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## MEDIA COMPETITION AND SOCIAL DISAGREEMENT

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## MEDIA COMPETITION AND SOCIAL DISAGREEMENT

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We study the competitive provision and endogenous acquisition of political information. Our main result identifies a natural equilibrium channel through which a more competitive market decreases the efficiency of policy outcomes. A critical insight we put forward is that competition among information providers leads to informational specialization: firms provide relatively less information on issues that are of common interest and relatively more information on issues on which agents' preferences are heterogeneous. This enables agents to acquire information about different aspects of the policy, specifically, those that are particularly important to them. This leads to an increase in social disagreement, which has negative welfare implications. We establish that, in large enough societies, competition makes every agent worse off by decreasing the utility that she derives from the policy outcome. Furthermore, we show that this decline cannot be compensated by the decrease in prices resulting from competition.

KEYWORDS: Information, media, competition, disagreement, spatial models.

### 1. INTRODUCTION

WE STUDY the competitive provision and endogenous acquisition of political information. Our interest is motivated by a growing public debate on the consequences of a fast-changing media landscape and information consumption habits on our democracies.<sup>1</sup> The political-economy literature still lacks a comprehensive understanding of how competition affects the strategic incentives of information providers in this market and its possible consequences on the political process (Strömberg (2015)). We contribute to filling this gap by presenting a simple model in which nonpartisan information providers compete to sell information to agents before they cast a vote. Our analysis leads to three novel conclusions. First, we show that competition leads to informational specialization. The critical insight we put forward is that competition forces information providers to become relatively less informative on issues that are of common interest and, therefore, are particularly important from a social perspective. Second, we analyze the downstream effects of such specialization and show that while agents become better informed on an individual level, competition amplifies social disagreement. Third, we highlight the social welfare implications of increased disagreement. Specifically, we establish that in societies that are large enough, competition makes every agent worse off by decreasing the utility that she derives from the policy outcome.

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<sup>1</sup>Pew Research Center (2016), Sunstein (2017), and Nichols (2017) provide a comprehensive description of the media market and how it dramatically changed in the last decade.

In our model, a finite number of firms compete to provide information to a finite number of Bayesian agents about a newly proposed policy with uncertain prospects. Whether the new policy is implemented to replace a known status quo depends on its approval rate. The policy features a vertical component, which is a *valence* aspect on which agents' preferences are identical, and two horizontal components, which are *ideological* aspects on which preferences are heterogeneous. Each firm sells a signal about the policy, but faces a constraint on how informative such a signal can be on the different components. That is, being more informative about one of these components requires the firm to be less informative about the others. To illustrate, imagine a new healthcare bill is under discussion, the details of which are not yet fully known to the public. The bill potentially affects many dimensions of social life, and voters might evaluate these dimensions differently. For example, the new bill could promote an increase in the overall quality of health care (vertical component), expand the budget deficit (horizontal component), and induce more redistribution via increasing the share of the population covered (horizontal component). Voters acquire information from the media before they approve or disapprove the policy. A larger consensus increases the probability that the bill is ultimately implemented. The news outlets compete for profits by allocating their limited resources (journalists, airtime, etc.) to a possibly different mix of these policy components and by setting prices.<sup>2</sup>

The equilibrium of our model demonstrates how competition among information providers induces informational specialization. While all agents want to learn about the policy, different agents care about different aspects of it. To maximize profits, firms sell information that is valuable for a diverse set of agents. They can do so by being informative about aspects of the policy that are of common interest, that is, valence. However, as the market becomes more competitive, the effectiveness of such a "generalist" approach declines; different firms target different agents, providing signals tailored to the specific needs of those agents.

The equilibrium analysis leads to novel insights. We find that competition creates a broader spectrum of informational options, enabling agents to acquire information that is better aligned with their needs. Also, the market does not overspecialize. Indeed, as the number of competing firms grows large, the equilibrium converges to a daily-me paradigm, a situation in which each agent finds an information provider that perfectly meets her unique informational needs (Sunstein (2001)). Furthermore, competition decreases the price associated with such information. Thus, competition benefits agents by enabling them to be better informed at lower prices. These results conform to the classic view that sees the market for news as a "marketplace of ideas" that promotes knowledge and the discovery of truth (see Posner (1986)).

We then use our model to study the effects of competition on welfare, which extend well beyond the information supplied by firms. The market for political news differs from other markets partly because of the externalities that information acquisition imposes on the political process. Such a process, by definition, aggregates the opinions of agents who are potentially in conflict with each other. Because of this, information has both direct and indirect welfare effects. The direct effect measures how the information that an agent personally acquires enables her to sway the policy outcome in the direction of her

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<sup>2</sup>As another example, consider the social-distancing policies adopted to slow the spread of COVID-19. These policies have both public health and economic components, which are weighted differently by different people. News outlets may differ in which components they emphasize (see Simonov, Sacher, Dubé, and Biswas (2020), Bursztyn, Rao, Roth, and Yanagizawa-Drott (2020)).

own preferences. The indirect effect, instead, measures how the information acquired by others is used to sway the policy outcome toward their preferences. Agents, who try to maximize their own impact on the political process, acquire information based on its direct value. Therefore, a competitive market specializes to meet such demand. However, as firms specialize, agents learn about increasingly different aspects of the policy. Thus, their opinions diverge, leading to an increase in social disagreement. This generates a decline in the indirect value of information, capturing the externality agents impose on each other. Our main result demonstrates that, in large enough societies, this externality becomes critical. That is, the utility that each agent derives from the policy outcome decreases with competition. Moreover, the decrease in prices resulting from competition does not compensate for this decline.

Finally, we discuss how the main insights of the paper extend beyond our simplifying assumptions by comparing two notable market structures: monopoly and perfect competition. This further highlights the importance of two key features of our model: the heterogeneity in agents' preferences and the constraints on how much they can learn about the policy. The interaction of these features leads to information specialization, which plays a critical role in the inefficiency identified in this paper.

The rest of the paper is organized as follows. The next subsection reviews the related literature and discusses the empirical implications of our work. Section 2 introduces the model, while Section 3 characterizes its equilibrium. Our main results are presented in Section 4, and Section 5 discusses their extensions. All proofs are relegated to Appendix A. Additional material and extensions are provided in Appendixes B and C in the Supplemental Material (Perego and Yuksel (2022)).

### 1.1. *Related Literature and Empirical Implications*

Our paper contributes to the burgeoning literature on the political economy of mass media (see Prat and Strömberg (2013), Anderson, Waldfogel, and Strömberg (2015)). Specifically, we contribute to the branch of this literature that studies the effects of the endogenous provision of information and its externalities on the political process. One robust finding of this literature is that when information providers are partisans—namely, they are interested in persuading the public to take a certain action—competition generally brings about better social outcomes. Intuitively, competition forces firms to better align with what consumers demand, thus reducing their inherent biases. Results along this line are reflected in the works of Baron (2006), Chan and Suen (2009), and Anderson and McLaren (2012).<sup>3</sup> Similarly, Duggan and Martinelli (2011) find that slanting is an equilibrium outcome in a richer model that allows for electoral competition, but otherwise abstracts away the problem of competitive information provision. While not modeling competition, the works of Alonso and Câmara (2016) and Bandyopadhyay, Chatterjee, and Roy (2020) also belong to this strand of the literature. Instead, a general treatment of competition among biased senders is discussed in Gentzkow and Kamenica (2016). Our work differs from these papers as we assume that information providers are non-partisans and compete for profits. Chan and Suen (2008) consider a model with features that can be mapped back to our setup. Their primary interest, however, is to study the effects of exogenously located firms on electoral competition. They show that a new entrant increases the probability that parties will choose the policy favored by the median

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<sup>3</sup>The welfare-increasing effects of competition are also illustrated in Besley and Prat (2006), Corneo (2006), and Gehlbach and Sonin (2014), although for reasons orthogonal from those discussed here, namely the potential risks of media capture by the government.

voter, thereby increasing social welfare. In an extension, they also endogenize competition, but the only industry structure they can feasibly analyze (a duopoly) typically leads to higher welfare. Closer to our work, [Chen and Suen \(2019\)](#) study a competition model in which biased media firms compete for the scarce attention of readers, finding that an increase in competition leads to an increase in the overall informativeness of the industry. Similarly, results consistent with the idea that competition is welfare-increasing are discussed in [Burke \(2008\)](#), [Gentzkow and Shapiro \(2006\)](#), and [Gentzkow, Shapiro, and Stone \(2014\)](#). [Sobbrio \(2014\)](#) does not analyze the social welfare implications of media competition, but shows that competition can lead to specialization. [Galperti and Trevino \(2020\)](#) study a model of endogenous provision and acquisition of information, and show how competition for attention can lead to a homogeneous supply of information, even when consumers would value accessing heterogeneous sources. Overall, when consumers are rational, the evidence is stacked in favor of the welfare-increasing effects of media competition.

Our paper contributes to this literature by developing a full-fledged competition model that illustrates a novel and natural channel through which competition can be welfare-decreasing. While not analyzing the competitive provision of information, [Ali, Mihm, and Siga \(2018\)](#) study the interaction between private information and distributive conflicts in the context of a voting game. More specifically, they provide necessary and sufficient conditions under which the strategic interactions among agents can preclude a policy that is both ex ante and ex post optimal from being implemented. This is due to a form of adverse selection when information is scarce—an effect that is markedly distinct from the inefficiency we highlight in this paper. Departing from the assumption of rationality when processing information, [Mullainathan and Shleifer \(2005\)](#) consider a model in which heterogeneous consumers derive psychological utility from having their prior views confirmed by the information they receive. Their main result demonstrates how firms specialize in response to competition by slanting news toward the beliefs of their readers, resulting in a less informed electorate. In contrast, our model shows that firm specialization comes at the expense of information about valence (the vertical dimension), and studies of how this channel affects voting and, ultimately, social welfare. In a related model with behavioral preferences for confirmation, [Bernhardt, Krasa, and Polborn \(2008\)](#) study the welfare implications of competition, showing that competition increases the probability the society will make mistakes in policy selection. [Bordalo, Gennaioli, and Shleifer \(2016\)](#) analyze a model in which two firms compete for the attention of a group of “salient thinkers” by strategically setting the quality and the price of the product they sell. They show how distortions in consumers’ perceptions can explain the equilibrium degree of “commoditization” of some markets. [Strömberg \(2004\)](#) shows that media outlets have incentives to invest more in the coverage of issues that are important for groups that are valuable to advertisers, thus inducing a policy bias. Relatedly, [Matějka and Tabellini \(2020\)](#) study policy selection when voters are rationally inattentive. They find that divisive issues attract the most attention from voters and that this can create inefficiencies in public good provision.

Our paper also relates to a large body of literature on spatial competition.<sup>4</sup> As in [Salop \(1979\)](#), we use a circular setup to tractably model competition with an arbitrary number of firms. As in [Lederer and Hurter \(1986\)](#), [Hamilton, MacLeod, and Thisse \(1991\)](#), and [Vogel \(2011\)](#), we use spatial price discrimination to avoid well known technical issues related to equilibrium existence when both prices and locations are chosen endogenously (see [D’Aspremont, Gabszewicz, and Thisse \(1979\)](#)). As in [Vogel \(2008\)](#), we allow firms to

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<sup>4</sup>See [Anderson, de Palma, and Thisse \(1992\)](#) for a review of such literature.

differentiate in both vertical and horizontal features of the product space. We contribute to this literature in three ways. First, we explicitly model equilibrium interactions between vertical and horizontal competition. With this, we can show that competition leads firms to disinvest from vertical features—which are beneficial to all consumers—in favor of horizontal features—which are beneficial only to a niche segment. Second, we study the consequences of specialization in a context in which private consumption generates social externalities. This feature is common to many markets, well beyond our political-economy application. Finally, our firms sell information and, to account for this, we build Bayesian foundations into a spatial competition model.<sup>5</sup> For these reasons, our model can be used to study other aspects of media competition (e.g., implications on turnout, campaign spending, or candidate selection), or, more generally, consequences of competition in other information markets (Bergemann and Bonatti (2019)).

*Empirical Implications.* Our paper also relates to the large body of empirical literature that studies the effects of media on political outcomes. We contribute to this literature with several predictions that have empirical content. First, we predict that agents with different ideological preferences will be differentially informed. Using a large-scale incentivized survey, Angelucci and Prat (2020) show that subjects with different party affiliations are informed about different political facts. Second, we predict that such differences are caused by the fact that these agents acquire information from different media. Using an “audience-based” approach, the literature has established that media outlets can be reliably ranked in terms of the ideological preferences of their audience (e.g., Gentzkow and Shapiro (2011), Zhou, Resnick, and Mei (2011), Bakshy, Messing, and Adamic (2015)). Third, we predict that media outlets differentiate by emphasizing different issues (e.g., civil rights, healthcare, labor issues). Early evidence for this type of differentiation relies on specific examples: Puglisi (2011) identifies a Democratic bias—more coverage of issues championed by Democrats—for the *New York Times*; Larcinese, Puglisi, and Snyder (2011) and Puglisi and Snyder (2011) study selective coverage of some economic issues and political scandals, respectively. Using an alternative approach, Chopra, Haaland, and Roth (2020) provide evidence that people expect newspapers to selectively choose which issues to report on. However, testing our specific predictions on how firms differentiate requires adopting a more direct “content-based” approach, which involves a comprehensive analysis of the content provided by the outlets. Incidentally, the research frontier is moving in this direction (see Gentzkow, Kelly, and Taddy (2019)).<sup>6</sup> Budak, Goel, and Rao (2016) recruit human subjects to classify political articles according to topic and ideological position. Cagé, Hervé, and Viaud (2019) use a topic-detection algorithm to identify the set of news stories in online media. Angelucci, Cagé, and Sinkinson (2020) use machine-learning techniques to identify changes in content production of local newspapers in the 1950s. Most closely connected to our prediction, Nimark and Pitschner (2019) and Chahrour, Nimark, and Pitschner (2019) use machine-learning techniques to document significant differences in the coverage of political and economic issues among media outlets.

The most substantive and novel testable predictions of our paper, however, concern the effects of increased competition. First, we predict that an increase in media competition should be associated with a decrease in the relative provision of information on

<sup>5</sup>Technically, the Bayesian value of information becomes a “transportation” cost, which is neither convex nor concave in the distance between the firm and the agent.

<sup>6</sup>Groseclose and Milyo (2005), Baum and Groeling (2008), Ho et al. (2008), Gentzkow and Shapiro (2010), and Martin and Yurukoglu (2017) are among the first papers in this field to use these techniques.

the vertical dimensions, such as valence. Extensive empirical literature studies the effects of the introduction of the radio (e.g., Stromberg (2004)), the television (e.g., Gentzkow (2006)), and internet broadband (e.g., Falck, Gold, and Heblich (2014), Gavazza, Nardotto, and Valletti (2019), Miner (2015), Campante, Durante, and Sobbrío (2018)) on political outcomes such as public spending and political participation. Gentzkow, Shapiro, and Sinkinson (2011), Drago, Nannicini, and Sobbrío (2014), and Cagé (2020) employ a more direct approach and study the impact of entry in the local newspaper industry. Of these papers, Cagé (2020) is the only one that can discern the effects of competition on the content supplied by firms. She documents a negative relationship between media competition and information quality, a vertical dimension. Moreover, the results suggest that increased competition affects the relative coverage of different issues. Second, we predict that increased specialization, resulting from media competition, generates higher social disagreement. Similar concerns have been raised in public discourse. For example, Sunstein (2001) has argued that convergence to a daily-me paradigm could lead individuals to isolate themselves from the larger public debate, making it harder for people to come together on common issues. Although the literature on political polarization and social media is growing (e.g., Prior (2013), Campante and Hojman (2013), Iyengar, Lelkes, Levendusky, Malhotra, and Westwood (2019)), the only implicit test for this prediction comes from Allcott, Braghieri, Eichmeyer, and Gentzkow (2020). In a large-scale field experiment, they show that social media usage causes a significant increase in social disagreement, measured as polarization in the strength of political preferences. Although this study does not explicitly control for increased competition, it is plausible that social media facilitates informational specialization.

## 2. MODEL

This section introduces the model and discusses its main assumptions. We model the interaction among a group of firms and agents: firms choose what information to produce about an uncertain policy and its price for each agent; agents choose which firm to acquire information from and whether to approve the policy, thereby affecting its chances of being implemented.

We now formally introduce the components of the model. There are  $N \geq 1$  identical firms and  $I \geq 1$  heterogeneous and Bayesian agents. We denote a typical firm by  $n$ , a typical agent by  $i$ , and her payoff type by  $\theta_i$ . Firms and agents interact over three consecutive stages.

In the first stage, before observing the agents' types, firms compete to provide agents with information about an uncertain policy  $\omega = (\omega_0, \omega_1, \omega_2)$ , whose three components are identically distributed as independent standard normals. Specifically, firm  $n$  chooses an *editorial strategy*  $b_n = (b_{n,0}, b_{n,1}, b_{n,2})$ , subject to the constraint that  $\|b_n\| \leq 1$ .<sup>7</sup>

In the second stage, agents' types  $(\theta_1, \dots, \theta_I)$  and firms' editorial strategies are publicly observed. Firm  $n$  sets a price  $p_n(\theta_i)$  for each agent.

In the last stage, each agent chooses at most one firm to acquire information from. If agent  $i$  chooses firm  $n$ , she pays the price  $p_n(\theta_i)$  and privately observes a signal realization  $s_i(\omega, b_n) = b_n \cdot \omega + \varepsilon_i$ . The error term  $\varepsilon_i$  is independent across firms and agents, and is distributed as a standard normal.

Finally, conditional on the observed signal, the agent approves or disapproves the policy. The policy is implemented with a probability equal to its approval rate, which is the

<sup>7</sup>We denote by  $\|\cdot\|$  the  $\ell_2$  norm of a vector.



that firms are constrained in the resources—journalists, pages, airtime, and so forth—they can allocate on the components of the policy (see Chan and Suen (2008), Strömberg (2015), Gentzkow, Shapiro, and Stone (2015)). Each component of the editorial strategy  $b_n$  can be interpreted as the firm’s emphasis on the corresponding component of the policy. More emphasis translates into a signal that is more informative about such component. This substitutability generates the trade-off that is at the heart of our model. In Section 5.2, we study a model of multimedia in which agents can acquire information from multiple firms.

Two other assumptions in our model are worth further discussion. First, the finite number of agents guarantees that information has instrumental value. Agents acquire information because it allows them to better sway the policy outcome in the direction of their preferences. Second, we assume that the policy is implemented probabilistically, as a function of the approval rate (e.g., Banks and Duggan (2004), Patty (2007)). This eliminates the scope for learning about the policy from pivotal reasoning and reduces the complexity of the agents’ problem, thus enabling us to focus on the most novel aspect of the model—the competitive supply of information.

Finally, prices in our model do not necessarily need to represent monetary transfers from agents to firms. Alternatively, they can be interpreted as advertising revenues. In this interpretation, firms compete for the agents’ attention, which increases with the value of the information they acquire, but decreases with the intensity of advertisements they observe. As in Lederer and Hurter (1986) and Hamilton, MacLeod, and Thisse (1991), we use spatial price discrimination to avoid well known technical issues related to equilibrium existence when both prices and locations are chosen endogenously (see D’Aspremont, Gabszewicz, and Thisse (1979)). While forms of price discrimination are common in the market for news, such an assumption is arguably even more reasonable when prices are interpreted as resulting from advertisement, which is increasingly targeted (Athey and Gans (2010)).

### 3. EQUILIBRIUM

This section analyzes the equilibrium of our game. First, we establish equilibrium existence by solving the game via backward induction. Second, we illustrate how to transform the firm’s problem into an equivalent location problem on a disk. This is not only analytically convenient, but also provides a useful spatial interpretation for firms’ equilibrium behavior. Building on this spatial interpretation, we conclude by discussing the uniqueness of the equilibrium.

#### 3.1. Existence and Characterization

##### 3.1.1. The Agent’s Problem: Information Acquisition and Approval

We begin by characterizing equilibrium behavior in the last stage of the game. In this stage, agents choose which information to acquire and, conditional on what they learn, whether to approve the policy. To this purpose, fix an agent’s type  $\theta_i$  and suppose that she acquires information from firm  $n$ , whose editorial strategy is  $b_n$ . Her equilibrium *approval strategy* is relatively straightforward, as it only depends on the realized signal and not on the strategies of other agents.

LEMMA 1—Approval: *Conditional on a signal realization  $\bar{s}_i = s(\omega, b_n)$ , type  $\theta_i$  approves the policy if and only if  $\mathbb{E}_\omega(u(\omega, \theta_i) | \bar{s}_i) \geq 0$ .*

The agent’s approval strategy affects the outcome of the game, as it impacts the probability with which the policy is ultimately implemented. Nonetheless, her equilibrium behavior is simple and abstracts from pivotal reasoning. Specifically, she computes the expectation of  $u(\omega, \theta_i)$  conditional on  $\bar{s}_i$  and approves the policy if and only if it leads to a payoff that is higher than the status quo.<sup>9</sup> That is, the agent behaves as if she were voting expressively (Brennan and Buchanan (1984)). Lemma 1 follows from the fact that the policy is implemented probabilistically, as a function of the approval rate. Because of this, each agent impacts the policy outcome equally—changing the implementation probability by  $1/I$ —regardless of the decisions of others. This eliminates the scope for learning about the policy by engaging in pivotal reasoning.

Next, we characterize the *information acquisition strategy* of the agent. Since information allows the agent to better sway the policy outcome in the direction of her preferences, she attaches an instrumental value to the information she acquires. Abstracting from prices, this *value of information* is defined as the difference between her expected equilibrium payoff associated with observing a signal from a firm  $n$  and the one associated with observing no signal whatsoever. Characterizing this value is a key step for the equilibrium analysis of the game.

LEMMA 2—Value of Information: *The value of firm  $n$ ’s information for an agent of type  $\theta_i$  is*

$$v(b_n|\theta_i) = \frac{|\theta_i \cdot b_n|}{I\sqrt{2\pi(1 + \|b_n\|^2)}}.$$

Lemma 2 computes the value of information from firm  $n$  for type  $\theta_i$ . It establishes that such value is independent of the information acquired by other agents and, hence, the editorial strategies of firms other than  $n$ . The value of information has several intuitive properties. First, it is decreasing in the number of agents  $I$ . This captures the fact that the larger a society is, the smaller is the marginal impact that an agent has on the policy outcome, thus decreasing the instrumental value that such an agent assigns to information. Second, the value of information is increasing in  $|\theta_i \cdot b_n|$ , which corresponds to the statistical correlation between the agent’s payoff  $u(\omega, \theta_i)$  and the signal  $s_i(\omega, b_n)$ .<sup>10</sup> We will return to this point shortly in Section 3.2.

In equilibrium, type  $\theta_i$  chooses the firm that provides the highest value of information net of its price. More formally, given a profile of editorial strategies and prices,  $(b_n, p_n(\theta_i))_{n=1}^N$ , type  $\theta_i$  acquires information from firm  $n$  only if  $v(b_n|\theta_i) - p_n(\theta_i) \geq v(b_m|\theta_i) - p_m(\theta_i)$  for all  $m$ .

### 3.1.2. The Firm’s Problem: Prices and Editorial Strategies

We now turn to the analysis of firms’ equilibrium behavior. We begin with the second stage of the game, where firms set prices after observing each other’s editorial strategies  $b = (b_n)_{n=1}^N$  and the agents’ types  $(\theta_1, \dots, \theta_I)$ . Each firm maximizes profits, which are affected by the prices it charges to its readers. Firms set a price for each type  $\theta_i$  and, hence, compete à la Bertrand for each potential reader (see Lederer and Hurter (1986)).

To provide intuition on what prices prevail in equilibrium, let us consider a simple example in which two firms compete for type  $\theta_i$ . Suppose that their editorial strategies  $b_1$

<sup>9</sup>We assume, without loss of generality, that the agent approves the policy when she is indifferent.

<sup>10</sup>Furthermore, note that  $\mathbb{V}(\epsilon_i) = 1$  and  $\|b_n\| \leq 1$  are normalizations.

and  $b_2$ , chosen in the first stage, are such that  $v(b_1|\theta_i) > v(b_2|\theta_i)$ . The most competitive price that firm 2 can set is  $p_2(\theta_i) = 0$ . Even in this case, firm 1 can nonetheless “win” the agent by simply setting a price  $p_1(\theta_i) < v(b_1|\theta_i) - v(b_2|\theta_i)$ . Therefore, in equilibrium, firm 1 must win the agent and earn a profit equal to  $v(b_1|\theta_i) - v(b_2|\theta_i)$ .

This reasoning easily generalizes to  $N > 2$ . Fix a profile of editorial strategies  $b = (b_n)_{n=1}^N$ . In equilibrium, firm  $n$  wins type  $\theta_i$  only if  $v(b_n|\theta_i) \geq \max_{m \neq n} v(b_m|\theta_i)$ , in which case she earns a profit of  $v(b_n|\theta_i) - \max_{m \neq n} v(b_m|\theta_i) \geq 0$ . Conversely, if  $v(b_n|\theta_i) < \max_{m \neq n} v(b_m|\theta_i)$ , the firm loses type  $\theta_i$  and earns no profit. Conveniently, the equilibrium profit that firm  $n$  accrues from type  $\theta_i$  is uniquely pinned down by  $\max_m v(b_m|\theta_i) - \max_{m \neq n} v(b_m|\theta_i) \geq 0$ .<sup>11</sup> Therefore, firm  $n$ ’s total profit is  $\sum_{i=1}^I \max_m v(b_m|\theta_i) - \max_{m \neq n} v(b_m|\theta_i)$ , which depends only on the profile of editorial strategies  $b$ .

Finally, we analyze the first stage of the game. Firms choose their editorial strategies before observing the agents’ types, which are identically and independently distributed according to distribution  $F$ . Given the analysis above, for any profile of editorial strategies  $(b_n, b_{-n})$ , firm  $n$ ’s expected profit is

$$\Pi_n(b_n, b_{-n}) = I \mathbb{E}_{\theta_i} \left( \max_m v(b_m|\theta_i) - \max_{m \neq n} v(b_m|\theta_i) \right). \tag{1}$$

In the first stage of the game, firms play a one-shot complete-information game with payoffs defined by  $\Pi_n$ . The next result establishes the existence of a pure-strategy Nash equilibrium in this game.

**THEOREM 1—Existence:** *A pure-strategy equilibrium  $(b_n)_{n=1}^N$  exists.*

By construction, the profit function  $\Pi_n$  incorporates the equilibrium behavior of firms and agents in the subsequent stages of the game. By backward induction, a Nash equilibrium of the first-stage game corresponds to a perfect Bayesian equilibrium (PBE) in the grand game, and the equilibrium strategies for the subsequent stages, both on and off the equilibrium path, are defined as described above. Conversely, any PBE of the grand game must induce a Nash equilibrium in the first-stage game.

### 3.2. Information Provision as a Location Problem

This subsection discusses the equilibrium and its properties. To this purpose, we transform the firm’s problem in the first stage of the game—which consists of choosing an editorial strategy—into an equivalent location problem on a disk. This transformation is both conceptually and analytically convenient, as it facilitates the interpretation of the equilibrium and allows us to characterize its uniqueness. We do so by transforming the agent’s type  $\theta_i$  and the firm’s editorial strategy  $b_n$  into polar coordinates.

**REMARK 1:** Let  $T = [-\pi, \pi]$ .

- For all  $\theta_i$ , a unique  $t_i \in T$  exists such that  $\theta_i = (1, \cos(t_i), \sin(t_i))$ .
- For all  $b_n$  such that  $\|b_n\| = 1$ , a unique pair  $(x_n, t_n) \in [0, 1] \times T$  exists such that  $b_n = (\sqrt{x_n}, \sqrt{1-x_n} \cos(t_n), \sqrt{1-x_n} \sin(t_n))$ .

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<sup>11</sup>This formula is valid even if  $N = 1$ . In that case,  $\{m \neq 1\} = \emptyset$  and we define  $\max_{m \neq 1} v(b_m|\theta_i) = 0$ .

In light of the equivalence of Remark 1, we abuse terminology and notation in the remainder of the paper and refer to  $t_i$  as the agent’s *type* and refer to the pair  $(x_n, t_n)$  as the firm’s *editorial strategy*.<sup>12</sup>

*Interpretation.* In this equivalent formulation of the model, each agent’s type  $t_i$  is a location on a circle and it is drawn uniformly from the set  $T$ . The closer two types  $t_i$  and  $t_j$  are to each other, the higher is the correlation in their preferences for the policy, namely  $u(\omega, t_i)$  and  $u(\omega, t_j)$ . In this sense, the arc distance between any two types on the circle represents their ideological distance.<sup>13</sup>

A firm’s editorial strategy, in this formulation, is equivalent to choosing the pair  $(x_n, t_n)$ , which has the following interpretation:  $x_n \in [0, 1]$  captures how generalist the firm is, as it measures the relative informativeness of the firm’s signal about the valence versus the ideological components;  $t_n \in T$  is the firm’s target type, who evaluates the different ideological components  $\omega_1$  and  $\omega_2$  of the policy in a way that perfectly matches the corresponding relative weights in the signal designed by the firm.

Graphically, each editorial strategy  $(x_n, t_n)$  corresponds to a location on a disk, as illustrated in Figure 2. In contrast to the familiar Salop (1979) model of product differentiation, firms can locate in the interior of the disk. For example, a firm could locate at the center of the disk by setting  $x_n = 1$ , which corresponds to choosing a maximally generalist editorial strategy. Such a firm would offer a signal that is informative only about the valence component. When  $x_n < 1$ , the firm specializes by locating away from the center, in the direction indicated by  $t_n$ . Such a firm would be offering a signal that is also informative about the two ideological components, which are weighted in a way that is perfectly aligned with the ideological preference of type  $t_n$ .

*The Value of Information, Revisited.* The transformation into polar coordinates also simplifies the expression of the value of information derived in Lemma 2. We can show that it is strictly dominated for firm  $n$  to choose an editorial strategy  $(x_n, t_n)$  such that

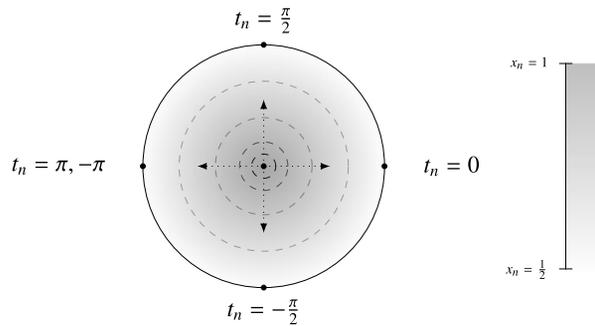


FIGURE 2.—Mapping the firm’s problem into a location choice.

<sup>12</sup>Note that in Remark 1, we focus on editorial strategies for which the constraint  $\|b_n\| \leq 1$  binds. These are the only strategies that firms use in equilibrium as shown in Lemma A.1 (Appendix A).

<sup>13</sup>When this correlation is high, for example, if one agent benefits from a policy, the other is likely to benefit as well. In this sense, they are ideologically similar. A large empirical literature measures polarization using the bliss-point distance as a proxy for ideological distance (Downs (1957)). Our model adds to this literature by showing that two agents can be ideologically different even when their respective “bliss points” are the same. This happens when they trade off the components of the policy in different ways.

$x_n < 1/2$ , irrespective of  $t_n$ . Therefore, without loss of generality, we restrict attention to editorial strategies that satisfy  $x_n \geq 1/2$ . In light of this, the value of information can be written as

$$v((x_n, t_n) | t_i) = \lambda(\sqrt{x_n} + \sqrt{1 - x_n} \cos(t_i - t_n)), \tag{2}$$

where  $\lambda = \frac{1}{2I\sqrt{\pi}}$ .<sup>14</sup> This expression is not only more tractable than that of Lemma 2, but it is also easier to interpret. Net of the scaling factor  $\lambda$ , the value of information is the sum of two terms. The first term,  $\sqrt{x_n}$ , refers to the valence component of the policy. This term is independent of the agent’s type  $t_i$  and is increasing in  $x_n$ —how generalist the firm is. Intuitively, since all agents care about the valence component, a signal that is more informative about it (higher  $x_n$ ) will benefit all agents, irrespective of their types. The second term,  $\sqrt{1 - x_n} \cos(t_i - t_n)$ , refers to the ideological components of the policy. This term is decreasing in  $x_n$  and depends on the agent’s type  $t_i$  as well as the firm’s target  $t_n$ . The lower is  $x_n$ , the more specialized is the firm’s editorial strategy and the more informative it is about a specific mixture of ideological issues. This mixture is determined by  $t_n$  and its value depends on  $\cos(t_i - t_n)$ , which represents the correlation in how agent  $t_i$  and target  $t_n$  evaluate the ideological dimensions of the policy. Intuitively, the closer the agent is to the firm’s target, the higher is the value she attaches to its information.

Equation (2) clarifies the trade-off that firms face when choosing their editorial strategies. By being more generalist, a firm generates higher values even for types that are far away from its chosen target. By being more specialized, instead, the firm generates higher value only for types who are ideologically close to its target. Figure 3 illustrates this trade-off by considering two strategies, both of which target type  $t_n = 0$ . The dotted gray line has a low  $x_n$  and, hence, it is highly specialized. It creates high value for the targeted type and the types nearby, but it creates a low value for agents that are farther away. The dashed dark line has a high  $x_n$  and, hence, it is more generalist. The value it induces is relatively flatter. By being informative about the valence component, it generates value for all agents, even those who are ideologically distant from the targeted agent  $t_n$ .

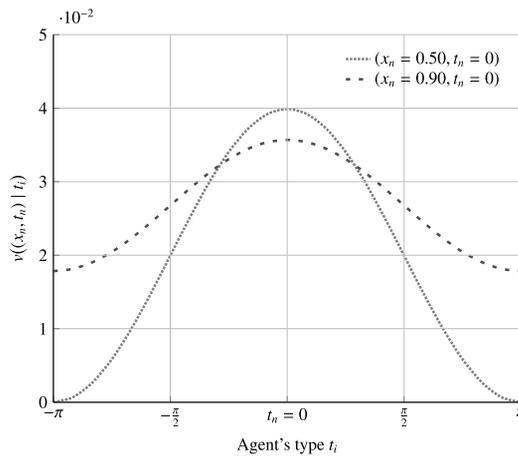


FIGURE 3.—The value of information induced by two editorial strategies (if  $I = 10$ ).

<sup>14</sup>These claims are shown in Lemma A.2.

What is the first-best editorial strategy  $(x_n, t_n)$  for an agent of type  $t_i$ ? From Equation (2), it is easy to see that firm  $n$  maximizes the value of information for type  $t_i$  by directly targeting this type—that is,  $t_n = t_i$ —and assigning equal weight to valence and ideology—that is,  $x_n = 1/2$ . By doing so, the firm induces a signal that is maximally correlated (given the firm’s constraints) with this type’s payoff  $u(\omega, t_i)$ . Let us denote such first-best value by  $\bar{v} = v((1/2, t_i)|t_i)$  and observe that it is independent of  $t_i$ . Note that any editorial strategy with  $x_n < 1/2$  would be overly specialized on ideology, even for the targeted type  $t_n$ . For this reason, in Figure 2,  $x_n = 1/2$  corresponds to the outer border of the disk: we can think of agents as lying on this border, as each one of its points represents the optimal editorial strategy for some type of agent.

*Equilibrium Uniqueness.* Finally, the transformation into polar coordinates discussed in this section is convenient for characterizing the equilibrium of the game, as we do in the next result.

**THEOREM 2—Uniqueness:** *Fix  $N \geq 1$ . There is a unique  $x^*(N) \in [1/2, 1]$  such that, for all equilibria  $(x_n, t_n)_{n=1}^N$ ,  $x_n = x^*(N)$  and  $|t_n - t_m| \geq 2\pi/N$  for all firms  $n$  and  $m$ .*

In equilibrium, all firms are equally specialized and the degree of specialization,  $1 - x^*(N)$ , is uniquely pinned down by  $N$ . Graphically, this means that firms locate equidistantly from the center of the disk. Moreover, firms’ editorial strategies satisfy  $|t_n - t_m| \geq 2\pi/N$  for all  $n$  and  $m$ .<sup>15</sup> Graphically, this means that firms are evenly spread out on an inner circles of the disk (e.g., the dashed circles in Figure 2). Clearly, due to the symmetry in the first-stage game and the uniformity of the type distribution, any relabeling of firms’ names or rotation in their locations also constitutes an equilibrium. Nonetheless, this multiplicity is not important for our main results. From an ex ante perspective, that is, before agents’ types realize, all economically relevant outcomes are uniquely pinned down by  $x^*(N)$  in equilibrium—for example, market share, profits, value of information, and the agent’s welfare.

#### 4. COMPETITION, DISAGREEMENT, AND WELFARE

We exploit the convenient equilibrium characterization discussed in Section 3 to analyze how firms’ and agents’ equilibrium behavior changes as the market for news becomes more competitive. We divide our analysis into four parts. We study how an increase in competition affects (i) the kind of information that firms supply in equilibrium, (ii) the value and the price of information, (iii) the distribution of agents’ opinions, and (iv) the welfare of the agents.

##### 4.1. Competition and the Supply of Information

We begin by characterizing the effects of competition on firms’ equilibrium behavior and, in particular, on the information they supply. We study the effects of competition by comparing equilibria as the number of firms in the market increases. We show that as the market becomes more competitive, a firm’s optimal response is to specialize. Importantly, this “informational” specialization takes a particular form: firms specialize by providing

<sup>15</sup>We write  $t_n + t_m$  (resp.  $t_n - t_m$ ) to indicate the modular addition (resp. subtraction) on the circle  $T$ . For example, if  $t_n = \pi/2$  and  $t_m = 3\pi/2$ , then  $t_n + t_m = 0 \in T$ .

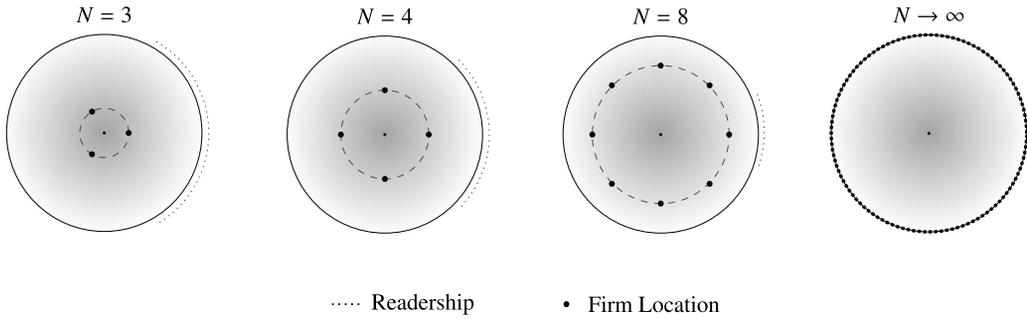


FIGURE 4.—Equilibrium in the information-provision stage.

relatively less information on the valence component, which is the common-interest component in agents’ preferences, and relatively more information on the ideological components.

**PROPOSITION 1:** *The equilibrium  $x^*(N)$  is strictly decreasing in  $N$ . That is, as competition increases, firms specialize by becoming less informative about the valence component of the policy.*

As the market for news becomes more competitive, it becomes increasingly harder for each firm to compete for types that are farther from its target. Indeed, in equilibrium, the firm’s expected readership is an arc of length  $2\pi/N$  centered around the firm’s target type  $t_n$ . As  $N$  increases, the firm’s readership shrinks and, thus, it becomes increasingly homogeneous from an ideological point of view. Expecting to face a more homogeneous set of readers, the firm reacts by further specializing— $x_n$  decreases—and, thus, provides relatively more information on the ideological components of the policy. Graphically, as  $N$  increases, firms locate farther from the center of the disk, as Figure 4 illustrates.

The equilibrium mechanism underlying Proposition 1 can be understood as an information-theoretic counterpart to the more standard idea of product differentiation. Differentiation is a ubiquitous feature of competition games with heterogeneous consumers. However, how do firms differentiate when they sell information? Our result shows that they achieve this by increasing the relative informativeness of private-interest components at the expense of common-interest ones. More broadly, our model captures the equilibrium interactions between vertical and horizontal competition, allowing us to highlight an important effect that has implications beyond the political economy setting studied in this paper. As competition increases, firms disinvest from vertical features—which are beneficial to all consumers—and instead focus on horizontal features—which are beneficial only to a niche segment.

#### 4.2. Competition and the Value of Information

The previous section illustrated how the equilibrium supply of information changes as competition increases. What are the consequences of this change on the agents? In this section, we highlight the positive effects. We focus attention on two main equilibrium objects: the value of information and its price.

We begin with the ex ante perspective of an agent whose type is yet to realize. More precisely, fix an arbitrary equilibrium with  $N$  firms and, in such an equilibrium,

let  $n(t_i)$  denote the firm from which  $t_i$  acquires information. Given this, let  $\mathcal{V}(N) = \mathbb{E}_{t_i}(v((x^*(N), t_{n(t_i)}^*)|t_i))$  be the expected value for the information that agent  $i$  acquires in equilibrium. Similarly, let  $\mathcal{P}(N) = \mathbb{E}_{t_i}(p_{n(t_i)}^*(t_i))$  be its expected price. Note that  $\mathcal{V}(N)$  and  $\mathcal{P}(N)$  are uniquely pinned down as a function of  $N$ —via  $x^*(N)$ —and, thus, do not depend on other features of the equilibrium. We establish the following results.<sup>16</sup>

PROPOSITION 2:

- (a) *The function  $\mathcal{V}$  is strictly increasing in  $N$ . That is, as competition increases, each agent expects to acquire information that is more valuable to her.*
- (b) *The function  $\mathcal{P}$  is strictly decreasing in  $N$ . That is, as competition increases, each agent expects to pay less for the information she acquires.*

The first part in this result speaks to the classic view that sees the market for news as a “marketplace of ideas,” which promotes knowledge and the discovery of truth (Posner (1986)). Competition pushes firms to provide information that is increasingly catered to the specific informational needs of each agent. With such information, each agent can better sway the policy outcome in the direction of her own preferences and, for this reason, she attaches a higher value to it. Furthermore, while each agent obtains better information from the market, she expects to pay a lower price, as established in the second part of the Proposition 2. As a consequence, industry profits decline.

When the number of firms tends to infinity, the market becomes perfectly competitive. In this limit, we show that, conditional on her type, each agent acquires her first-best signal, thus achieving the highest possible value  $\bar{\mathcal{V}}$ . Moreover, she pays a price of zero for it. More precisely, fix  $t_i$  and an arbitrary equilibrium with  $N$  firms. Let  $\mathcal{V}(N|t_i) = v((x^*(N), t_{n(t_i)}^*)|t_i)$  be the value for the information that type  $t_i$  acquires in equilibrium. Similarly, let  $\mathcal{P}(N|t_i) = p_{n(t_i)}^*(t_i)$  be its equilibrium price. While  $\mathcal{V}(N|t_i)$  and  $\mathcal{P}(N|t_i)$  depend on the specific equilibrium that we fixed, their respective limits do not.

REMARK 2—Daily-Me: Fix a type  $t_i$ . Type  $t_i$ ’s equilibrium value of information converges to the first-best,  $\lim_{N \rightarrow \infty} \mathcal{V}(N|t_i) = \bar{\mathcal{V}}$ . Moreover, type  $t_i$ ’s equilibrium price converges to zero,  $\lim_{N \rightarrow \infty} \mathcal{P}(N|t_i) = 0$ .

We refer to this limit result as the daily-me paradigm, a situation in which every consumer in a perfectly competitive market can find an information structure that is exactly tailored to her specific informational needs (Sunstein (2001)). That is, as the market becomes more competitive, the equilibrium value of information converges to the highest possible value for each agent, while its price converges to zero.<sup>17</sup> Graphically, as  $N \rightarrow \infty$ , firms occupy the whole circumference of the disk, where each point on this circumference represents the optimal editorial strategy for some type of agent (Figure 4).

These results show that the equilibrium force that pushes firms to specialize is, indeed, demand-driven. As the number of firms grows, each firm serves a progressively smaller set of agents and provides them with an information structure that is increasingly better suited to their specific needs, thus increasing their value of information. Moreover,

<sup>16</sup>Conceptually similar results hold when we condition on a specific type, as demonstrated by Remark B.3. Taking an ex ante perspective allows us to abstract away from equilibrium multiplicity due to rotation in firms’ locations.

<sup>17</sup>Note that  $\mathcal{V}(N|t_i)$  and  $\mathcal{P}(N|t_i)$  are the interim versions of  $\mathcal{V}(N)$  and  $\mathcal{P}(N)$ , respectively. Therefore, in light of Remark 2, Proposition 2 implies that  $\lim_{N \rightarrow \infty} \mathcal{V}(N) = \bar{\mathcal{V}}$  and  $\lim_{N \rightarrow \infty} \mathcal{P}(N) = 0$ .

competition does not lead to overspecialization. As competition increases, so does the value agents attach to the information they acquire. Incidentally, this explains why no firm has an incentive to deviate back toward the center of the disk by choosing a generalist editorial strategy: since agents consider the signal they acquire in equilibrium to be underspecialized relative to their first-best, an editorial strategy that is highly generalist cannot be enticing for them.

### 4.3. Competition and Social Disagreement

We established that a more competitive market enables agents to learn more effectively about the components of the policy they care about at lower prices. While this is intuitively good at the individual level, it has social repercussions. Indeed, information is not a standard product: its private consumption generates social externalities that arise because of the policy-approval stage, which aggregates agents' preferences. In this section, we begin exploring the effects of competition in light of such externalities. The most apparent one, perhaps, results from agents becoming more informed about increasingly different aspects of the policy—the different mixtures of  $\omega_1$  and  $\omega_2$ —at the expense of the valence component  $\omega_0$ . Consequently, agents' opinions on the policy become increasingly uncorrelated, thus increasing social disagreement.

More precisely, fix an arbitrary equilibrium with  $N$  firms and suppose that, in such an equilibrium, type  $t_i$  acquires information from firm  $n$ , thus observing the realization of signal  $s_i^*(\omega) = s(\omega, (x^*(N), t_n^*))$ . Conditional on such a signal, let  $z_i(t_i) = \mathbb{E}_\omega(u(\omega, t_i) | s_i^*(\omega))$  be the expected payoff that type  $t_i$  associates with the implementation of the policy. We refer to  $z_i(t_i)$  as type  $t_i$ 's equilibrium *opinion* about the policy. As shown in Lemma 1, such a type approves the policy if she has a positive opinion about the policy and disapproves otherwise. A society in which agents' opinions are highly correlated is a society in which agreement is high. Thus, we define *social agreement* as the expected correlation in the opinions of two agents,  $i$  and  $j$ , denoted  $\mathcal{S}(N) = \mathbb{E}_{t_i, t_j}(\text{Corr}(z_i(t_i), z_j(t_j)))$ . Intuitively, a society features high social agreement if it is relatively common to find agents whose opinions about the policy are highly correlated.

**PROPOSITION 3:** *The function  $\mathcal{S}$  is strictly decreasing in  $N$ . That is, social agreement decreases with competition.*

The intuition for this result is simple and it is best conveyed by looking at an extreme example. Consider agents  $i$  and  $j$  with  $t_i = 0$  and  $t_j = \pi/2$ : the former cares about  $\omega_1$ , while the latter cares about  $\omega_2$ . When competition is low, equilibrium editorial strategies are more generalist— $x^*(N)$  is high. That is, even if these two agents acquire information from different firms, their signals are highly informative about the common valence component  $\omega_0$ , about which they both care. Consequently, their opinions  $z_i(t_i)$  and  $z_j(t_j)$  are highly correlated. When  $N$  grows large,  $x^*(N)$  decreases, and both agents can find information that is increasingly tailored to their specific needs. In particular, agent  $i$  can learn relatively more about  $\omega_1$ , while agent  $j$  can learn relatively more about  $\omega_2$ . As a consequence, their opinions depend relatively less on the common component  $\omega_0$ , and relatively more on  $\omega_1$  and  $\omega_2$ , which are independent aspects of the policy. Hence, their opinions become less correlated.

Proposition 3 summarizes an important aspect of the equilibrium mechanism. It is perhaps unsurprising to see that agents are more likely to disagree, provided that they receive more information about  $\omega_1$  and  $\omega_2$ . The subtlety is that there is, in principle, a multitude

of ways in which competition could affect the supply of information. Our model demonstrates that, due to the natural interplay between agents’ incentives to learn and firms’ incentives to maximize profits, competition pushes firms to provide relatively more information precisely about those dimensions on which agents disagree more. This gives rise to a social inefficiency that we document in the next section.

4.4. *Competition and Its Welfare Consequences*

In this section, we conclude our analysis of the effects of competition by studying how increased disagreement ultimately affects agents’ welfare. Our main investigation shows that, in large enough societies, competition strictly decreases the expected welfare of the agents. To this purpose, fix an equilibrium of the game with  $N$  firms. Denote by  $a_i^*(\omega, t_i)$  the approval decision of type  $t_i$  conditional on the information that she receives in equilibrium. This random variable takes a value of 1 if the agent approves the policy and 0 otherwise. The equilibrium approval rate is then  $A^*(\omega, t) = \frac{1}{I} \sum_i a_i^*(\omega, t_i)$ , namely, the fraction of agents who approve the policy. By assumption, this also corresponds to the probability that the society implements policy  $\omega$ . Using this, the expected welfare of an agent is  $\mathcal{U}(N) = \mathbb{E}_{\omega,t}(A^*(\omega, t)u(\omega, t_i) - p^*(t_i))$ . This expression captures both the utility that the agent expects to receive from the implemented policy and the disutility associated with the price that she expects to pay for the information she will acquire in equilibrium. The following result characterizes the effects of competition on the agent’s welfare.

PROPOSITION 4: *There exists  $\bar{I}$  such that, for all societies with  $I > \bar{I}$ ,  $\mathcal{U}$  is strictly decreasing in  $N$ . That is, as competition increases, an agent’s expected welfare decreases.*

Competition has an overall negative effect on an agent’s welfare, despite the positive effects previously highlighted in Proposition 2. To provide intuition for this result, it is useful to decompose agent  $i$ ’s welfare  $\mathcal{U}(N)$  and consider separately agent  $i$ ’s own impact on the policy outcome and the impact of all other agents. Specifically, we have<sup>18</sup>

$$\mathcal{U}(N) = \mathcal{V}(N) + \mathcal{G}(N) - \mathcal{P}(N). \tag{3}$$

The first term  $\mathcal{V}(N)$  is the expected value of information, which we introduced in Section 4.2. This can equivalently be rewritten as  $\frac{1}{I} \mathbb{E}_{\omega,t_i}(a_i^*(\omega, t_i)u(\omega, t_i))$ , which is the impact of agent  $i$ ’s own approval decision on her utility. The second term is  $\mathcal{G}(N) = \frac{1}{I} \mathbb{E}_{\omega,t}(\sum_{j \neq i} a_j^*(\omega, t_j)u(\omega, t_i))$ , which is the impact that others’ approval decisions have on agent  $i$ ’s utility. The last term,  $\mathcal{P}(N)$ , is also familiar from Section 4.2 and denotes the expected price that agent  $i$  pays for the information she acquires.

This decomposition reveals the key features of the equilibrium mechanism highlighted in this paper. Information has both direct and indirect effects on an agent’s welfare. The direct effect is captured by  $\mathcal{V}(N)$ , which measures how an agent values the information that she personally acquires to sway the policy outcome in the direction of her own preferences. The indirect effect is captured by  $\mathcal{G}(N)$ , which measures how an agent values the information that other agents acquire to sway the policy outcome in the direction of their preferences. All agents try to maximize their own impact on the political process and,

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<sup>18</sup>This decomposition follows from the definition of welfare  $\mathcal{U}(N) = \mathbb{E}_{\omega,t}(A^*(\omega, t)u(\omega, t_i) - p^*(t_i))$  and the fact that the approval rate  $A^*(\omega, t)$  can be written as the sum of  $i$ ’s approval decision,  $\frac{1}{I} a_i^*(\omega, t_i)$ , and those of all the other agents,  $\frac{1}{I} \sum_{j \neq i} a_j^*(\omega, t_j)$ . See the proof of Proposition 4 for more details.

thus, acquire information based on its direct value. The profit-seeking firms specialize to meet such demand. From this perspective, it is not surprising that  $\mathcal{V}(N)$  is strictly increasing in  $N$ , as shown in Proposition 2. However, as firms specialize, agents learn about increasingly different aspects of the policy, leading to an increase in social disagreement (Proposition 3). As a consequence, the information that other agents acquire becomes increasingly less valuable to agent  $i$ , as their approval decisions are less likely to benefit her. This decreased  $\mathcal{G}(N)$ —the indirect value of information—captures the externality that agents impose on each other.

When the society is large enough, specifically when  $I \geq 3$ , the overall effect is negative and  $\mathcal{V}(N) + \mathcal{G}(N)$  decreases.<sup>19</sup> That is, as competition increases, the total—direct and indirect—value of the information supplied by the market decreases. It is not surprising that this overall effect depends on the size of the society. In larger societies, agent  $i$ 's own approval decision is less consequential for the final outcome relative to the approval decisions of others. Thus, the increase in  $\mathcal{V}$  cannot compensate for the decline in  $\mathcal{G}$  resulting from competition. More importantly, the reader may wonder if the negative effect highlighted above could be compensated for by the fact that competition also lowers prices. Proposition 4 shows that when  $I$  is sufficiently large,<sup>20</sup> the decrease in prices is unable to compensate for the loss of utility generated by the informational externality.

In conclusion, Proposition 4 highlights how competition in the market for political news can have very different consequences than in other, more traditional markets. Our model illustrates how political information differs from other types of products. Political information has value because it allows agents to influence electoral outcomes in a way that aligns with their own personal preferences. However, by definition, electoral outcomes represent collective decisions that have consequences for all members of the society. This implies that individual information-acquisition strategies have social externalities on others, which are exacerbated by the increase in competition.

*Complete-Information Benchmark.* We conclude this section by highlighting a final result that further illustrates the inefficiency captured by Proposition 4. To do so, we focus on two special sets of policies  $\omega$ , for which either  $u(\omega, t_i) > 0$  for all  $t_i$  or  $u(\omega, t_i) < 0$  for all  $t_i$ . Let us denote them by  $\Omega^+$  and  $\Omega^-$ , respectively. The policies in these sets are special in that if the society could perfectly learn  $\omega$ , agents would unanimously agree on its approval, if  $\omega \in \Omega^+$ , or disapproval, if  $\omega \in \Omega^-$ . Recall that  $A^*(\omega, t)$  is the equilibrium approval rate conditional on policy  $\omega$  and the profile of agents' types  $t$ . It also corresponds to the probability that the society implements policy  $\omega$ . Hence, when  $\omega \in \Omega^+$ , the policy is “correctly” implemented with probability  $A^*(\omega)$ ; equivalently, when  $\omega \in \Omega^-$ , the policy is “correctly” implemented with probability  $1 - A^*(\omega)$ . From an ex ante perspective, the probability the society correctly implements policies in  $\Omega^+$  (resp.  $\Omega^-$ ) is given by  $\mathbb{E}_\omega(A^*(\omega, t) | \omega \in \Omega^+)$  (resp.  $\mathbb{E}_\omega(1 - A^*(\omega, t) | \omega \in \Omega^-)$ ). The next result shows that these terms are decreasing in  $N$ , irrespective of the equilibrium that is played by firms and agents.

REMARK 3: The probability that a policy in  $\Omega^+$  or  $\Omega^-$  is correctly implemented by the society is strictly decreasing in  $N$ .

<sup>19</sup>This is shown in Corollary 1. In passing, note that  $\mathcal{V}(N) + \mathcal{G}(N)$  corresponds to social welfare (i.e., agents and firms). This is because prices simply transfer resources from agents to firms.

<sup>20</sup>Specifically, when  $I$  is larger than  $\bar{I} = 3(1 + 2\pi)$ .

This result allows us to formalize the following idea. In our model, ignorance is not bliss. Rather, there is plenty of scope for information to play a positive role. For example, it could allow agents to identify policies that are uncontroversially good for them. However, the market does not provide such information to the agents. On the contrary, as competition increases, the society is less likely to correctly implement even this class of policies about which there would be full agreement under the complete-information benchmark. This result points to the pervasiveness of the inefficiency in the policy selection that is highlighted by the mechanism of this paper.

### 5. EXTENSIONS

In this section, we discuss the robustness of our main results to some of the simplifying assumptions of our model. This exercise allows us to better appreciate the role of two key ingredients: the heterogeneity in agents’ preferences and the constraints on how much they can learn about the policy.

#### 5.1. Preference Heterogeneity

In our baseline model, we assumed that agents’ types are uniformly distributed on the circle, a ubiquitous assumption in the industrial-organization literature on spatial competition (see Section 1.1). This endows the model with symmetry: firms spread out evenly and this allows us to pin down the equilibrium behavior for all levels of competition, irrespective of the number of firms  $N$ . Thanks to this, we can clearly demonstrate the mechanism that leads firms to change their editorial strategies as  $N$  increases and how such a change affects the value of information, disagreement, and social welfare. In this section, we drop this distributional assumption and consider a more general class of distributions over the agents’ types. These distributions are symmetric around some “median” type  $t^m$ , and their density is bounded away from zero.

**DEFINITION 1:** The distribution  $F$  is *regular* if its density satisfies the following properties: (a) a type  $t^m \in T$  exists such that for any  $\delta > 0$ ,  $f(t^m + \delta) = f(t^m - \delta)$ ; (b) there exists a  $C > 0$  such that  $f(t_i) > C > 0$  for all  $t_i$ .

Regular distributions allow for a richer kind of heterogeneity in agents’ ideological preferences. In doing so, we go beyond the stark distinction between valence and ideology in our baseline model. For example, a regular distribution  $F$  could have a “political center,” with most of its mass around type  $t^m$ , thus restoring the familiar right–left interpretation of ideology that is not possible with the uniform distribution. Unfortunately, moving beyond the uniform distribution means losing tractability: it is no longer feasible to solve for the equilibrium at all  $N$ . Nonetheless, we can show that the main insights of the paper still hold by comparing two notable cases: the monopoly case, where  $N = 1$ , and the perfect competition case, where  $N \rightarrow \infty$ .

**PROPOSITION 5:** Fix a regular distribution  $F$ .

- (a) *Existence.* An equilibrium exists for all  $N \geq 1$  and  $I \geq 1$ .
- (b) *Daily-me.* Fix any  $t_i$ . As  $N \rightarrow \infty$ , the equilibrium value of information for type  $t_i$ ,  $\mathcal{V}(N|t_i)$ , converges to the first-best value  $\bar{\mathcal{V}}$ .
- (c) *Inefficiency.* There exists  $\bar{I}$  such that, for all societies with  $I > \bar{I}$  agents, the agent’s welfare is higher in a monopoly than under perfect competition, that is,  $\mathcal{U}(1) > \lim_{N \rightarrow \infty} \mathcal{U}(N)$ .

There are three results. First, we establish the existence of an equilibrium with an arbitrary number of firms. Such an equilibrium involves possibly mixed editorial strategies in the first stage of the game. Second, we demonstrate that as the market becomes perfectly competitive, every agent can acquire information that is perfectly tailored to her specific needs (the daily-me paradigm). As competition increases, profits decline and firms find it optimal to target even the least populated niches of the market. Third, we show that competition decreases agents' welfare relative to the monopoly benchmark. That is, the inefficiency highlighted by Proposition 4 remains present under this broader class of distributions.

This latter result clarifies the key role that preference heterogeneity plays in our model. Recall from the previous section that the agent's welfare  $\mathcal{U}$  can be decomposed into three terms: the direct value of information  $\mathcal{V}$ , the indirect value of information  $\mathcal{G}$ , and its associated price  $\mathcal{P}$ . Just like in our baseline model, when the type distribution is regular,  $\mathcal{V}$  converges to the daily-me value, while  $\mathcal{P}$  converges to zero. What is perhaps more striking is that even within this broader class of distributions, specialization by firms leads to a decline in the indirect value of information. That is,  $\mathcal{G}$  declines when going from a monopoly to perfect competition.<sup>21</sup> More importantly, the proof of Proposition 5 shows that this decline in  $\mathcal{G}$  is more pronounced—hence, the overall inefficiency is higher—when the heterogeneity in agents' preferences is higher. Formally, the decline in  $\mathcal{G}$  is a function of  $\beta_F := \mathbb{E}_{t_i}(\cos(t_i - t^m)) \in [0, 1)$ , which is the expected correlation between the ideological preferences of an arbitrary agent and the median type  $t^m$ . This statistic of  $F$  is a measure of the degree of homogeneity in the agents' preferences. When  $F$  is uniform, as it is in our baseline model,  $\beta_F = 0$  and the society is maximally heterogeneous. In contrast, when  $F$  approaches a degenerate distribution centered around  $t^m$ ,  $\beta_F \rightarrow 1$  and the society is maximally homogeneous. We show that  $\mathcal{G}(1) - \lim_N \mathcal{G}(N)$  decreases in  $\beta_F$ . This implies that the lower is the value of  $\beta_F$ , the more heterogeneous society becomes and the larger the welfare decline as we transition from the monopoly to perfect competition. From this perspective, we note that our baseline model constitutes a useful extreme benchmark, as it provides the most acute demonstration of the inefficiency associated with competition.

## 5.2. Multimedia

In our model, agents can acquire information from at most one firm (or “single homing”). To understand the implications of this assumption, it is useful to distinguish between two different ways in which competition can affect the market for news. On the one hand, competition could impact what kind of information agents acquire in equilibrium. For example, a more competitive market could allow agents to find information that is better tailored to their needs. This is the channel that we have emphasized in this paper. On the other hand, competition could also impact how much information agents acquire. For example, a more competitive market could cause agents to spend more time on the news. Multimedia consumption (or “multi-homing”) could have implications for both these channels. We briefly sketch two extensions that address the two channels separately.

The first extension is faithful to the main exercise of the paper. In Appendix B.2, we let agents acquire information from multiple firms while maintaining the baseline assumption on how much they can learn. More specifically, we assume that each agent is endowed

<sup>21</sup>The highest value for  $\mathcal{G}$  is achieved when the signal induces a policy outcome that maximizes the utility of an arbitrary agent. The monopolist, due to the lack of competition, captures the whole market and, thus, shares this same goal (see Remark B.1).

with a unit of time, which she can allocate among the  $N$  firms. The agent then observes a signal that is a mixture of the firms’ editorial strategies, with weights determined by the agent’s allocation. By dividing her time on different products, the agent can “construct” new signals that are not directly supplied by the market, but are nonetheless better tailored to her own needs. To maintain tractability, we simplify the pricing stage by making a reduced-form assumption on how editorial strategies map into firms’ profits. With this setup, we prove Proposition 6, which generalizes the results of Section 5.1. In particular, we show that a perfectly competitive market decreases agents’ welfare relative to the monopoly benchmark.

The second extension relaxes the constraint on how much agents can learn. In Appendix C.1, we allow the precision of the signal received by an agent to exogenously increase with the number of firms in the market. This dependence could be the result of firms investing more in news production as competition intensifies, or it could be due to agents spending more time acquiring information from one or multiple sources. We do not mean to suggest that such changes are plausible;<sup>22</sup> our goal is merely to study the limits of our results in the presence of such changes. Proposition 7 in Appendix C shows that the results of Section 5.1 can be extended to settings where competition leads to some increase in the signal’s precision. However, our result reverses when the increase in precision is excessively large. For example, if agents become fully informed in the limit, the perfectly competitive market can make agents better off. This result is useful as it demonstrates once again that there is plenty of scope for information to play a positive role in our model (see also the end of Section 4.4). In doing so, it highlights that the main inefficiency identified in our paper ultimately stems from the trade-offs that firms and agents face when choosing which aspects of the policy to emphasize and what kind of information to acquire, respectively. These trade-offs imply that a competitive market leads to informational specialization, which results in agents becoming less informed about components of the policy that are of common interest.

## APPENDIX A: PROOFS

### A.1. Proofs for Section 3

#### A.1.1. Equilibrium Characterization

PROOF OF LEMMA 1: Fix an arbitrary profile of editorial strategies  $(b_1, \dots, b_N)$  and types  $(\theta_1, \dots, \theta_I)$ . Fix agent  $i$  and an arbitrary signal realization  $\bar{s}_i \in \mathbb{R}$ . Let  $a_j(\omega, \theta_j)$  for  $j \neq i$  be agent  $j$ ’s approval strategy. Denote by  $A_{-i}(\omega, \theta_{-i}) = I^{-1} \sum_{j \neq i} a_j(\omega, \theta_j)$  the approval rate excluding  $i$ . If  $i$  approves, the policy is implemented with probability  $A_{-i}(\omega, \theta_{-i}) + 1/I$ . If  $i$  disapproves, instead, the policy is implemented with probability  $A_{-i}(\omega, \theta_{-i})$ . When the policy is implemented, the agent earns  $u(\omega, \theta_i)$  and zero otherwise. Therefore, the value of agent  $i$ ’s problem is

$$\begin{aligned} & \max\{\mathbb{E}_\omega(A_{-i}(\omega, \theta_{-i})u(\omega, \theta_i)|s_i(\omega, b_n) = \bar{s}_i), \\ & \quad \mathbb{E}_\omega((A_{-i}(\omega, \theta_{-i}) + 1/I)u(\omega, \theta_i)|s_i(\omega, b_n) = \bar{s}_i)\} \\ & = \mathbb{E}_\omega(A_{-i}(\omega, \theta_{-i})u(\omega, \theta_i)|s_i(\omega, b_n) = \bar{s}_i) \\ & \quad + I^{-1} \max\{0, \mathbb{E}_\omega(u(\omega, \theta_i)|s_i(\omega, b_n) = \bar{s}_i)\}, \end{aligned}$$

<sup>22</sup>In fact, Cagé (2020) empirically shows that increased competition leads newspapers to reduce investments.

where the second line exploits the linearity of the operator  $\mathbb{E}_\omega$ . Therefore, the agent approves the policy if and only if  $\mathbb{E}_\omega(u(\omega, \theta_i)|s_i(\omega, b_n) = \bar{s}_i) \geq 0$ . *Q.E.D.*

**PROOF OF LEMMA 2:** Fix agent  $i$  of type  $\theta_i$ . Consider an arbitrary profile of approval strategies for agents other than  $i$ ,  $a_j(\omega, \theta_j)$  for  $j \neq i$ . Denote by  $A_{-i}(\omega, \theta_{-i}) = I^{-1} \sum_{j \neq i} a_j(\omega, \theta_j)$  the resulting approval rate excluding  $i$ . First, we compute the expected utility if type  $\theta_i$  does not receive any information:

$$\begin{aligned} & \max\{\mathbb{E}_\omega(A_{-i}(\omega, \theta_{-i})u(\omega, \theta_i)), \mathbb{E}_\omega((A_{-i}(\omega, \theta_{-i}) + 1/I)u(\omega, \theta_i))\} \\ &= \mathbb{E}_\omega(A_{-i}(\omega, \theta_{-i})u(\omega, \theta_i)) + I^{-1} \max\{0, \mathbb{E}_\omega(u(\omega, \theta_i))\} \\ &= \mathbb{E}_\omega(A_{-i}(\omega, \theta_{-i})u(\omega, \theta_i)). \end{aligned}$$

The last equality holds because  $\mathbb{E}_\omega(u(\omega, \theta_i)) = 0$ , since  $\mathbb{E}_\omega \omega_k = 0$  for  $k \in \{0, 1, 2\}$ .

Second, we compute type  $\theta_i$ 's expected utility when she observes the signal induced by  $b_n$ :

$$\begin{aligned} & \mathbb{E}_{\bar{s}_i}(\max\{\mathbb{E}_\omega(A_{-i}(\omega, \theta_{-i})u(\omega, \theta_i)|s(\omega, b_n) = \bar{s}_i), \\ & \quad \mathbb{E}_\omega((A_{-i}(\omega, \theta_{-i}) + 1/I)u(\omega, \theta_i)|s(\omega, b_n) = \bar{s}_i)\}) \\ &= \mathbb{E}_{\bar{s}_i}(\mathbb{E}_\omega(A_{-i}(\omega, \theta_{-i})u(\omega, \theta_i)|s(\omega, b_n) = \bar{s}_i)) \\ & \quad + I^{-1} \mathbb{E}_{\bar{s}_i}(\max\{0, \mathbb{E}_\omega(u(\omega, \theta_i)|s(\omega, b_n) = \bar{s}_i)\}). \end{aligned}$$

In the second line, let us separately analyze the two components of the sum. By the law of iterated expectations, the first component is

$$\mathbb{E}_{\bar{s}_i}(\mathbb{E}_\omega(A_{-i}(\omega, \theta_{-i})u(\omega, \theta_i)|s(\omega, b_n) = \bar{s}_i)) = \mathbb{E}_\omega(A_{-i}(\omega, \theta_{-i})u(\omega, \theta_i)).$$

For the second component, let us note that  $u(\omega, \theta_i) \sim \mathcal{N}(0, \|\theta_i\|^2)$  and  $s_i(\omega, b_n) = b_n \cdot \omega + \varepsilon_i \sim \mathcal{N}(0, 1 + \|b_n\|^2)$ . By the properties of conditional expectations under normal distributions, we have that

$$\begin{aligned} \mathbb{E}_\omega(u(\omega, \theta_i)|s(\omega, b_n) = \bar{s}_i) &= \frac{\theta_i \cdot b_n}{\|\theta_i\| \sqrt{1 + \|b_n\|^2}} \frac{\|\theta_i\|}{\sqrt{1 + \|b_n\|^2}} \bar{s}_i \\ &= \frac{\theta_i \cdot b_n}{1 + \|b_n\|^2} \bar{s}_i \sim \mathcal{N}\left(0, \frac{(\theta_i \cdot b_n)^2}{1 + \|b_n\|^2}\right); \end{aligned} \tag{A.1}$$

that is, the interim expectation  $\mathbb{E}_\omega(u(\omega, \theta_i)|s(\omega, b_n) = \bar{s}_i)$  is itself a random variable that is normally distributed. Therefore,

$$\begin{aligned} \mathbb{E}_{\bar{s}_i}(\max\{0, \mathbb{E}_\omega(u(\omega, \theta_i)|s(\omega, b_n) = \bar{s}_i)\}) &= \frac{1}{2} \mathbb{E}_{\bar{s}_i}(|\mathbb{E}_\omega(u(\omega, \theta_i)|s(\omega, b_n) = \bar{s}_i)|) \\ &= \frac{1}{2} \frac{\sqrt{2}}{\sqrt{\pi}} \sqrt{\frac{(\theta_i \cdot b_n)^2}{1 + \|b_n\|^2}} \\ &= \frac{|\theta_i \cdot b_n|}{\sqrt{2\pi(1 + \|b_n\|^2)}}, \end{aligned}$$

where the second equality uses the formula for the expectation of the absolute value of a normal distribution with mean zero and variance as defined above. Therefore, the value of information induced by  $b_n$  for an agent of type  $\theta_i$  is

$$\begin{aligned} v(b_n|\theta_i) &= \mathbb{E}_\omega(A_{-i}(\omega, \theta_{-i})u(\omega, \theta_i)) + \frac{|\theta_i \cdot b_n|}{I\sqrt{2\pi(1 + \|b_n\|^2)}} - \mathbb{E}_\omega(A_{-i}(\omega, \theta_{-i})u(\omega, \theta_i)) \\ &= \frac{|\theta_i \cdot b_n|}{I\sqrt{2\pi(1 + \|b_n\|^2)}}. \end{aligned}$$

This concludes the proof.

*Q.E.D.*

LEMMA A.1: *It is never optimal for a firm to choose a strategy  $b_n$  such that  $\|b_n\| < 1$ .*

PROOF: Let  $b_n$  be such that  $\|b_n\| < 1$ . We show that there exists a  $b'_n$  such that, for all  $\theta_i$ ,  $v(b'_n|\theta_i) > v(b_n|\theta_i)$ . Define  $c = 1/\|b_n\| > 1$  and  $b'_n = cb_n$ . Notice that  $\|b'_n\| = 1$  and  $|\theta_i b'_n| = c|\theta_i b_n|$ . By Lemma 2,

$$\begin{aligned} v(b_n|\theta_i) &= \frac{|\theta_i \cdot b_n|}{I\sqrt{2\pi}} \frac{1}{\sqrt{1 + \|b_n\|^2}} \\ &< \frac{|\theta_i \cdot b_n|}{I\sqrt{2\pi}} \frac{1}{\sqrt{\|b_n\|^2 + \|b_n\|^2}} = \frac{|\theta_i \cdot b_n|}{I\sqrt{2\pi}} \frac{1}{\sqrt{2}\|b_n\|} \\ &= \frac{|\theta_i \cdot b_n|}{I\sqrt{2\pi}} \frac{c}{\sqrt{2}} = \frac{|\theta_i \cdot b'_n|}{2I\sqrt{\pi}} = v(b'_n|\theta_i). \end{aligned}$$

Therefore, since  $\theta_i$  was arbitrary, editorial strategy  $b_n$  with  $\|b_n\| < 1$  is strictly dominated.

*Q.E.D.*

PROOF OF REMARK 1: Fix  $\theta_i$ . By assumption,  $\|\theta_i\| = 2$  and  $\theta_{i,0} = 1$ . That is,  $\theta_{i,1}^2 + \theta_{i,2}^2 = 1$  and  $(\theta_{i,1}, \theta_{i,2})$  is a point on the unit circle. Thus, there exists a unique  $t_i \in T = [-\pi, \pi]$  such that  $(\theta_{i,1}, \theta_{i,2}) = (\cos(t_i), \sin(t_i))$ . Therefore,  $u(\omega, \theta_i) = \omega_0 + \omega_1\theta_{i,1} + \omega_2\theta_{i,2} = \omega_0 + \omega_1 \cos(t_i) + \omega_2 \sin(t_i)$ . Now fix an arbitrary  $b_n$ . Clearly,

$$s_i(\omega, b_n) = \omega_0 b_{n,0} + \sqrt{\|b_n\|^2 - b_{n,0}^2} \left( \omega_1 \frac{b_{n,1}}{\sqrt{\|b_n\|^2 - b_{n,0}^2}} + \omega_2 \frac{b_{n,2}}{\sqrt{\|b_n\|^2 - b_{n,0}^2}} \right) + \varepsilon_i.$$

Moreover,  $\frac{b_{n,1}^2}{\|b_n\|^2 - b_{n,0}^2} + \frac{b_{n,2}^2}{\|b_n\|^2 - b_{n,0}^2} = 1$ . Therefore,  $(\frac{b_{n,1}}{\sqrt{\|b_n\|^2 - b_{n,0}^2}}, \frac{b_{n,2}}{\sqrt{\|b_n\|^2 - b_{n,0}^2}})$  is a point on the unit circle and it equals  $(\cos(t_n), \sin(t_n))$  for a unique  $t_n \in T$ . Letting  $x_n = b_{n,0}^2 \in [0, \|b_n\|^2]$ , we have

$$s_i(\omega, b_n) = \sqrt{x_n}\omega_0 + \sqrt{\|b_n\|^2 - x_n}(\omega_1 \cos(t_n) + \omega_2 \sin(t_n)) + \varepsilon_i.$$

Setting  $\|b_n\| = 1$  concludes the proof.

*Q.E.D.*

LEMMA A.2: *It is never optimal for a firm to choose an editorial strategy  $(x_n, t_n)$  with  $x_n < 1/2$ . Moreover, setting  $\lambda = \frac{1}{2I\sqrt{\pi}}$ , the value of information  $(x_n, t_n)$  when  $x_n \geq 1/2$  can be written as*

$$v((x_n, t_n) | t_i) = \lambda(\sqrt{x_n} + \sqrt{1 - x_n} \cos(t_i - t_n)).$$

PROOF: Fix an arbitrary strategy  $b_n$ . By Remark 1 and its proof, notice that

$$|b_n \cdot \theta_i| = |\sqrt{x_n} + \sqrt{1 - x_n} \cos(t_i - t_n)|.$$

To establish this equality, we used the angle-addition trigonometric identity  $\cos(t_n) \cos(t_i) + \sin(t_n) \sin(t_i) = \cos(t_i - t_n)$ . It is straightforward to see that for all  $(x_n, t_n)$  with  $x_n \geq 1/2$ ,  $\sqrt{x_n} + \sqrt{1 - x_n} \cos(t_i - t_n) \geq 0$  for all  $t_i$  and  $t_n$ . Therefore, whenever  $x_n \geq 1/2$ , the value of information simplifies to

$$v((x_n, t_n) | t_i) = \frac{1}{2I\sqrt{\pi}}(\sqrt{x_n} + \sqrt{1 - x_n} \cos(t_i - t_n)).$$

Now fix  $(x_n, t_n)$  with  $x_n < 1/2$ . We want to show that there is a feasible  $(x'_n, t'_n)$  such that  $v((x'_n, t'_n) | t_i) \geq v((x_n, t_n) | t_i)$  for all  $t_i$ . To see this, let  $x'_n = 1 - x_n > 1/2$  and  $t'_n = t_n$ . We need to show that

$$\sqrt{1 - x_n} + \sqrt{x_n} \cos(t_i - t_n) \geq |\sqrt{x_n} + \sqrt{1 - x_n} \cos(t_i - t_n)|.$$

Let us first consider the case when the argument in the absolute value is positive. Then

$$\begin{aligned} \sqrt{1 - x_n} + \sqrt{x_n} \cos(t_i - t_n) &\geq \sqrt{x_n} + \sqrt{1 - x_n} \cos(t_i - t_n), \\ (\sqrt{1 - x_n} - \sqrt{x_n})(1 - \cos(t_i - t_n)) &\geq 0. \end{aligned}$$

Note that  $\sqrt{1 - x_n} - \sqrt{x_n} \geq 0$ , since  $x_n < 1/2$ . Therefore, the above inequality holds for all  $t_i$  and  $t_n$ . Next, we consider the case when the argument in the absolute value is negative. In such a case,

$$\begin{aligned} \sqrt{1 - x_n} + \sqrt{x_n} \cos(t_i - t_n) &\geq -\sqrt{x_n} - \sqrt{1 - x_n} \cos(t_i - t_n), \\ (\sqrt{1 - x_n} + \sqrt{x_n})(1 + \cos(t_i - t_n)) &\geq 0, \end{aligned}$$

which trivially holds for all  $t_i$  and  $t_n$ . Since  $v((x_n, t_n) | t_i) \leq v((1 - x_n, t_n) | t_i)$  for all  $t_i$ , the firm can weakly increase its profit by deviating from  $(x_n, t_n)$  to  $(1 - x_n, t_n)$ . It is therefore with no loss of generality to focus on editorial strategies  $(x_n, t_n)$  that have  $x_n \geq 1/2$ . *Q.E.D.*

### A.1.2. Proving Theorem 1

It is convenient to prove the statement of the theorem using the polar-coordinate transformation illustrated in Remark 1. Recall that the circle is defined on  $T = [\pi, \pi]$  and that we use a modular convention: For example,  $t_n = 2\pi$  and  $t'_n = 0$  do indicate the same type.

PROOF OF THEOREM 1: If  $N = 1$ , the profit of the (monopolist) firm when choosing editorial strategy  $(x_1, t_1)$  is

$$\begin{aligned} I \int_{-\pi}^{\pi} v((x_1, t_1)|t_i) dF(t_i) &= I \int_{-\pi}^{\pi} v((x_1, 0)|t_i) dF(t_i) \\ &= I\sqrt{x_1} + I\sqrt{1-x_1} \int_{-\pi}^{\pi} \cos(t_i) dF(t_i) = I\sqrt{x_1}. \end{aligned}$$

The last inequality follows from the fact that  $F$  is the cumulative distribution function (cdf) of the uniform distribution on  $T = [-\pi, \pi]$ . Therefore,  $x_1 = x^*(1) = 1$  maximizes the monopolist’s profit.

Now let  $N \geq 2$ . We divide proof into two parts. First, we establish the existence and uniqueness of  $x^* \in [1/2, 1]$  such that if the  $N$  firms are evenly spread on the circle, no firm  $n$  would want to unilaterally deviate by choosing an  $x_n \neq x^*$ . Second, we establish that if all firms  $n' \neq n$  choose  $x_{n'} = x^*$  and are evenly located on the circle, firm  $n$  does not have incentives to deviate away from  $(x^*, t_n^*)$  to a different strategy  $(x_n, t_n)$ .

*Part 1.* Consider a candidate profile of strategies  $(x_n, t_n)_{n=1}^N$ . Suppose that firms’ locations  $(t_n)_{n=1}^N$  are evenly spread on the circle and, without loss of generality, let  $t_n = 0$ . Moreover, let  $x_{n'} = \bar{x} \in [1/2, 1]$  for all  $n' \neq n$ . Define  $V((x_{n'}, t_{n'})_{n' \neq n}|t_i) = \max\{v((x_{n'}, t_{n'})|t_i) : n' \neq n\}$ . Let  $R_n := \{t_i | v((x_n, t_n)|t_i) \geq V((x_{n'}, t_{n'})_{n' \neq n}|t_i)\}$  be the *readership* of firm  $n$ , namely, the set of types for whom firm  $n$  generates a weakly higher value than the competition. Thus, the profit for firm  $n$ , defined in Equation (1), can be rewritten as

$$\begin{aligned} \Pi((x_n, t_n = 0), (x_{n'}, t_{n'})_{n' \neq n}) &= I \int_{-\pi}^{\pi} \max\{0, v((x_n, t_n)|t_i) - V((x_{n'}, t_{n'})_{n' \neq n}|t_i)\} dF(t_i) \\ &= I \int_{R_n} v((x_n, t_n)|t_i) - V((x_{n'}, t_{n'})_{n' \neq n}|t_i) dF(t_i). \end{aligned}$$

Notice that readership  $R_n$  is equal to the union of intervals  $R_n = \bigcup_{k=1}^K [\bar{t}_l^k, \bar{t}_r^k]$ . We guess and later verify that  $K$  is finite (indeed, equal to 1). We refer to  $\bar{t}_l^k$  and  $\bar{t}_r^k$  as *threshold* types. Thus,

$$\Pi((x_n, t_n = 0), (x_{n'}, t_{n'})_{n' \neq n}) = I \sum_{k=1}^K \int_{\bar{t}_l^k}^{\bar{t}_r^k} v((x_n, t_n)|t_i) - V((x_{n'}, t_{n'})_{n' \neq n}|t_i) dF(t_i). \tag{A.2}$$

The derivative of such function with respect to  $x_n$  is given by

$$\Pi_{x_n}((x_n, t_n = 0), (x_{n'}, t_{n'})_{n' \neq n}) = I \sum_{k=1}^K \frac{d}{dx_n} \int_{\bar{t}_l^k}^{\bar{t}_r^k} v((x_n, t_n)|t_i) - V((x_{n'}, t_{n'})_{n' \neq n}|t_i) dF(t_i).$$

Importantly, for each  $k$ ,

$$\begin{aligned} & \frac{d}{dx_n} \int_{\bar{t}_l^k}^{\bar{t}_r^k} v((x_n, t_n)|t_i) - V((x_{n'}, t_{n'})_{n' \neq n}|t_i) dF(t_i) \\ &= \int_{\bar{t}_l^k}^{\bar{t}_r^k} \frac{d}{dx_n} v((x_n, t_n)|t_i) dF(t_i) \\ &= \frac{1}{2\pi} \left( \frac{1}{2\sqrt{x_n}} (\bar{t}_r^k - \bar{t}_l^k) - \frac{1}{2\sqrt{1-x_n}} (\sin(\bar{t}_r^k) - \sin(\bar{t}_l^k)) \right). \end{aligned}$$

The first equality holds because, by definition of each threshold type  $\bar{t}_z^k$  for  $z \in \{l, r\}$ ,  $v((x_n, t_n)|\bar{t}_z^k) - V((x_{n'}, t_{n'})_{n' \neq n}|\bar{t}_z^k) = 0$ . Therefore, all terms with  $d\bar{t}_z^k/dx_n$  cancel. Thus,

$$\begin{aligned} & \Pi_{x_n}((x_n, t_n = 0), (x_{n'}, t_{n'})_{n' \neq n}) \\ &= \frac{I}{2\pi} \left( \frac{1}{2\sqrt{x_n}} \sum_{k=1}^K (\bar{t}_r^k - \bar{t}_l^k) - \frac{1}{2\sqrt{1-x_n}} \sum_{k=1}^K (\sin(\bar{t}_r^k) - \sin(\bar{t}_l^k)) \right). \end{aligned} \tag{A.3}$$

Setting this derivative equal to zero gives the equilibrium condition

$$\sqrt{\frac{1-x_n}{x_n}} = \frac{\sum_{k=1}^K (\sin(\bar{t}_r^k) - \sin(\bar{t}_l^k))}{\sum_{k=1}^K (\bar{t}_r^k - \bar{t}_l^k)}.$$

When  $x_n = \bar{x}$ ,  $K = 1$ , that is, readership is a single connected interval. To see this, note that a necessary condition for  $K > 1$  is that  $v((x_n, t_n = 0)|3\pi/N) > v((\bar{x}, 2\pi/N)|3\pi/N)$  or, equivalently,  $v((x_n, t_n = 0)|3\pi/N) > v((\bar{x}, 0)|\pi/N)$ . This is ruled out by Lemma B.7 and the fact that  $v((x_n, t_n = 0)|3\pi/N) < v((x_n, t_n = 0)|2\pi/N)$  in this range. Therefore, the equilibrium condition above simplifies to

$$\sqrt{\frac{1-\bar{x}}{\bar{x}}} = \frac{\sin(\bar{t}_r) - \sin(\bar{t}_l)}{\bar{t}_r - \bar{t}_l} = \frac{\sin(\bar{t}_r)}{\bar{t}_r} = \frac{\sin(\pi/N)}{\pi/N}. \tag{A.4}$$

In the equation above, we dropped the index  $k = 1$  for notational simplicity. In the second equality, we used the fact that since  $(t_n)_{n=1}^N$  are equidistant,  $\bar{t}_l = -\bar{t}_r$ . Finally, in the last equality, we used the fact that since  $x_n = \bar{x}$ , the threshold type  $\bar{t}_r$  is  $\pi/N$ . It is immediate to see that this equation has a unique solution  $\bar{x} = x^* \in (1/2, 1)$ .

*Part 2.* To verify that  $(x^*, t_n)_{n=1}^N$  is indeed an equilibrium, we need to make sure there is no profitable deviation  $(x'_n, t'_n)$  for firm  $n$ , provided that every other firm follows  $(x^*, t_{n'})_{n' \neq n}$ . Our strategy is to show that  $\Pi_n((x'_n, t'_n), (x^*, t_{n'})_{n' \neq n}) < 0$  for arbitrary  $(x'_n, t'_n)$  with  $x'_n \in [1/2, 1]$  and  $t'_n \in (0, 2\pi/N)$ . Note that a deviation in the opposite direction,  $t'_n \in (-2\pi/N, 0)$ , would lead to a derivation that is identical to the one below. Therefore, we omit this case. The derivative of the profit function, as expressed in Equation (A.2), is

$$\Pi_{t_n}((x'_n, t'_n), (x^*, t_{n'})_{n' \neq n}) = I \sum_{k=1}^K \frac{d}{dt_n} \int_{\bar{t}_l^k}^{\bar{t}_r^k} v((x'_n, t'_n)|t_i) - V((x^*, t_{n'})_{n' \neq n}|t_i) dF(t_i).$$

As in Part 1, for each  $k$ , the derivative in  $t_n$  simplifies and we get

$$\begin{aligned} & \frac{d}{dt_n} \int_{\bar{t}_l^k}^{\bar{t}_r^k} v((x'_n, t'_n)|t_i) - V((x^*, t'_n)_{n' \neq n}|t_i) dF(t_i) \\ &= \int_{\bar{t}_l^k}^{\bar{t}_r^k} \frac{d}{dt_n} v((x'_n, t'_n)|t_i) dF(t_i) \\ &= -\frac{1}{2\pi} \sqrt{1 - x'_n} (\cos(\bar{t}_r^k - t'_n) - \cos(\bar{t}_l^k - t'_n)). \end{aligned}$$

Therefore,

$$\Pi_{t_n} < 0 \iff \sum_{k=1}^K (\cos(\bar{t}_r^k - t'_n) - \cos(\bar{t}_l^k - t'_n)) > 0. \tag{A.5}$$

Let us first consider the case when  $K = 1$ , that is, the readership is a single interval. To simplify notation, we drop the index  $k = 1$  and denote the readership interval  $R_n = [\bar{t}_l, \bar{t}_r]$ . By definition,  $\bar{t}_l \leq \bar{t}_r$  and  $t_n \in [\bar{t}_l, \bar{t}_r]$ . Moreover,  $\bar{t}_l \geq -2\pi/N$ . To see this, note that if  $\bar{t}_l < -2\pi/N$ , we would need  $v((x'_n, t'_n)|-2\pi/N) > v((x^*, -2\pi/N)|-2\pi/N)$ . However, this is not possible due to Lemma B.7 and the fact that  $v((x'_n, t'_n)|-2\pi/N) \leq v((x'_n, 0)|-2\pi/N) = v((x'_n, 0)|2\pi/N)$  and  $v((x^*, -2\pi/N)|-2\pi/N) = v((x^*, 0)|0)$ .

We consider three different cases, according to which values  $\bar{t}_l$  and  $\bar{t}_r$  take.

Case 1. Suppose  $\bar{t}_l \geq 0$ . Note that this implies  $\bar{t}_l \leq 2\pi/N$ . If this was not the case,  $\bar{t}_n \geq 2\pi/N$ —a contradiction. Let us assume by contradiction that  $\cos(\bar{t}_r - t'_n) \leq \cos(\bar{t}_l - t'_n)$ . This is equivalent to assuming that  $v((x'_n, t'_n)|\bar{t}_l) \geq v((x'_n, t'_n)|\bar{t}_r)$ . Define  $\hat{t} = 2\pi/N + 2\pi/N - \bar{t}_l$ . By construction, type  $\hat{t}$  is located as far to the right of  $2\pi/N$  as  $t_l$  is to the left of  $2\pi/N$ . Because  $v((x^*, 2\pi/N)|t_i)$  is symmetric around  $2\pi/N$ , we have  $v((x^*, 2\pi/N)|\bar{t}_l) = v((x^*, 2\pi/N)|\hat{t})$ . Since, by assumption,  $v((x^*, 2\pi/N)|\hat{t}) \geq v((x'_n, t'_n)|\bar{t}_r)$ , it must be that  $v((x'_n, t'_n)|\hat{t}) \geq v((x^*, 2\pi/N)|\hat{t})$ . Therefore, we have

$$v((x'_n, t'_n)|\bar{t}_l) \leq v((x'_n, t'_n)|\hat{t}) \implies \cos(\bar{t}_l - t'_n) \leq \cos(\hat{t} - t'_n).$$

Note that  $\bar{t}_l - t'_n \leq 0$  and  $\hat{t} - t'_n \geq 0$ . Thus,  $\bar{t}_l - t'_n \leq -\hat{t} + t'_n$  or

$$t_n \geq \frac{\hat{t} + t_l}{2} = \frac{2\pi/N + 2\pi/N - \bar{t}_l + t_l}{2} = 2\pi/N,$$

which contradicts our initial assumption that  $t_n < 2\pi/N$ .

Case 2. We now suppose that  $\bar{t}_l \leq 0$  and  $\bar{t}_r \leq 2\pi/N$ . This necessarily implies that  $v((x^*, 2\pi/N)|\bar{t}_r) = v((x'_n, t'_n)|\bar{t}_r)$  and  $v((x^*, -2\pi/N)|\bar{t}_l) = v((x'_n, t'_n)|\bar{t}_l)$ . As before, let us assume by contradiction that  $\cos(\bar{t}_r - t'_n) \leq \cos(\bar{t}_l - t'_n)$ . This is equivalent to assuming that  $v((x'_n, t'_n)|\bar{t}_l) \geq v((x'_n, t'_n)|\bar{t}_r)$ . Since  $v((x'_n, t'_n)|t_i)$  is symmetric in  $t_i$  relative to  $t'_n$ , this means that  $t'_n \leq \frac{1}{2}(\bar{t}_r + \bar{t}_l)$ . By assumption, we also have that  $v((x^*, -2\pi/N)|\bar{t}_l) \geq v((x^*, 2\pi/N)|\bar{t}_r)$ , which implies  $\cos(\bar{t}_l + 2\pi/N) \geq \cos(\bar{t}_r - 2\pi/N)$ , which requires  $|\bar{t}_l + 2\pi/N| < |\bar{t}_r - 2\pi/N|$ . By assumption,  $\bar{t}_l + 2\pi/N \geq 0$  and  $\bar{t}_r - 2\pi/N < 0$ . Therefore, we have that  $-\bar{t}_l - 2\pi/N \geq \bar{t}_r - 2\pi/N$ , hence,  $\bar{t}_r + \bar{t}_l \leq 0$ . Since  $t'_n \leq \frac{1}{2}(\bar{t}_r + \bar{t}_l)$ , we have  $t'_n \leq 0$ —a contradiction.

Case 3. Finally, suppose that  $\bar{t}_l \leq 0$  and  $\bar{t}_r \geq 2\pi/N$ . As before, suppose by contradiction that  $v((x'_n, t'_n)|\bar{t}_l) \geq v((x'_n, t'_n)|\bar{t}_r)$ . This implies that  $v((x^*, -2\pi/N)|\bar{t}_l) \geq$

$v((x^*, 2\pi/N)|\bar{t}_r)$ . This holds irrespective of whether  $v((x^*, 2\pi/N)|\bar{t}_r) = v((x'_n, t'_n)|\bar{t}_r)$  or  $v((x^*, 2\pi/N)|\bar{t}_r) < v((x'_n, t'_n)|\bar{t}_r)$ . Therefore,  $\cos(\bar{t}_l + 2\pi/N) \geq \cos(\bar{t}_r - 2\pi/N)$ . By assumption,  $\bar{t}_l + 2\pi/N \geq 0$  and  $\bar{t}_r - 2\pi/N \geq 0$ . Therefore,  $\bar{t}_l + 2\pi/N \leq \bar{t}_r - 2\pi/N$  and, hence,  $\bar{t}_r - \bar{t}_l \geq 4\pi/N$ . Moreover, note that  $v((x'_n, t'_n)|\bar{t}_r)$  is bounded below by  $v((x^*, 2\pi/N)|3\pi/N)$  or, equivalently, by  $v((x^*, 0)|\pi/N)$ . A necessary condition for  $\bar{t}_r - \bar{t}_l \geq 4\pi/N$  and  $v((x'_n, t'_n)|\bar{t}_r) \geq v((x^*, 0)|\pi/N)$  to be jointly true is that there exists a  $x'_n \in [1/2, 1]$  such that  $v((x'_n, 0)|2\pi/N) \geq v((x^*, 0)|\pi/N)$ . By Lemma B.7, this is not possible; hence, we have a contradiction.

Therefore, we showed that when  $K = 1$ ,  $\Pi_n < 0$ . Hence, the arbitrary deviation  $(x'_n, t'_n)$  cannot be a profitable one.

To conclude the proof, we analyze the case  $K > 1$ . In this case, deviation  $(x'_n, t'_n)$  generates a readership with  $K$  disconnected intervals. Note that  $K > 1$  is possible only if  $N > 2$ . Therefore, let  $N \geq 3$  for the remainder of the proof. Consider an arbitrary deviation  $(x'_n, t'_n)$  with  $t'_n \in (0, 2\pi/N)$ . We begin by noting that firm  $n$  cannot win over type  $t = -3\pi/N$ . That is,

$$v((x'_n, t'_n)|-3\pi/N) \leq v((x'_n, 0)|-3\pi/N) \leq v((x^*, -2\pi/N)|-3\pi/N).$$

This is equivalent to showing that, for all  $x'_n \in [1/2, 1]$ ,  $v((x'_n, 0)|3\pi/N) \leq v((x^*, 0)|\pi/N)$ , which immediately follows from Lemma B.7. Next, we show that firm  $n$  cannot win over type  $t = 5\pi/N$  either (this type exists only if  $N \geq 5$ ). That is,

$$v((x'_n, t_n)|5\pi/N) \leq v((x'_n, 2\pi/N)|5\pi/N) \leq v((x^*, 4\pi/N)|5\pi/N).$$

This is equivalent to showing that, for all  $x'_n \in [1/2, 1]$ ,  $v((x'_n, 0)|3\pi/N) \leq v((x^*, 0)|\pi/N)$ . Again, this immediately follows from Lemma B.7. This means that the only possible multi-interval case to consider is the one where  $K = 2$ . In such case, there are exactly two intervals, which we shall denote  $[\bar{t}_l^1, \bar{t}_r^1]$  and  $[\bar{t}_l^2, \bar{t}_r^2]$ . Moreover, it is easy to see that, in this case,  $\bar{t}_l^1 \leq 0$  and  $\bar{t}_r^1 \in [0, 2\pi/N]$ , and that  $\bar{t}_l^2 \geq 2\pi/N$  and  $\bar{t}_r^2 \geq 3\pi/N$ . By Equation (A.5), we need to show that

$$\cos(\bar{t}_r^1 - t'_n) - \cos(\bar{t}_l^1 - t'_n) + \cos(\bar{t}_r^2 - t'_n) - \cos(\bar{t}_l^2 - t'_n) > 0.$$

We first show that  $\cos(\bar{t}_r^2 - t'_n) \geq \cos(\bar{t}_l^1 - t'_n)$ . Suppose not. Then  $v((x'_n, t'_n)|\bar{t}_l^1) > v((x'_n, t'_n)|\bar{t}_r^2)$ . Note that  $v((x'_n, t'_n)|\bar{t}_r^2)$  is bounded below by  $v((x^*, 2\pi/N)|3\pi/N) = v((x^*, 0)|\pi/N)$ . This implies that  $\bar{t}_r^2 - \bar{t}_l^1 > 4\pi/N$ . This is possible only if there exists a  $x'_n$  such that  $v((x'_n, 0)|2\pi/N) > v((x^*, 0)|\pi/N)$ . However, Lemma B.7 shows that this is not possible and, therefore, we must have  $\cos(\bar{t}_r^2 - t'_n) \geq \cos(\bar{t}_l^1 - t'_n)$ .

We now show that  $\cos(\bar{t}_r^1 - t'_n) - \cos(\bar{t}_l^2 - t'_n) > 0$ . There are two cases to consider. If  $t'_n \leq \bar{t}_r^1$ , then  $\bar{t}_r^1 - t'_n < \bar{t}_l^2 - t'_n$ , which immediately implies  $\cos(\bar{t}_r^1 - t'_n) - \cos(\bar{t}_l^2 - t'_n) > 0$ . Therefore, suppose instead that  $t'_n > \bar{t}_r^1$ . Recall that, by definition of  $\bar{t}_r^1$ ,  $v((x'_n, t'_n)|\bar{t}_r^1) = v((x^*, 2\pi/N)|\bar{t}_r^1)$ . Define  $\hat{t} = t'_n + (t'_n - \bar{t}_r^1)$  and  $\tilde{t} = 2\pi/N + (2\pi/N - \bar{t}_r^1)$ . Since  $t'_n < 2\pi/N$ , we have  $\tilde{t} > \hat{t}$ . By the symmetry of the value function,  $v((x'_n, t'_n)|\bar{t}_r^1) = v((x'_n, t'_n)|\hat{t})$  and  $v((x^*, 2\pi/N)|\bar{t}_r^1) = v((x^*, 2\pi/N)|\tilde{t})$ . Therefore, since  $\tilde{t} > \hat{t}$ ,  $v((x^*, 2\pi/N)|\tilde{t}) > v((x^*, 2\pi/N)|\hat{t}) = v((x'_n, t'_n)|\hat{t})$ . This implies that  $\hat{t} < \bar{t}_l^2$ ; hence,  $v((x'_n, t'_n)|\bar{t}_r^1) > v((x'_n, t'_n)|\bar{t}_l^2)$ . We conclude that  $\cos(\bar{t}_r^1 - t'_n) > \cos(\bar{t}_l^2 - t'_n)$ . Q.E.D.

### A.1.3. Proving Theorem 2

LEMMA A.3: *Let  $(x_n, t_n)_{n=1}^N$  be a pure-strategy equilibrium. For all  $n$ , readership  $R_n$  is an interval on the circle.*

PROOF: If  $N = 1$ , there is nothing to prove. Let  $N > 1$  and  $(x_n, t_n)_{n=1}^N$  be a pure-strategy equilibrium. Without loss of generality, let the firms' labels be such that  $x_1 \leq x_2 \leq \dots \leq x_N$ . We divide the proof into three steps. In the first step, we establish that  $R_1$  must be an interval on the circle. In the second step, we let  $N \geq 2$  and assume that  $x_N < 1$ . We establish that if all  $R_m$  are intervals on the circle for  $m < n$ , then  $R_n$  is an interval on the circle as well. In the final step, we prove that when  $N \geq 2$ , for  $(x_n, t_n)_{n=1}^N$  to be an equilibrium, it must be that  $x_N < 1$ .

*Step 1.* We establish that firm 1's readership  $R_1$  is an interval on the circle. Without loss of generality, let us normalize locations in  $(x_n, t_n)_{n=1}^N$  such that  $t_1 = 0$ . By definition of readership,  $R_1 = \{t \in [-\pi, \pi] | v((x_1, t_1 = 0)|t) \geq V((x_n, t_n)_{n \neq 1}|t)\}$ .<sup>23</sup> For each  $n$ , define  $R_{1,n} = \{t \in [-\pi, \pi] | v((x_1, t_1 = 0)|t) \geq v((x_n, t_n)|t)\}$  and note that  $R_1 = \bigcap_{n \neq 1} R_{1,n}$ . Fix an arbitrary  $n \neq 1$ . Since  $x_1 \leq x_n$ , the set  $R_{1,n}$  is an interval by Lemma B.8. Therefore,  $R_1$  is the intersection of finitely many intervals in  $[-\pi, \pi]$ . Hence, it is an interval.

*Step 2.* Fix  $1 < n \leq N$  and suppose that for all firms  $m < n$ ,  $R_m$  is an interval on the circle. Note that when  $N = 2$ , firm 1's readership being an interval on the circle implies that firm 2's readership, the complement of  $R_1$ , is an interval on the circle as well. Therefore, let  $N \geq 3$ . In the proof of this step, we will assume  $x_N < 1$ , a result that we will establish in the next and final step.

By way of contradiction, suppose that firm  $n$ 's readership  $R_n$  is the union of at least two disconnected intervals on the circle denoted  $[\underline{a}, \bar{a}]$  and  $[\underline{b}, \bar{b}]$ . Without loss of generality, let us normalize locations in  $(x_n, t_n)_{n=1}^N$  such that  $t_n = 0$ . Moreover, it is without loss to take  $\bar{a} < \underline{b}$  such that  $R_n \cap (\bar{a}, \underline{b}) = \emptyset$ . Note that it must be that  $\underline{a} \geq -\pi$  and  $\bar{b} \leq \pi$ , with at least one inequality being strict. If this was not the case, that is, if both  $\underline{a} = -\pi$  and  $\bar{b} = \pi$ ,  $[\underline{a}, \bar{a}] \cup [\underline{b}, \bar{b}]$  would represent a single interval on the circle  $[-\pi, \pi]$ —a contradiction. Since  $x_n \leq x_{n'}$  for all  $n' \geq n$ , Lemma B.8 implies that  $\bar{R} = \bigcap_{n' \geq n} R_{n,n'}$  is an interval. Moreover,  $[\underline{a}, \bar{a}] \cup [\underline{b}, \bar{b}] \subseteq \bar{R}$ . Therefore, types in  $(\bar{a}, \underline{b})$  belong to the readership of firms in  $M \subseteq \{1, \dots, n - 1\}$ . By the inductive assumption,  $\{R_m\}_{m \in M}$  are non-overlapping intervals.<sup>24</sup>

Suppose  $M = \{m\}$  is a singleton and, therefore,  $R_m = [\bar{a}, \underline{b}]$ . There are three cases to consider, depending on the location of  $\bar{a}$  and  $\underline{b}$  relative to  $t_n = 0$ .

- Suppose that  $\underline{b} \leq t_n = 0$ . Since  $x_n \leq x_N < 1$ ,  $v((x_n, t_n)|t)$  is strictly increasing for all  $-\pi < t < t_n$ . Therefore,  $v((x_m, t_m)|\bar{a}) = v((x_n, t_n)|\bar{a}) < v((x_n, t_n)|\underline{b}) = v((x_m, t_m)|\underline{b})$ , where the equalities follow from the definition of threshold types. However, by Equation (A.5),  $v((x_m, t_m)|\bar{a}) < v((x_m, t_m)|\underline{b})$  implies that  $\Pi_{t_m} < 0$ . Therefore, firm  $m$  has a profitable deviation in  $t_m$ —a contradiction.
- Suppose, instead, that  $\bar{a} \geq t_n = 0$ . Since  $x_n \leq x_N < 1$ ,  $v((x_n, t_n)|t)$  is strictly decreasing for all  $t_n < t < \pi$ . Therefore,  $v((x_m, t_m)|\bar{a}) = v((x_n, t_n)|\bar{a}) > v((x_n, t_n)|\underline{b}) = v((x_m, t_m)|\underline{b})$ . Therefore, by Equation (A.5),  $\Pi_{t_m} > 0$ . Hence, firm  $m$  has a profitable deviation—a contradiction.
- Finally, suppose that  $\bar{a} < 0 < \underline{b}$ . Equilibrium requires that  $v((x_m, t_m)|\bar{a}) = v((x_n, t_n)|\bar{a}) = v((x_n, t_n)|\underline{b}) = v((x_m, t_m)|\underline{b})$ . This implies that  $t_m = t_n = 0$ . While  $\Pi_{t_m} = 0$ , profits for firm  $m$  are at a local minimum. Suppose firm  $m$  deviates to  $t'_m = t_m + dt_m$ . Such deviation would strictly increase  $v((x_m, t'_m)|\bar{a})$  (since  $v((x_n, t_n)|t)$  is strictly increasing at  $t = \bar{a}$ ) and strictly decreases  $v((x_m, t'_m)|\underline{b})$  (since  $v((x_n, t_n)|t)$  is decreasing at  $t = \bar{a}$ ).

<sup>23</sup>See definitions at the beginning of the Proof of Theorem 1, Part 1.

<sup>24</sup>Whether two intervals  $R_m$  and  $R_{m'}$  overlap at an end point is a matter of convention. This has no bearing on the firms' behavior because a threshold type—namely, the type who is at the boundary of a readership interval—yields a profit of 0 to the firm from which she acquires information.

$t = \underline{b}$ ). Therefore, by Equation (A.5), this implies  $\Pi_{t_m} > 0$ . Hence, firm  $m$  has a profitable deviation—a contradiction.

Suppose  $M$  is not a singleton. Denote by  $m_A$  and  $m_B$  the two firms whose readerships are at opposite extremes of the interval  $(\bar{a}, \underline{b})$ . Since  $m_A, m_B \in M$ ,  $R_{m_A}$  and  $R_{m_B}$  are disjoint intervals in  $(\bar{a}, \underline{b})$ . Therefore, there must be  $\bar{a}' \leq \underline{b}'$  such that  $R_{m_A} = [\bar{a}, \bar{a}']$  and  $R_{m_B} = [\underline{b}', \underline{b}]$ . There are two cases to consider, depending on the location of  $\bar{a}'$  relative to  $t_n = 0$ .

- Suppose  $\bar{a}' \leq t_n = 0$ . Since  $x_n \leq x_N < 1$ ,  $v((x_n, t_n)|t)$  is strictly increasing for all  $-\pi < t < t_n$ . Therefore,  $v((x_{m_A}, t_{m_A})|\bar{a}) = v((x_n, t_n)|\bar{a}) < v((x_n, t_n)|\bar{a}') \leq v((x_{m_A}, t_{m_A})|\bar{a}')$ . The last inequality comes about because if firm  $m_A$  does not share type  $\bar{a}'$  with firm  $n$ , it must be sharing  $\bar{a}'$  with some firm in  $M$  yielding a value higher than  $v((x_n, t_n)|\bar{a}')$ . However, by Equation (A.5),  $v((x_{m_A}, t_{m_A})|\bar{a}) < v((x_{m_A}, t_{m_A})|\bar{a}')$  implies that  $\Pi_{m_A} < 0$ . Therefore, firm  $m_A$  has a profitable deviation—a contradiction.
- Conversely, suppose that  $\bar{a}' > t_n = 0$ . Therefore,  $\underline{b}' \geq \bar{a}' > 0$ . Since  $x_n \leq x_N < 1$ ,  $v((x_n, t_n)|t)$  is strictly decreasing for all  $t_n < t < \pi$ . Therefore,  $v((x_{m_B}, t_{m_B})|\underline{b}') \geq v((x_n, t_n)|\underline{b}') > v((x_n, t_n)|\underline{b}) = v((x_{m_B}, t_{m_B})|\underline{b})$ . The first inequality comes about because if firm  $m_B$  does not share type  $\underline{b}'$  with firm  $n$ , it must be sharing  $\underline{b}'$  with some firm in  $M$  yielding a value higher than  $v((x_n, t_n)|\underline{b}')$ . However, by Equation (A.5),  $v((x_{m_B}, t_{m_B})|\underline{b}) < v((x_{m_B}, t_{m_B})|\underline{b}')$  implies that  $\Pi_{m_B} > 0$ . Therefore, firm  $m_B$  has a profitable deviation—a contradiction.

Therefore,  $R_n$  must be an interval, which concludes the inductive step. By induction,  $R_n$  is an interval for all  $1 \leq n \leq N$ .

*Step 3.* We are left to establish that  $x_N < 1$  and, a fortiori,  $x_n < 1$  for all  $n \leq N$ .<sup>25</sup> To see this, suppose not, that is,  $x_N = 1$ . By the inductive assumption,  $R_n = [\underline{t}_n, \bar{t}_n]$  is an interval on the circle for all  $n < N$ . Since  $x_N = 1$ ,  $v((x_n, t_n)|\bar{t}_n) = 1$  for all  $n$ . For  $n < N$ , denote  $\delta_n = \bar{t}_n - t_n$ . Equation (A.5) requires that  $t_n - \underline{t}_n = \delta_n$  as well. Therefore,  $\delta_n > 0$ ; otherwise firm  $n$  would make zero profits. Using Equation (A.4), the value generated for the threshold type with distance to  $\delta_n$  to the target,  $G(\delta_n)$ , must satisfy

$$G(\delta_n) = \frac{2\delta_n + \sin(2\delta_n)}{2\sqrt{\delta_n^2 + \sin^2(\delta_n)}} = 1.$$

Note that  $\lim_{\delta_n \rightarrow 0^+} G(\delta_n) = \sqrt{2} > 1$  and  $G(\pi/2) < 1$ . Moreover, by Lemma B.9,  $G(\delta_n)$  is strictly decreasing for all  $\delta_n \in (0, \pi/2)$ . Therefore,  $G(\delta_n) = 1$  admits at most one solution in such an interval. It is easy to verify that  $\delta = \frac{\pi}{2} - \frac{\sqrt{3}}{5}$  is such a solution, which is independent of  $n$ . That is, all firms  $n < N$  have a readership of  $2\delta$ . If  $N > 3$ ,  $(N - 1)2\delta > 2\pi$ ; hence, firm  $N$  would make zero profits, a contradiction since  $(x_n, t_n)_{n=1}^N$  is an equilibrium. Thus, the only nontrivial case to consider is  $N = 3$ . Without loss of generality, let  $t_1 < t_2$  and  $t_3 = \frac{1}{2}(t_1 + t_2) = 0$ . Thus,  $t_2 = -t_1$ . Moreover, we can let  $t_2 \geq \pi/2$  (if this was not the case, firm 3 could deviate to  $t'_3 = \pi$  and the argument that follows would hold). Finally, since  $t_2 + \delta \leq \pi$ , let  $t_2 \leq \pi - \delta = \pi/2 + \sqrt{3}/5$ . Therefore,  $t_2 \in [\pi/2, \pi/2 + \sqrt{3}/5]$ . Now consider a deviation  $x'_3$  that is arbitrarily close to 1. If  $(x_n, t_n)_{n=1}^N$  is indeed an equilibrium, such deviation should be weakly unprofitable. We will show instead that it is strictly profitable. Let  $R_2 = [\underline{t}, \bar{t}]$  denote the new readership for firm 2 that such deviation induces.

<sup>25</sup>Note that if  $x_n = 1$  and  $n < N$ , at least two firms,  $n$  and  $N$ , have  $x_n = x_N = 1$ . Therefore, they make zero profits, which is an immediate contradiction

By symmetry,  $R_1 = [-\bar{t}, -\underline{t}]$ . Consider the derivative with respect to  $x_3$  of firm 3's profit function evaluated at  $x'_3$ . Equation (A.3) gives

$$\Pi_{x_3}|_{x'_3} = \frac{1}{2\pi} \left( \frac{1}{2\sqrt{x'_3}} (2\underline{t} + 2(\pi - \bar{t})) - \frac{1}{2\sqrt{1-x'_3}} (2\sin(\underline{t}) - 2\sin(\bar{t})) \right).$$

The first term is bounded above by  $\sqrt{2}\pi$ . The second term grows unboundedly to either plus or minus infinity, as  $x'_3$  is closer to 1. Its sign is equal to the sign of  $\sin(\bar{t}) - \sin(\underline{t})$ . Note that  $t_2 \geq \pi/2$  by assumption, and  $\bar{t} = t_2 + \delta$  and  $\underline{t} = t_2 - \delta$  with  $t_2, \bar{t} \in [0, \pi]$ . Therefore,  $\sin(\bar{t}) - \sin(\underline{t}) < 0$ , implying that the derivative  $\Pi_{x_3}$  is strictly negative when evaluated at a  $x'_3$  that is sufficiently close to 1. Therefore, a small deviation that marginally decreases  $x_3 = 1$  would be profitable for the firm. Q.E.D.

**PROOF OF THEOREM 2:** Let  $N \geq 1$  and consider an arbitrary pure-strategy equilibrium  $(x_n, t_n)_{n=1}^N$ . By Lemma A.3, the readership of firm  $n$  is an interval  $R_n$  on the circle. By Equation (A.5), this implies that each firm is located at the midpoint of its readership interval, that is,  $R_n = [t_n - \delta_n, t_n + \delta_n]$  for some  $\delta_n > 0$ . Moreover, it implies that firm  $n$  sets  $x_n = x^*(\delta_n)$ , the only value of  $x_n$  that solves Equation (A.4), given  $\bar{t}_{n,r} = \delta_n$  and  $\bar{t}_{n,l} = -\delta_n$ . We want to show that  $\delta_n = \delta = \pi/N$  for all  $n$  and, thus,  $x_n = x^*$ . That is,  $(x_n, t_n)_{n=1}^N$  is the equilibrium characterized by Theorem 1.

Suppose that in this equilibrium, there are two firms, 1 and 2, such that  $\delta_1 > \delta_2$ . Without loss of generality, let  $0 = t_1 < t_2$  and suppose these firms are adjacent. That is, type  $\bar{t} = t_1 + \delta_1 = t_2 - \delta_2$  is their threshold type. This implies that  $v((x_1, t_1)|\bar{t}) = v((x_2, t_2)|\bar{t})$ . Since  $\bar{t} - t_n = \delta_n$  and  $x_n = x^*(\delta_n)$  can be expressed in terms of  $\delta_n$  only, we can write  $v((x_n, t_n)|\bar{t})$  as a function of  $\delta_n$ :

$$v((x_1, t_1)|\bar{t}) = \frac{2\delta_1 + \sin(2\delta_1)}{2\sqrt{\delta_1^2 + \sin^2(\delta_1)}} \quad \text{and} \quad v((x_2, t_2)|\bar{t}) = \frac{2\delta_2 + \sin(2\delta_2)}{2\sqrt{\delta_2^2 + \sin^2(\delta_2)}}.$$

Suppose  $\delta_1 \leq \pi/2$  and, a fortiori,  $\delta_2 \leq \pi/2$ . Lemma B.9 shows that this function is strictly decreasing in the interval  $(0, \pi/2)$ . Therefore,  $v((x_1, t_1)|\bar{t}) = v((x_2, t_2)|\bar{t})$  if and only if  $\delta_1 = \delta_2$ —a contradiction.

Suppose instead  $\delta_1 > \pi/2$ . Since the size of the market is  $2\pi$ ,  $\delta_2 \leq \frac{2\pi - 2\delta_1}{2} = \pi - \delta_1 < \pi/2$ . We will show that in this case,  $v((x_1, t_1)|\bar{t}) < v((x_2, t_2)|\bar{t})$ —a contradiction. Note that

$$v((x_2, t_2)|\bar{t}) = \frac{2\delta_2 + \sin(2\delta_2)}{2\sqrt{\delta_2^2 + \sin^2(\delta_2)}} \geq \frac{2(\pi - \delta_1) + \sin(2(\pi - \delta_1))}{2\sqrt{(\pi - \delta_1)^2 + \sin^2(\pi - \delta_1)}},$$

since  $0 < \delta_2 \leq \pi - \delta_1 < \pi/2$  and using Lemma B.9. Put  $y = \pi - \delta_1$  and  $\delta_1 = \pi - y$ . Thus, we need to show that

$$\frac{2y + \sin(2y)}{2\sqrt{y^2 + \sin^2(y)}} > \frac{2(\pi - y) + \sin(2(\pi - y))}{2\sqrt{(\pi - y)^2 + \sin^2(\pi - y)}}.$$

Use  $\sin(2(\pi - y)) = -\sin(2y)$  and  $\sin^2(\pi - y) = \sin^2(y)$  and simplify to obtain

$$\frac{(2y + \sin(2y))^2}{y^2 + \sin^2(y)} > \frac{(2(\pi - y) - \sin(2y))^2}{(\pi - y)^2 + \sin^2(y)}$$

or, equivalently,

$$(2y + \sin(2y))^2((\pi - y)^2 + \sin^2(y)) > (2(\pi - y) - \sin(2y))^2(y^2 + \sin^2(y)).$$

Simplifying, we obtain

$$\begin{aligned} &4y^2 \sin^2(y) + 4y \sin(2y)(\pi - y)^2 + 4y \sin(2y) \sin^2(y) + \sin^2(2y)(\pi - y)^2 \\ &> 4(\pi - y)^2 \sin^2(y) - 4(\pi - y) \sin(2y)(y)^2 - 4(\pi - y) \sin(2y) \sin^2(y) + \sin^2(2y)y^2. \end{aligned}$$

Looking at the last term on both sides, note that  $\sin^2(2y)(\pi - y)^2 > \sin^2(2y)y^2$ , since  $y \in (0, \pi/2)$ . Looking at the second-to-last term on both sides, note that  $4y \sin(2y) \sin^2(y) > -4(\pi - y) \sin(2y) \sin^2(y)$ . Therefore, it is enough to show that in the interval  $y \in (0, \pi/2)$ ,

$$G(y) = y^2 \sin^2(y) + y \sin(2y)(\pi - y)^2 - (\pi - y)^2 \sin^2(y) + (\pi - y) \sin(2y)y^2 > 0.$$

Note that  $G(0) = 0$  and  $G(\pi/2) = 0$ . Moreover, if  $y \in (0, \pi/4)$ , then

$$G'(y) = \sin^2(y)2\pi + 2 \cos(2y)(y(\pi - y)^2 + (\pi - y)y^2) > 0.$$

Therefore,  $G(y)$  is strictly positive for all  $y \in (0, \pi/4)$ . Moreover, if  $y \in (\pi/4, \pi/2)$ , then

$$G''(y) = \sin(2y)2\pi + 2 \cos(2y)((\pi - y)^2 - y^2) - 4 \sin(2y)(y(\pi - y)^2 + (\pi - y)y^2) < 0.$$

This implies that when  $G'(y)$  turns negative, it remains negative. Since  $G(\pi/2) = 0$ , this implies that  $G(y)$  cannot cross zero before  $\pi/2$ .

Therefore,  $G(y) > 0$  for all  $y \in (0, \pi/2)$ . This implies that  $v((x_1, t_1)|\bar{t}) < v((x_2, t_2)|\bar{t})$ —a contradiction. *Q.E.D.*

### A.2. Proofs for Section 4

**PROOF OF PROPOSITION 1:** Let  $(x_n^*, t_n^*)_{n=1}^N$  be an equilibrium with  $N$  firms. From Equation (A.4) in the proof of Theorem 1, we have that  $x_n^* = x^*$  satisfies

$$\sqrt{\frac{1 - x^*}{x^*}} = \frac{\sin(\pi/N)}{\pi/N}.$$

This implies a one-to-one relationship between  $x^*$  and  $N$ , which we denote by  $x^*(N)$ . With a change of variable  $\delta = \pi/N$ , let

$$x^*(\delta) = \frac{\delta^2}{\delta^2 + \sin^2(\delta)}. \tag{A.6}$$

It is enough to show that  $x^*(\delta)$  is strictly increasing in  $\delta$  for all  $\delta \in (0, \pi)$ . Note that

$$\frac{d}{d\delta} x^*(\delta) = \frac{2\delta(\delta^2 + \sin^2(\delta)) - \delta^2(2\delta + 2 \sin(\delta) \cos(\delta))}{(\delta^2 + \sin^2(\delta))^2}.$$

We need to show that for all  $\delta \in (0, \pi)$ ,  $\delta \sin(\delta)(\sin(\delta) - \delta \cos(\delta)) > 0$ . Note that  $\delta \sin(\delta) > 0$  for all  $\delta \in (0, \pi)$ . Therefore, it is enough to show that  $G(\delta) = \sin(\delta) -$

$\delta \cos(\delta) > 0$ . Since  $G(0) = 0$ ,  $G'(\delta) = \cos(\delta) - \cos(\delta) + \delta \sin(\delta) = \delta \sin(\delta) > 0$  for all  $\delta \in (0, \pi)$  implies  $G(\delta) > 0$ . We conclude that  $x^*(\delta)$  is strictly increasing in  $\delta$  for all  $\delta \in (0, \pi)$  or, equivalently,  $x^*(N)$  is strictly decreasing in  $N$  for all  $N > 1$ . *Q.E.D.*

**PROOF OF PROPOSITION 2:** Part (a). Fix  $N \geq 1$ . We begin by computing the  $\mathcal{V}^*(N)$  for an arbitrary pure-strategy equilibrium of the game with  $N$  firms. Let  $(x^*(N), t_n^*)_{n=1}^N$  be the equilibrium profile of editorial strategies and let  $r^*(t_i) \in \{1, \dots, N\}$  be the equilibrium information-acquisition strategy for type  $t_i$ . Then  $\mathcal{V}^*(N) = \mathbb{E}_{t_i}(v(x^*(N), t_{r^*(t_i)}^*)|t_i)$ , where the expectation is taken over  $t_i$ , which is uniformly distributed on  $T = [-\pi, \pi]$ . In equilibrium, we know that  $r^*(t_i) = n$  only if  $t_i \in [t_n^* - \pi/N, t_n^* + \pi/N]$ . Therefore,

$$\begin{aligned} \mathcal{V}^*(N) &= \sum_{n=1}^N \int_{t_n^* - \frac{\pi}{N}}^{t_n^* + \frac{\pi}{N}} v(x^*(N), t_n^*)|t_i \frac{1}{2\pi} dt_i \\ &= N \int_{-\frac{\pi}{N}}^{\frac{\pi}{N}} v(x^*(N), 0)|t_i \frac{1}{2\pi} dt_i \\ &= \lambda \frac{N}{\pi} \left( \sqrt{x^*(N)} \frac{\pi}{N} + \sqrt{1 - x^*(N)} \sin(\pi/N) \right). \end{aligned}$$

The second equality obtains because, thanks to the symmetry in the equilibrium editorial strategies, we can normalize the location of a firm to 0. By substituting the equilibrium value of  $x^*(N)$  (see Equation (A.4)) in the expression above, we obtain

$$\begin{aligned} \mathcal{V}^*(N) &= \lambda \frac{N}{\pi} \sqrt{(\pi/N)^2 + \sin^2(\pi/N)} \\ &= \frac{\lambda}{\sqrt{x^*(N)}}. \end{aligned}$$

The last equality holds by definition of  $x^*(N)$ . We are left to show that  $\mathcal{V}^*(N)$  is strictly increasing in  $N$ . This follows from Proposition 1, since  $x^*(N)$  is strictly decreasing in  $N$ .

Part (b). Fix  $N \geq 1$ . We begin by computing  $\mathcal{P}(N)$  for an arbitrary pure-strategy equilibrium of the game with  $N$  firms. Later, we will show that it is strictly decreasing in  $N$ . Let  $(x^*(N), t_n^*)_{n=1}^N$  be an equilibrium profile of editorial strategies, let  $(p_n^*)_{n=1}^N$  be the equilibrium prices, and let  $r^*(t_i) \in \{1, \dots, N\}$  be the equilibrium information-acquisition strategy for a type  $t_i$ . We have that  $\mathcal{P}(N) = I \cdot \mathbb{E}_{t_i}(p_{r^*(t_i)}^*(t_i)|t_i)$ . Indeed,  $\mathbb{E}_{t_i}(p_{r^*(t_i)}^*(t_i)|t_i)$  is the industry profit generated by one of the  $I$  agents. In equilibrium,  $r^*(t_i) = n$  only if  $t_i \in [t_n^* - \pi/N, t_n^* + \pi/N]$ . Moreover, if  $t_i \in [t_n^* - \pi/N, t_n^* + \pi/N]$ ,  $p_n^*(t_i) = v((x^*(N), t_n^*)|t_i) - \max\{v((x^*(N), t_m^*)|t_i) | m \neq n\}$ . If  $N = 1$ , it is immediate to see that  $\mathcal{P}(1) = I \int_{-\pi}^{\pi} v((1, 0)|t_i) \frac{1}{2\pi} dt_i = \frac{1}{2\sqrt{\pi}}$ . If  $N > 1$ , we can write

$$\begin{aligned} \mathcal{P}(N) &= 2I \sum_{n=1}^N \int_{t_n^*}^{t_n^* + \frac{\pi}{N}} p_n^*(t_i) \frac{1}{2\pi} dt_i \\ &= \frac{2IN}{2\pi} \int_0^{\frac{\pi}{N}} v(x^*(N), 0)|t_i - v(x^*(N), 2\pi/N)|t_i dt_i \end{aligned}$$

$$\begin{aligned} &= \frac{1}{2\sqrt{\pi}} \sqrt{1 - x^*(N)} \frac{2 \sin\left(\frac{\pi}{N}\right) - \sin\left(\frac{2\pi}{N}\right)}{\pi/N} \\ &= \frac{1}{\sqrt{\pi}} \frac{1 - x^*(N)}{\sqrt{x^*(N)}} (1 - \cos(\pi/N)). \end{aligned}$$

The last equality obtains by using Equation (A.4). We want to show that  $\mathcal{P}(N)$  is strictly decreasing in  $N$ . With a change of variable, let  $\delta = \pi/N \in (0, \pi]$ . Using Equation (A.6), we can rewrite  $\mathcal{P}(N)$  as

$$\mathcal{P}(\delta) = \frac{1}{\sqrt{\pi}} \frac{\sin^2(\delta)}{\delta} \frac{1 - \cos(\delta)}{\sqrt{\delta^2 + \sin^2(\delta)}}.$$

Using the expression above, it is immediate to compute  $\mathcal{P}(\frac{\pi}{2})$  and verify that it is strictly smaller than  $\mathcal{P}(\pi)$ . Similarly, we can directly verify that  $\mathcal{P}(\frac{\pi}{4}) < \mathcal{P}(\frac{\pi}{3}) < \mathcal{P}(\frac{\pi}{2})$ . We are left to show that  $\mathcal{P}(\delta)$  is strictly increasing for all  $\delta \in (0, \pi/4]$ . Note that  $\mathcal{P}(\delta) > 0$  for all  $\delta \in (0, \pi/4]$ . Therefore, it is enough to show that  $(\mathcal{P}(\delta))^2$  is strictly increasing. Dropping the constant and replacing variable  $\delta$  with  $x$ , let

$$G(x) = \frac{\sin^4(x)(1 - \cos(x))^2}{x^2(\sin^2(x) + x^2)}.$$

Since  $\lim_{x \rightarrow 0} G(x) = 0$ , it is enough to show that  $G'(x) > 0$  for all  $x \in (0, \pi/4]$ . The sign of  $G'(x)$  is determined by the sign of its numerator, which is

$$\begin{aligned} &(4 \sin^3(x) \cos(x)(1 - \cos(x))^2 + \sin^5(x)2(1 - \cos(x)))(x^2(\sin^2(x) + x^2)) \\ &- (\sin^4(x)(1 - \cos(x))^2)(2x(\sin^2(x) + x^2) + x^2(2x + 2 \sin(x) \cos(x))). \end{aligned}$$

Dividing everything by  $2 \sin^3(x)(1 - \cos(x))x$ , which is strictly positive for  $x \in (0, \pi/4]$ , we obtain

$$\begin{aligned} &(2 \cos(x)(1 - \cos(x)) + \sin^2(x))(x(\sin^2(x) + x^2)) \\ &- (\sin(x)(1 - \cos(x)))(2x^2 + \sin^2(x) + x \sin(x) \cos(x)) \\ &= (1 - \cos(x))(3 \cos(x) + 1)(x(\sin^2(x) + x^2)) \\ &- (\sin(x)(1 - \cos(x)))(2x^2 + \sin^2(x) + x \sin(x) \cos(x)). \end{aligned}$$

The equality holds since  $\sin^2(x) = 1 - \cos^2(x) = (1 - \cos(x))(1 + \cos(x))$ . We can further divide the last expression by  $1 - \cos(x) > 0$  to obtain

$$\begin{aligned} &(1 + 3 \cos(x))(x \sin^2(x) + x^3) - \sin(x)(2x^2 + \sin^2(x) + x \sin(x) \cos(x)) \\ &= x \sin^2(x) + 2 \cos(x)x \sin^2(x) + (1 + 3 \cos(x))x^3 - \sin(x)2x^2 - \sin^3(x) \end{aligned}$$

$$\begin{aligned}
 &> x \sin^2(x) + 2 \cos(x)x \sin^2(x) + 3 \cos(x)x^3 - \sin(x)2x^2 \\
 &> 3 \cos(x)x^3 - \sin(x)2x^2 \\
 &> 0.
 \end{aligned}$$

The first inequality holds because  $x > \sin(x)$  if  $x \in (0, \pi/4]$ . Similarly, the second inequality holds because  $x \sin^2(x) \geq 0$  and  $2 \cos(x)x \sin^2(x) > 0$  in the same range. The last inequality holds because  $3 \cos(x)x^3 - \sin(x)2x^2 > 0$  if and only if  $3 \cos(x) - 2 \frac{\sin(x)}{x} > 0$ . Since  $x > \sin(x)$ ,  $3 \cos(x) - 2 \frac{\sin(x)}{x} > 3 \cos(x) - 2 > 0$ , which holds true for  $\delta \in (0, \pi/4]$ . Therefore,  $G'(x) > 0$  for all  $x \in (0, \pi/4]$ . Hence,  $G(x)$  is strictly increasing in  $x$  and, equivalently,  $\mathcal{P}(\delta)$  is strictly increasing in  $\delta \in (0, \pi/4]$ . Q.E.D.

**PROOF OF REMARK 2:** Fix an arbitrary type  $t_i$ . The value of information for type  $t_i$  at an arbitrary equilibrium  $(x^*(N), t_n^*)_{n=1}^N$  is bounded below by  $\underline{v}_N = \lambda(\sqrt{x^*(N)} + \sqrt{1 - x^*(N)} \cos(\pi/N))$  and it is bounded above by  $\hat{v}_N = \lambda(\sqrt{x^*(N)} + \sqrt{1 - x^*(N)})$ . Equation (A.4) implies that  $\lim_{N \rightarrow \infty} x^*(N) = 1/2$ . Therefore,  $\lim_{N \rightarrow \infty} \underline{v}_N = \lim_{N \rightarrow \infty} \hat{v}_N = \lambda\sqrt{2}$ . This implies that  $v((x^*(N), t_{r^*(t_i)}^*)|t_i)$  converges to  $\lambda\sqrt{2}$  as  $N \rightarrow \infty$ . Finally, note that  $\lambda\sqrt{2}$  is the first-best value of information of an agent of type  $t_i$ , namely  $\max_{(x_n, t_n)} v((x_n, t_n)|t_i) = \lambda\sqrt{2}$ . Q.E.D.

**PROOF OF PROPOSITION 3:** Fix  $N \geq 1$  and let  $(x^*(N), t_n^*)_n$  be the equilibrium profile of editorial strategies. Consider two agents  $t_i$  and  $t_j$ , and suppose that, in equilibrium, they acquire information from firms  $n$  and  $m$ , respectively. Denote  $s_i = s_i(\omega, x^*(N), t_n^*)$  the signal that agent  $i$  receives,  $z_i = \mathbb{E}_\omega(u(\omega, t_i)|s_i)$  her expected utility, and  $v_i = v((x^*(N), t_n^*)|t_i)$ . Using Equation (A.1) and Remark 1, we have that

$$z_i = \frac{v_i}{\lambda} (\sqrt{x^*(N)}\omega_0 + \sqrt{1 - x^*(N)}(\omega_1 \cos(t_n^*) + \omega_2 \sin(t_n^*)) + \varepsilon_i) \sim \mathcal{N}(0, 2v_i^2/\lambda^2).$$

Therefore, the correlation between  $z_i$  and  $z_j$  is given by

$$\begin{aligned}
 \rho_{z_i, z_j} &= \frac{\lambda^2 \text{Cov}(z_i, z_j)}{2v_i v_j} \\
 &= \frac{1}{2v_i v_j \lambda^2} v_i v_j \lambda^2 (x^*(N) + (1 - x^*(N))(\cos(t_n^*) \cos(t_m^*)) + \sin(t_n^*) \sin(t_m^*)) \\
 &= \frac{1}{2} (x^*(N) + (1 - x^*(N)) \cos(t_n^* - t_m^*)).
 \end{aligned}$$

Next, we let the type  $t_i$  of agent  $i$  be uniformly drawn from the type space  $T$ . In this case, the firm  $n$  that agent  $i$  chooses is random. However, since in equilibrium firms are spread out evenly, agent  $i$  is equally likely to choose any of the  $N$  firms. Therefore,

$$\begin{aligned}
 \mathbb{E}_{t_i, t_j} \rho_{z_i, z_j} &= \frac{1}{2} x^*(N) + (1 - x^*(N)) \mathbb{E}_{t_j} \mathbb{E}_{t_i} (\cos(t_n^* - t_m^*)) \\
 &= \frac{1}{2} x^*(N) + (1 - x^*(N)) \frac{1}{2N^2} \sum_{n=1}^N \sum_{m=1}^N (\cos(t_n^* - t_m^*)).
 \end{aligned}$$

We are going to show that  $\sum_{n=1}^N \sum_{m=1}^N (\cos(t_n^* - t_m^*)) = 0$ . Without loss of generality, we can normalize the location of firm  $n = 1$  to be  $t_1^* = 0$ . As a consequence,  $t_n^* = \frac{2\pi(n-1)}{N}$  for all  $n$ . Therefore, letting  $\delta = 2\pi/N$ ,

$$\begin{aligned} \sum_{n=1}^N \sum_{m=1}^N (\cos(t_n^* - t_m^*)) &= \sum_{n=0}^{N-1} \sum_{m=0}^{N-1} \cos((n-1)\delta - (m-1)\delta) \\ &= \sum_{n=1}^N \sum_{m=1}^N \cos((n-m)\delta) \\ &= \sum_{n=1}^N \sum_{k=n-N}^{n-1} \cos(k\delta) \\ &= \sum_{n=1}^N \left( \sum_{k=n-N}^0 \cos(k\delta) + \sum_{k=1}^{n-1} \cos(k\delta) \right). \end{aligned}$$

The second-to-last equality follows from the substitution  $k = n - m$ . The lower and upper indexes of the summation are substituted accordingly. The highest possible  $m$  is  $N$  and it leads to the lower index  $n - N$ . The lowest possible  $m$  is 1 and it leads to the highest index  $n - 1$ . The last equality follows from splitting in two the summation  $\sum_{k=n-N}^{n-1} \cos(k\delta)$ . This separates the terms with  $k \leq 0$  and  $k > 0$ .

Using  $N\delta = 2\pi$  and  $\cos(y) = \cos(y + 2\pi)$  for all  $y \in \mathbb{R}$ , we have

$$\sum_{k=n-N}^0 \cos(k\delta) = \sum_{k=n-N}^0 \cos(k\delta + N\delta) = \sum_{k=n-N}^0 \cos((k+N)\delta) = \sum_{k=n}^N \cos(k\delta).$$

Thus,

$$\begin{aligned} \sum_{n=1}^N \sum_{m=1}^N (\cos(t_n^* - t_m^*)) &= \sum_{n=1}^N \left( \sum_{k=n-N}^0 \cos(k\delta) + \sum_{k=1}^{n-1} \cos(k\delta) \right) \\ &= \sum_{n=1}^N \left( \sum_{k=n}^N \cos(k\delta) + \sum_{k=1}^{n-1} \cos(k\delta) \right) \\ &= \sum_{n=1}^N \sum_{k=1}^N \cos(k\delta) \\ &= N \sum_{k=1}^N \cos(k\delta) \end{aligned}$$

$$\begin{aligned}
 &= N \left( -\frac{1}{2} + \frac{\sin\left(\left(N + \frac{1}{2}\right)\frac{2\pi}{N}\right)}{2 \sin\left(\frac{\pi}{N}\right)} \right) \\
 &= N \left( -\frac{1}{2} + \frac{\sin\left(\frac{\pi}{N}\right)}{2 \sin\left(\frac{\pi}{N}\right)} \right) = 0.
 \end{aligned}$$

The third-to-last row follows from the Lagrange’s trigonometric identity. The last row, instead, uses  $\sin(y + 2\pi) = \sin(y)$  for all  $y \in \mathbb{R}$ .

Therefore, we conclude that  $\mathbb{E}_{t_i, t_j} \rho_{z_i, z_j} = \frac{1}{2} x^*(N)$ , which is strictly decreasing in  $N$  by Proposition 1. Q.E.D.

**PROOF OF PROPOSITION 4:** Fix arbitrary  $I$  and  $N$ . Let  $(x^*(N), t_n^*, p_n^*)_{n=1}^N$  be the equilibrium profile of editorial strategies and prices. Let  $r^*(t_i) \in \{1, \dots, N\}$  be the equilibrium information-acquisition strategy for a type  $t_i$ . Our first goal is to compute the agent’s expected welfare  $\mathcal{U}(N)$ . Fix a realization of agents’ types  $t = (t_1, \dots, t_I)$ . We have that

$$\mathcal{U}(N|t) = \mathbb{E}_\omega(A_{-i}^*(\omega, t_{-i})u(\omega, t_i)) + v((x^*(N), t_n^*)|t_i) - p_n^*(t_i).$$

Therefore, the agent’s expected welfare is

$$\mathcal{U}(N) = \mathbb{E}_{(t_1, \dots, t_I)}(\mathbb{E}_\omega(A_{-i}^*(\omega, t_{-i})u(\omega, t_i)) + v((x^*(N), t_{r^*(t_i)}^*)|t_i) - p_{r^*(t_i)}^*(t_i)).$$

Note that the first term corresponds to the indirect value of information,  $\mathcal{G}(N)$ , the second term to the direct value of information,  $\mathcal{V}^*(N)$ , and the last term is the expected price,  $\mathcal{P}(N)$ . To compute  $\mathcal{U}(N)$ , we proceed in steps. First, by the proof of Proposition 2(a), we have that

$$\mathcal{V}(N) = \mathbb{E}_{(t_1, \dots, t_I)}(v((x^*(N), t_{r^*(t_i)}^*)|t_i)) = \mathbb{E}_{t_i}(v((x^*(N), t_{r^*(t_i)}^*)|t_i)) = \mathcal{V}^*(N) = \frac{\lambda}{\sqrt{x^*(N)}}.$$

Second, we focus on  $\mathcal{P}$ . When  $N = 1$ , note that  $\frac{\mathcal{P}(1)}{I} = \lambda$ . If  $N \geq 2$ , instead, from the proof of Proposition 2(b), we know that

$$\mathbb{E}_{(t_1, \dots, t_I)}(p_{r^*(t_i)}^*(t_i)) = \mathbb{E}_{t_i}(p_{r^*(t_i)}^*(t_i)) = \frac{\mathcal{P}(N)}{I} = 2\lambda \frac{1 - x^*(N)}{\sqrt{x^*(N)}} (1 - \cos(\pi/N)).$$

Last, we focus on the firm term of  $\mathcal{U}(N)$ . We have

$$\begin{aligned}
 \mathcal{G}(N) &= \mathbb{E}_{(t_1, \dots, t_I)}(\mathbb{E}_\omega(A_{-i}^*(\omega, t_{-i})u(\omega, t_i))) \\
 &= \mathbb{E}_{t_{-i}}(\mathbb{E}_\omega(A_{-i}^*(\omega, t_{-i})\mathbb{E}_{t_i}u(\omega, t_i))) \\
 &= \mathbb{E}_{t_{-i}}(\mathbb{E}_\omega(A_{-i}^*(\omega, t_{-i})\omega_0)) \\
 &= \mathbb{E}_{\omega_0}(\omega_0 \mathbb{E}_{t_{-i}}(\mathbb{E}_{(\omega_1, \omega_2)}(A_{-i}^*(\omega, t_{-i}))))),
 \end{aligned} \tag{A.7}$$

where the second equality holds since  $\mathbb{E}_{t_i} u(\omega, t_i) = \omega_0 + \frac{\omega_1}{2\pi} \int_{-\pi}^{\pi} \cos(t_i) dt_i + \frac{\omega_2}{2\pi} \times \int_{-\pi}^{\pi} \sin(t_i) dt_i = \omega_0$ . Next, let us focus on the two innermost expectations in the last expression. Recall that  $A_{-i}^*(\omega, t_{-i})$  is defined as  $\frac{1}{I} \sum_{j \neq i} a_j^*(\omega, t_j)$ , where  $a_j^*(\omega, t_j)$  is the equilibrium approval decision of agent  $j$ . By Lemma B.10, we have

$$\begin{aligned} &\mathbb{E}_{\omega_1, \omega_2, t_{-i}} A_{-i}^*((\omega_0, \omega_1, \omega_2), t_{-i})) \\ &= \mathbb{E}_{\omega_1, \omega_2, t_{-i}} \frac{1}{I} \sum_{j \neq i} a_j^*(\omega, t_j) = \frac{1}{I} \sum_{j \neq i} \mathbb{E}_{\omega_1, \omega_2, t_{-i}} a_j^*(\omega, t_j) \\ &= \frac{1}{I} \sum_{j \neq i} \bar{a}_j(\omega_0) = \frac{I-1}{I} \Phi\left(\frac{\sqrt{x^*(N)}}{\sqrt{2-x^*(N)}} \omega_0\right). \end{aligned} \tag{A.8}$$

Putting Equations (A.7) and (A.8) together, we obtain

$$\mathcal{G}(N) = \frac{I-1}{I} \mathbb{E}_{\omega_0} \left( \omega_0 \Phi\left(\frac{\sqrt{x^*(N)}}{\sqrt{2-x^*(N)}} \omega_0\right) \right).$$

Next, we use the integral identity  $\int_{\mathbb{R}} y \Phi(\gamma y) \phi(y) dy = \frac{\gamma}{\sqrt{2\pi(1+\gamma^2)}}$  (see Patel and Read (1996)) and let  $y = \omega_0$  and  $\gamma = \sqrt{x^*(N)}/\sqrt{2-x^*(N)}$  to obtain

$$\mathcal{G}(N) = \frac{I-1}{2I\sqrt{\pi}} \sqrt{x^*(N)} = (I-1)\lambda \sqrt{x^*(N)}.$$

Therefore, we established that, if  $N \geq 2$ , then

$$\mathcal{U}(N) = \lambda \left( (I-1)\sqrt{x^*(N)} + \frac{1}{\sqrt{x^*(N)}} - 2\frac{1-x^*(N)}{\sqrt{x^*(N)}}(1-\cos(\pi/N)) \right), \tag{A.9}$$

whereas  $\mathcal{U}(1) = \lambda(I-1)$  when  $N = 1$ .

The second part of the proof consists of showing that, when letting  $\bar{I} = 3(1+2\pi)$  and  $I > \bar{I}$ ,  $\mathcal{U}(N)$  is strictly decreasing in  $N$ . It can be directly verified that  $\mathcal{U}(2) < \mathcal{U}(1)$  when  $I > 4 = \bar{I}$ . Therefore, the rest of the proof focuses on the case  $N \geq 2$ . To this purpose, let us ignore the constant term  $\lambda$  in  $\mathcal{U}(N)$ , let  $\delta = \pi/N$ , and let us write  $x$  in place of  $x^*(N)$ , thus leaving the dependence on  $\delta$  implicit. Our goal is to show that

$$G(\delta) = (I-1)\sqrt{x} + \frac{1}{\sqrt{x}} - 2\frac{1-x}{\sqrt{x}}(1-\cos(\delta))$$

is strictly increasing in  $\delta \in (0, \pi/2]$ . Taking the derivative with respect to  $\delta$ , we obtain

$$\begin{aligned} G'(\delta) &= \frac{1}{2}x^{-3/2}((I-1)x-1)x' + 2(1-\cos(\delta))\frac{x'}{x} \frac{1+x}{2\sqrt{x}} - 2\frac{1-x}{\sqrt{x}} \sin(\delta) \\ &\geq \frac{1}{2}x^{-3/2}((I-1)x-1)x' - 2\frac{1-x}{\sqrt{x}} \sin(\delta) \\ &= 2\frac{1-x}{\sqrt{x}} \left( \frac{1}{4(1-x)} \frac{x'}{x} ((I-1)x-1) - \sin(\delta) \right). \end{aligned}$$

The inequality holds since the middle term in the first expression is positive (by Proposition 1,  $x$  is strictly increasing in  $\delta$  and, thus,  $x' > 0$ ). Therefore, it is sufficient to show that

$$\frac{1}{4(1-x)} \frac{x'}{x} ((I-1)x - 1) - \sin(\delta) > 0.$$

Note that

$$x' = \frac{d}{d\delta} \left( \frac{\delta^2}{\delta^2 + \sin^2(\delta)} \right) = \frac{2\delta(\sin^2(\delta) - \delta \sin(\delta) \cos(\delta))}{(\delta^2 + \sin^2(\delta))^2} = \frac{2x (\sin^2(\delta) - \delta \sin(\delta) \cos(\delta))}{\delta (\delta^2 + \sin^2(\delta))}.$$

By substituting  $x'$  into the previous inequality and letting  $C = \frac{(I-1)x-1}{2(1-x)}$ , we obtain

$$\frac{\sin(\delta)}{\delta^2 + \sin^2(\delta)} (C(\sin(\delta) - \delta \cos(\delta)) - \delta^3 - \delta \sin^2(\delta)) > 0.$$

Since  $\frac{\sin(\delta)}{\delta^2 + \sin^2(\delta)} > 0$  for all  $\delta \in (0, \pi]$ , the proof is complete if we show that

$$F(\delta) = C(\sin(\delta) - \delta \cos(\delta)) - \delta^3 - \delta \sin^2(\delta) > 0.$$

To this purpose note that  $F(0) = 0$ . Moreover,

$$\begin{aligned} F'(\delta) &= \delta C \sin(\delta) - 3\delta^2 - \sin^2(\delta) - 2\delta \sin(\delta) \cos(\delta) \\ &= \delta^2 \left( C \frac{\sin(\delta)}{\delta} - 3 - \left( \frac{\sin(\delta)}{\delta} \right)^2 - 2 \cos(\delta) \frac{\sin(\delta)}{\delta} \right) \\ &\geq \delta^2 \left( \frac{2C}{\pi} - 6 \right) \\ &\geq \delta^2 \frac{I - 3(1 + 2\pi)}{\pi} > 0. \end{aligned}$$

The first inequality holds because  $\cos(\delta) \leq 1$  and  $\frac{\sin(\delta)}{\delta} \in [\frac{2}{\pi}, 1]$  for all  $\delta \in (0, \pi/2]$ . The second-to-last inequality holds instead because  $C$  is bounded below by  $C \geq \frac{(I-3)}{2}$  (since  $x \geq 1/2$ ). The last inequality holds because, by assumption,  $I > \bar{I} = 3(1 + 2\pi)$ . Therefore,  $F'(\delta) > 0$  for all  $\delta \in (0, \pi/2]$  and, thus,  $F(\delta) > 0$ . This implies that  $G'(\delta) > 0$  and, thus, that  $G(\delta)$  is strictly increasing for all  $\delta \in (0, \pi/2]$ . Hence, we conclude that  $\mathcal{U}(N)$  is strictly decreasing in  $N$  for all  $N \geq 1$ . Q.E.D.

**COROLLARY 1:** For  $I \geq 3$ ,  $\mathcal{V}(N) + \mathcal{G}(N)$  is decreasing in  $N$ .

**PROOF:** As shown in the proof of Proposition 4,  $\mathcal{V}(N) + \mathcal{G}(N) = \lambda \left( \frac{1}{\sqrt{x^*(N)}} + (I - 1) \sqrt{x^*(N)} \right)$ . The sign of the derivative with respect to  $N$  is determined by  $\left( \frac{-1}{x^*(N)} + (I - N) \right) \frac{dx^*(N)}{N}$ . Since  $x^*(N) > 0.5$ , the first term in the parentheses is positive whenever  $I \geq 3$ . Thus, the result follows from Proposition 1 which establishes  $x^*(N)$  to be decreasing in  $N$ . Q.E.D.

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