaller than or equal to the largest of the two Computer's Random Numbers, so you earned 100 points.

# Experimental Design: Summary

Round 7 of 30: Summary

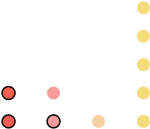
You are the Sender

## Sender's Summary

The secret Urn was **Yellow**

Available Balls

2      2      1      5



A      B      C      D

Sender's Message:



## Receiver's Summary

The Sender had 10 available balls and they could disclose 3 or less. This is the Sender's message:



Use the slider below to indicate your Guess of how likely it is that the secret Urn is Red.

Guess: 10



# Experimental Design: History

Round 7 of 30: History

You are the Sender

Round	Secret Urn	Message	Guess
7	Yellow	A A B	10
6	Red	A A ○	77
5	Red	A B B	77
4	Red	A A A	97
3	Red	A A ○	87
2	Yellow	C C ○	52
1	Red	○ ○ ○	0

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## Challenge

- ▶ Large number of urn / balls / message combinations
- ▶ Specific behavior of interest varies across treatments
  - ▶ Number of balls sent ( $K = 1$  vs  $K = 3$ )
  - ▶ Balls sent vs balls available ( $N = K$  vs  $N > K$ )

→ Precludes a unified approach using those variables

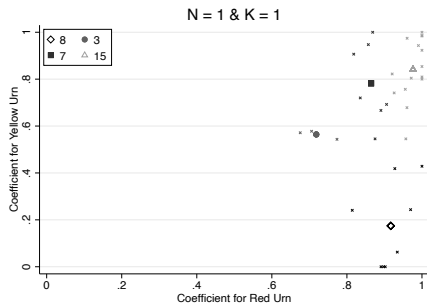
# Heterogeneity: Senders

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## Solution

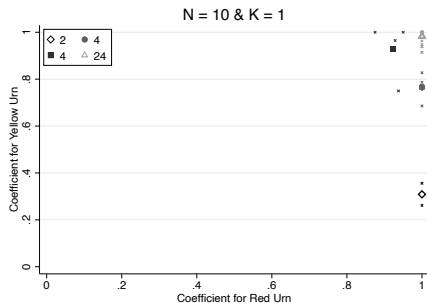
- ▶ Transform balls and messages to numbers ( $B^\#$  and  $M^\#$ )
- ▶ Regress  $M^\#$  on  $B^\#|_{\text{yellow urn}}$  and  $B^\#|_{\text{red urn}}$
- ▶ Cluster the coefficient estimates
- ▶ Describe behavior along key dimensions of interest

# Heterogeneity: Senders



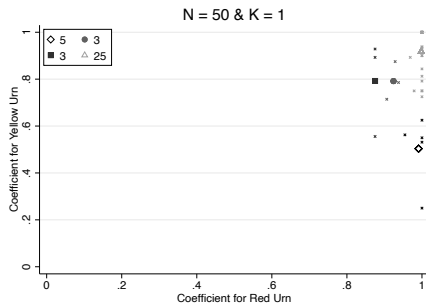
Cluster	Obs (33)	Urn	$K$	A	D
Triangle	15	Red	0.91	1	0.38
		Yellow	0.64	1	0.27
Square	7	Red	0.73	1	0.25
		Yellow	0.51	1	0.21
Circle	3	Red	0.5	0.92	n/a
		Yellow	0.54	0.67	0.49
Diamond	8	Red	0.71	1	0.20
		Yellow	0.30	0	0.46

# Heterogeneity: Senders



Cluster	Obs (34)	Urn	$K$	A	D
Triangle	24	Red	1	1	0
		Yellow	1	0.97	0.02
Square	4	Red	1	0.81	0.08
		Yellow	1	0.88	0.07
Circle	4	Red	1	1	0
		Yellow	1	0.46	0.14
Diamond	2	Red	1	1	0
		Yellow	1	0	0.89

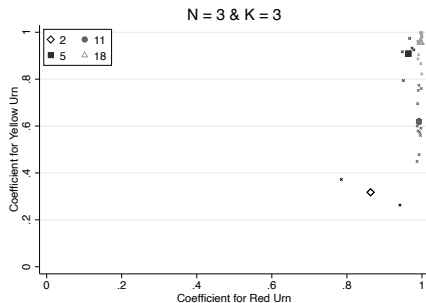
# Heterogeneity: Senders



Cluster	Obs (36)	Urn	$K$	A	D
Triangle	25	Red	1	0.99	0
		Yellow	1	0.74	0.03
Square	3	Red	0.96	0.82	0.1
		Yellow	1	0.51	0.15
Circle	3	Red	1	0.78	0
		Yellow	1	0.63	0.18
Diamond	5	Red	1	0.96	0
		Yellow	0.95	0.26	0.46

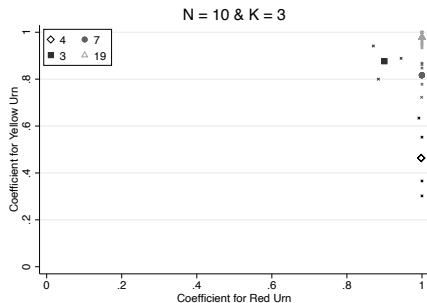


# Heterogeneity: Senders



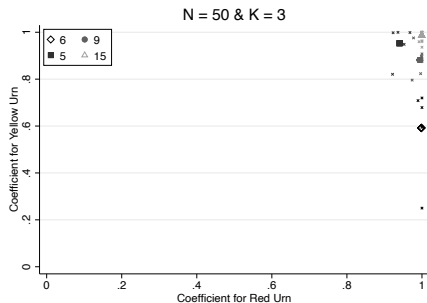
Cluster	Obs (36)	Urn	$K$	A	D
Triangle	18	Red	0.58	1	0.15
		Yellow	0.18	1	0.12
Square	5	Red	0.29	1	0
		Yellow	0.10	0.88	0.05
Circle	11	Red	0.26	1	0.06
		Yellow	0.15	0.23	0.60
Diamond	2	Red	0	1	0
		Yellow	0.06	0.25	0.50

# Heterogeneity: Senders



Cluster	Obs (33)	Urn	$K$	A	D
Triangle	19	Red	0.99	0.99	0
		Yellow	0.88	0.96	0.01
Square	3	Red	1	0.46	0.17
		Yellow	1	0.43	0.04
Circle	7	Red	1	0.94	0
		Yellow	0.74	0.66	0.10
Diamond	4	Red	0.92	0.83	0
		Yellow	0.76	0.28	0.43

# Heterogeneity: Senders



Cluster	Obs (35)	Urn	$K$	A	D
Triangle	15	Red	1	0.88	0
		Yellow	0.94	0.80	0
Square	5	Red	0.89	0.17	0
		Yellow	0.87	0.32	0
Circle	9	Red	0.97	0.70	0
		Yellow	0.94	0.31	0.04
Diamond	6	Red	1	0.86	0.03
		Yellow	0.95	0.31	0.41

# Heterogeneity: Senders

## Equilibrium type (56%)

- ▶ Most common
- ▶  $N > K$ : Mostly report best balls independently of the state
- ▶  $N = K$ : Disclose fewer than  $K$  balls

## Deception Averse Type (17%)

- ▶ A's reported more often when the state is high
- ▶ D's reported more often when the state is low
- ▶  $N = K$ : Disclose fewer than  $K$  balls

## Others (27%)

- ▶ Similar to equilibrium types when the state is high
- ▶ Report A's less but do not report D's when the state is low
- ▶ Some low rates of A's when the state is high [confusion]

## Challenge

- ▶ Large number of messages
- ▶ Different messages across treatments
- ▶ Some messages have very few observations

→ Precludes a unified approach using that variable

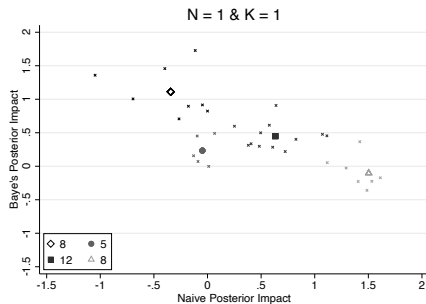
# Heterogeneity: Receivers

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## Solution

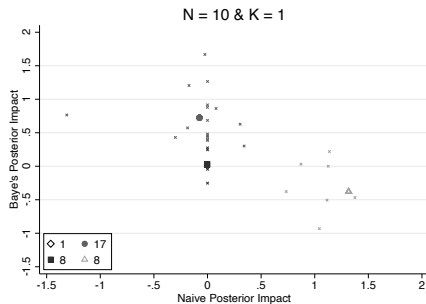
- ▶ Compute equilibrium update following each message
- ▶ Compute the update of someone who ignores selection: naive update
- ▶ Regress guesses on a constant ( $\alpha$ ) and the equilibrium and naive updates
- ▶ Cluster the coefficient estimates
- ▶ Describe behavior along key dimensions of interest

# Heterogeneity: Receivers



Cluster	Obs (33)	A	B	$\emptyset$	C
Diamond	8				
$\alpha = 0.23$		0.87	0.67	0.23	0.47
Circle	5				
$\alpha = 0.39$		0.56	0.49	0.41	0.37
Square	12				
$\alpha = 0.02$		0.86	0.73	0.41	0.38
Triangle	8				
$\alpha = -0.23$		0.90	0.67	0.51	0.23

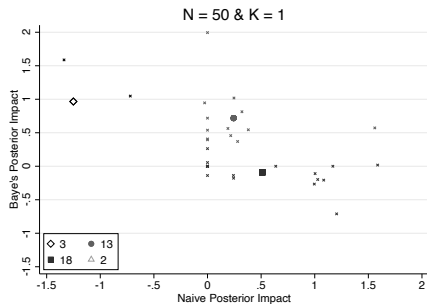
# Heterogeneity: Receivers



Cluster	Obs (34)	A	B	$\emptyset$	D
Diamond	1				
$\alpha = 4.20$		0.60*	0.23*	0.60*	n/a
Circle	17				
$\alpha = 0.28$		0.66	0.26	n/a	0.11
Square	8				
$\alpha = 0.56$		0.58	0.60	n/a	0.60
Triangle	8				
$\alpha = -0.23$		0.62	0.52	n/a	0.11

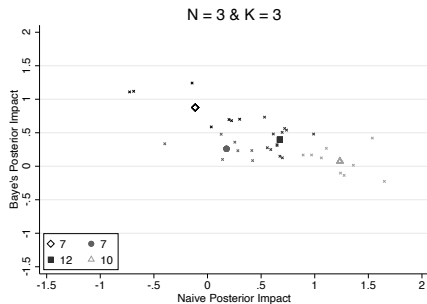


# Heterogeneity: Receivers



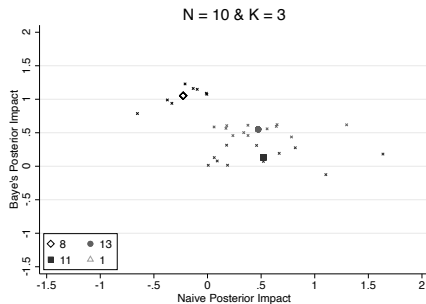
Cluster	Obs (36)	A	B	$\emptyset$	D
Diamond	3				
$\alpha = 0.89$		0.35	0.17	0.21*	0.75
Circle	13				
$\alpha = 0.15$		0.71	0.29	0.46*	0.11
Square	18				
$\alpha = 0.26$		0.63	0.53	n/a	0.19
Triangle	2				
$\alpha = -1.15$		0.69	0.41	n/a	n/a

# Heterogeneity: Receivers



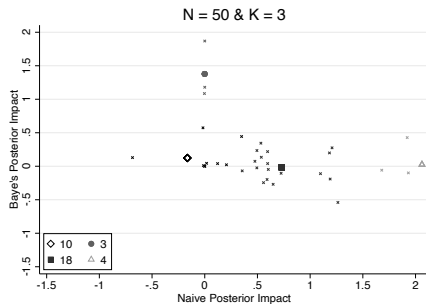
Cluster	Obs (36)	AAA	AAB	AA	AB
Diamond	7				
$\alpha = 0.20$		0.92*	0.86	0.86	0.62
Circle	7				
$\alpha = 0.30$		0.72	0.66	0.63	0.68
Square	12				
$\alpha = -0.04$		0.88	0.92	0.91	0.86
Triangle	10				
$\alpha = -0.24$		1	0.97	0.96	0.90

# Heterogeneity: Receivers



Cluster	Obs (33)	AAA	AAB	AA	ABB
Diamond	8				
$\alpha = 0.19$		0.95	0.11	0.02	0.03
Circle	13				
$\alpha = -0.07$		0.89	0.70	0.24	0.26
Square	11				
$\alpha = 0.10$		0.74	0.70	n/a	0.61
Triangle	1				
$\alpha = -3.98$		1*	0.54*	n/a	0.02*

# Heterogeneity: Receivers



Cluster	Obs (35)	AAA	AAB	AA	DDD
Diamond	10				
$\alpha = 0.64$		0.54	0.49	0.33	0.32
Circle	3				
$\alpha = 0.11$		0.84	0.01*	n/a	0.07
Square	18				
$\alpha = -0.04$		0.67	0.69	0.57	0.12
Triangle	4				
$\alpha = -1.16$		0.89	0.80	0.91*	n/a

# Heterogeneity: Receivers

- ▶ Variation in updating strategies
  - ▶ Extent they account for selection
- ▶ Being closer to equilibrium  $\nrightarrow$  higher payoffs
- ▶ However, in many treatments, groups better at accounting for selection are among the highest
- ▶ With  $N = 50$ , few differences in payoffs

# Summary

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## Senders

- ▶ The majority:
  - ▶ Select the better balls to send.
  - ▶ Behave similarly for both urns.
- ▶ Some convey more information by conditioning on the type.

→ More information transmitted than predicted.

## Receivers

- ▶ Many do not fully account for selection.
- ▶ Some are not very responsive.

→ Less information received than predicted.